

Machine Learning in Compilers

Program Analyses and Optimizations - DCC888

Fernando Magno Quintão Pereira

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What is Machine Learning?

What is Machine Learning?

▶ Program Synthesis

What is Machine Learning?

▶ ~~Program~~ Function Synthesis

What is Machine Learning?

▶ ~~Program~~ Function Synthesis - From Examples

What is Machine Learning?

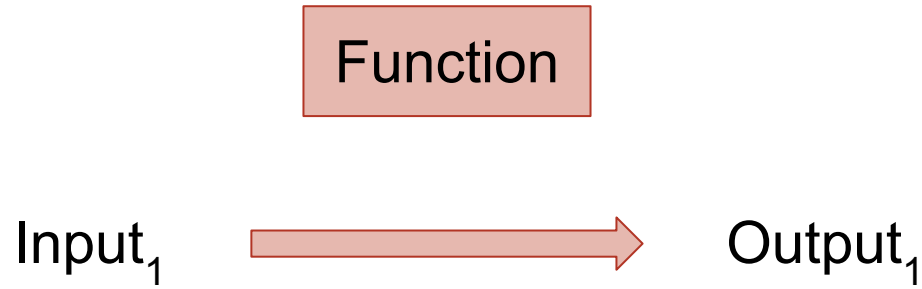
▶ ~~Program~~ Function Synthesis - From Examples

Function

???

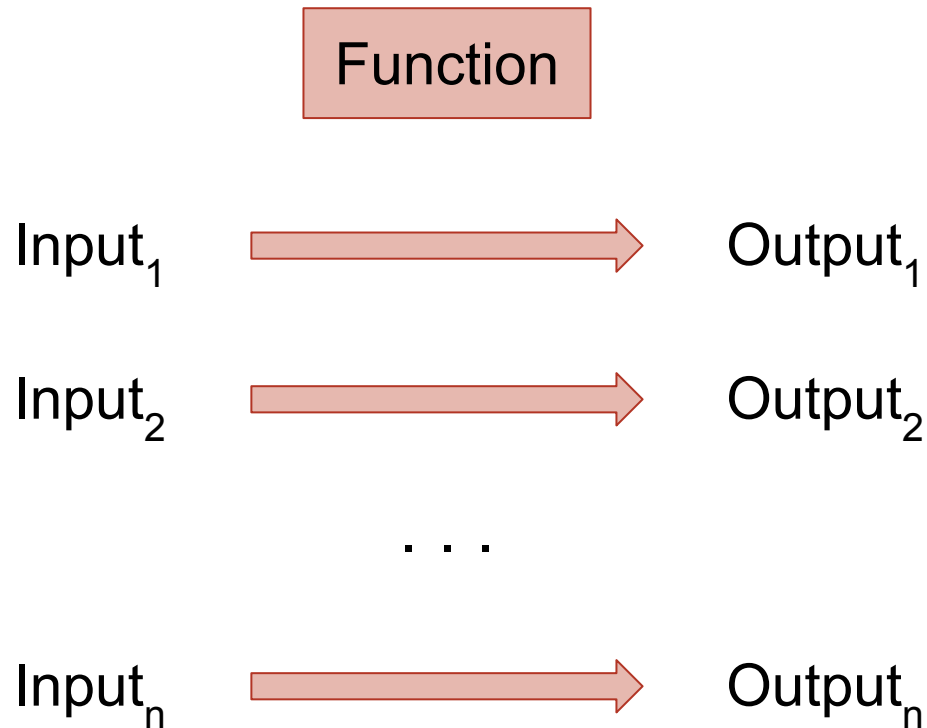
What is Machine Learning?

▶ ~~Program~~ Function Synthesis - From Examples



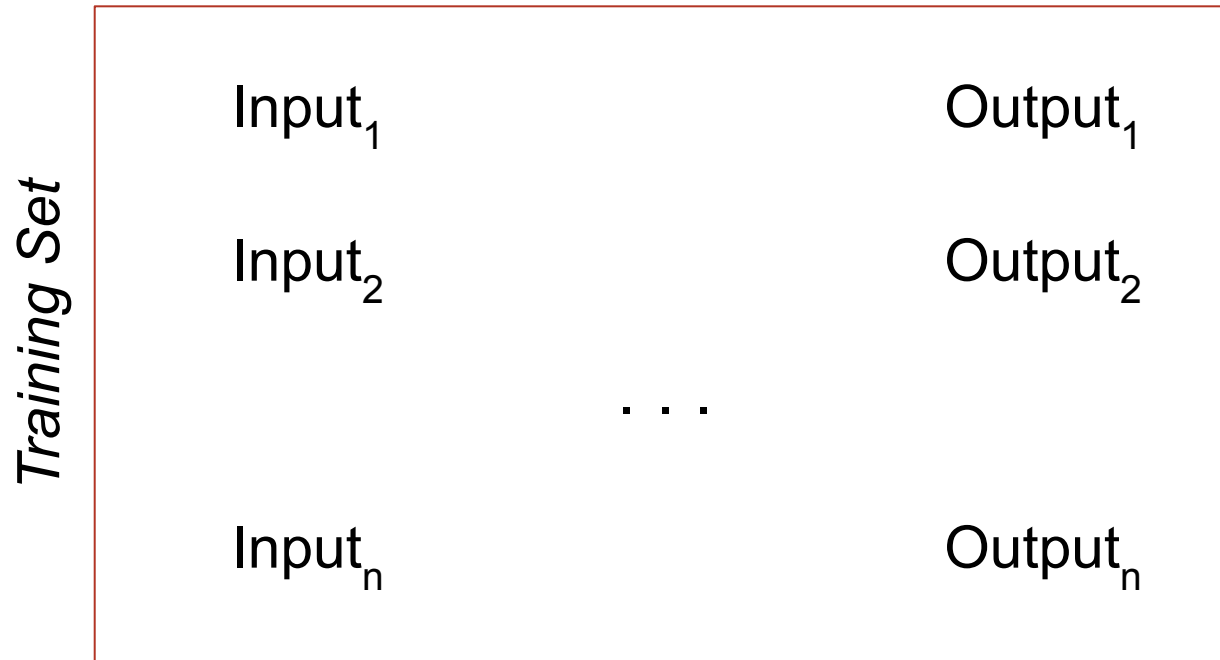
What is Machine Learning?

▶ ~~Program~~ Function Synthesis - From Examples



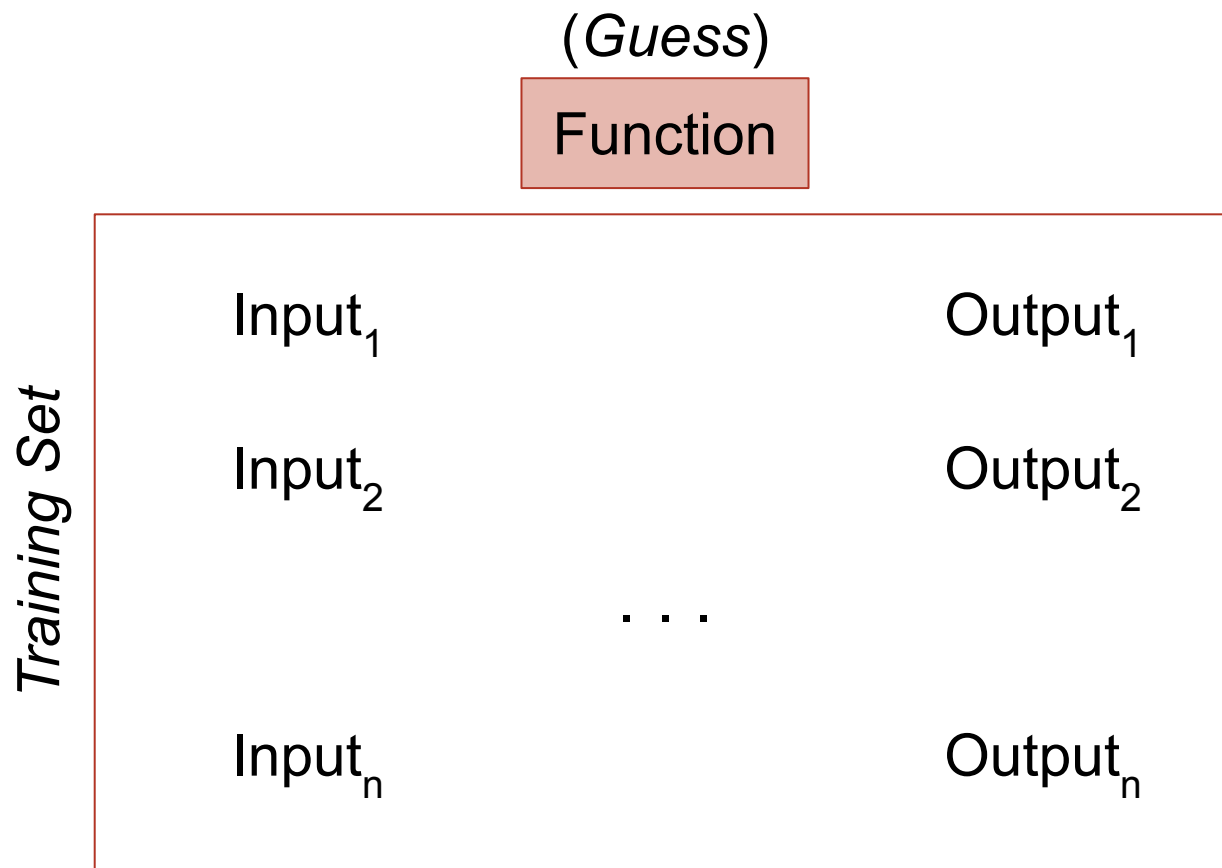
What is Machine Learning?

▶ ~~Program~~ Function Synthesis - From Examples



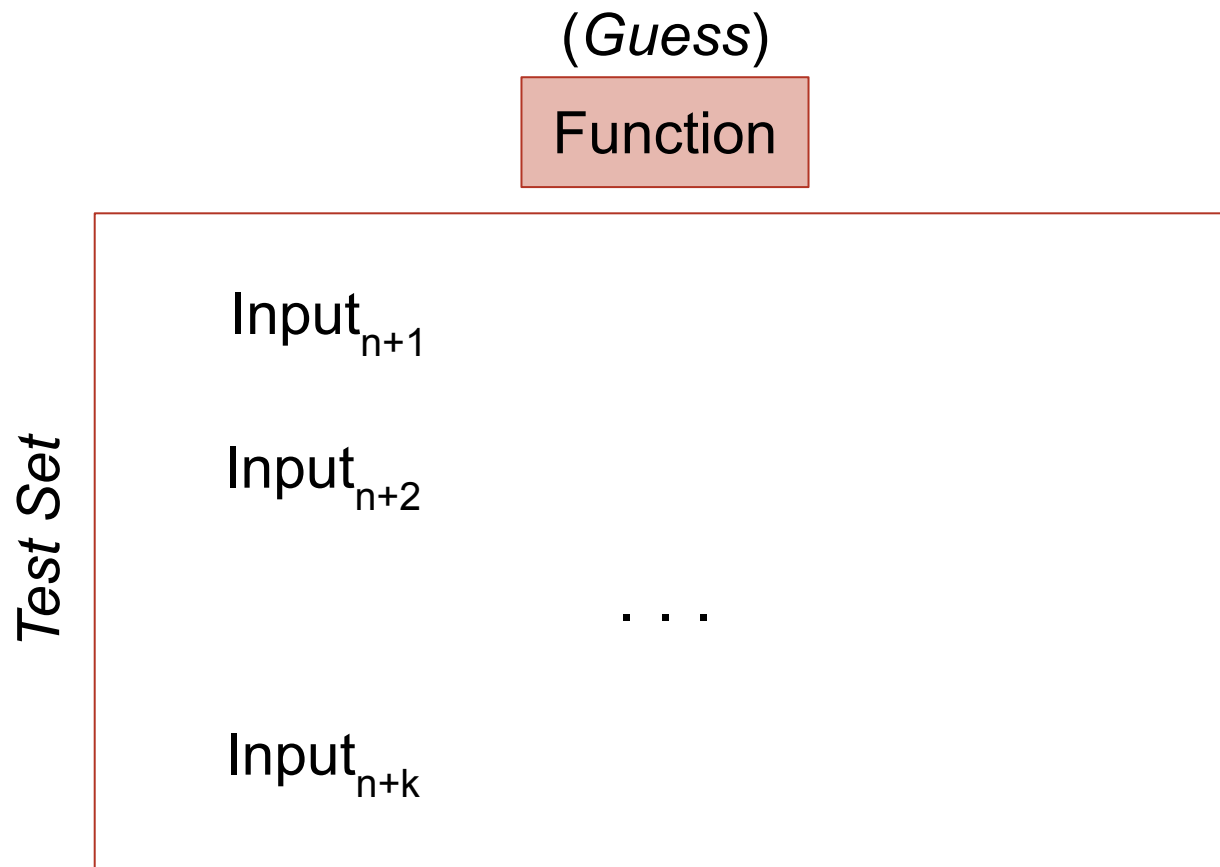
What is Machine Learning?

▶ ~~Program~~ Function Synthesis - From Examples



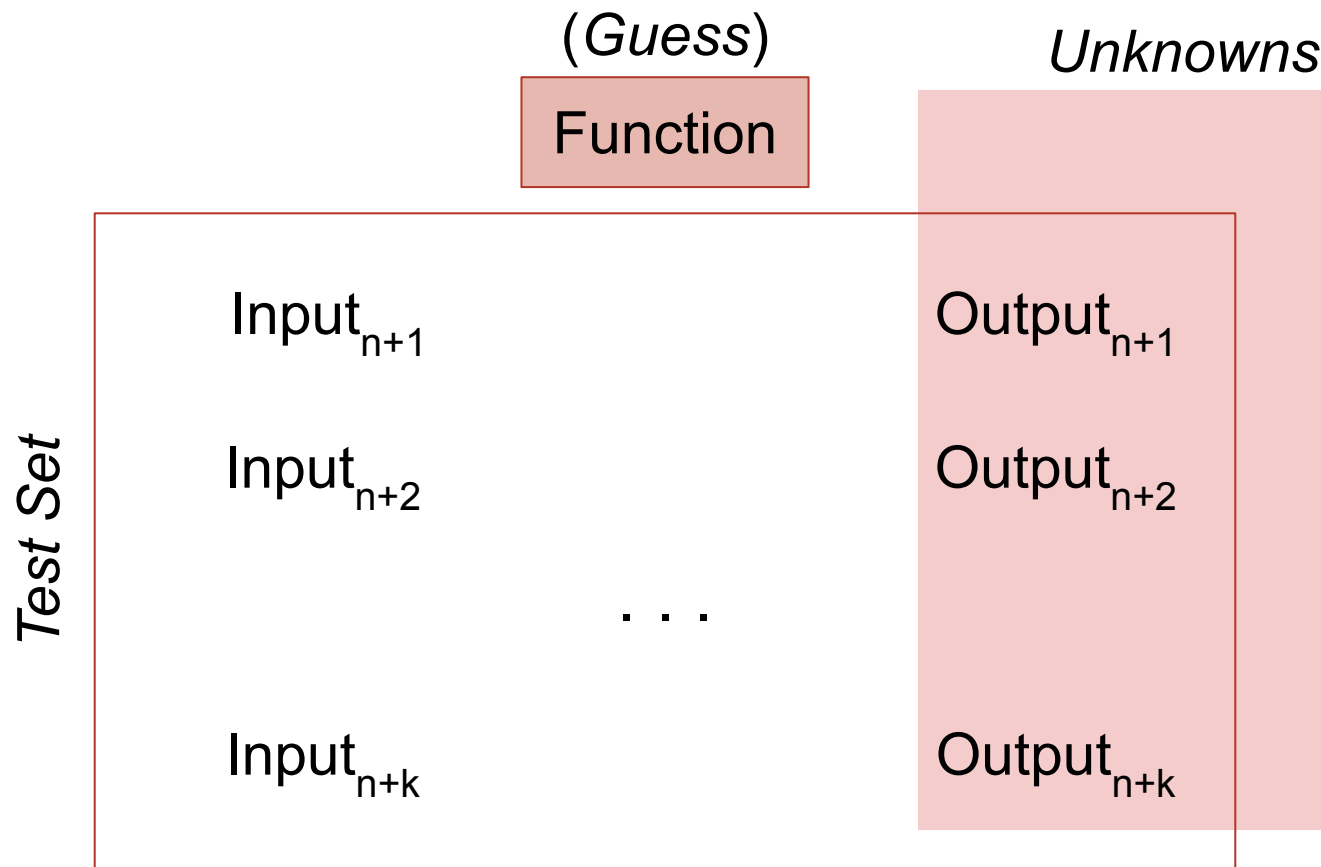
What is Machine Learning?

▶ ~~Program~~ Function Synthesis - From Examples



What is Machine Learning?

▶ ~~Program~~ Function Synthesis - From Examples



Why is this Process Stochastic?

Why is this Process Stochastic?

- ▶ Approximations are acceptable

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- ▶ Approximations are acceptable
- ▶ The exact function might not exist

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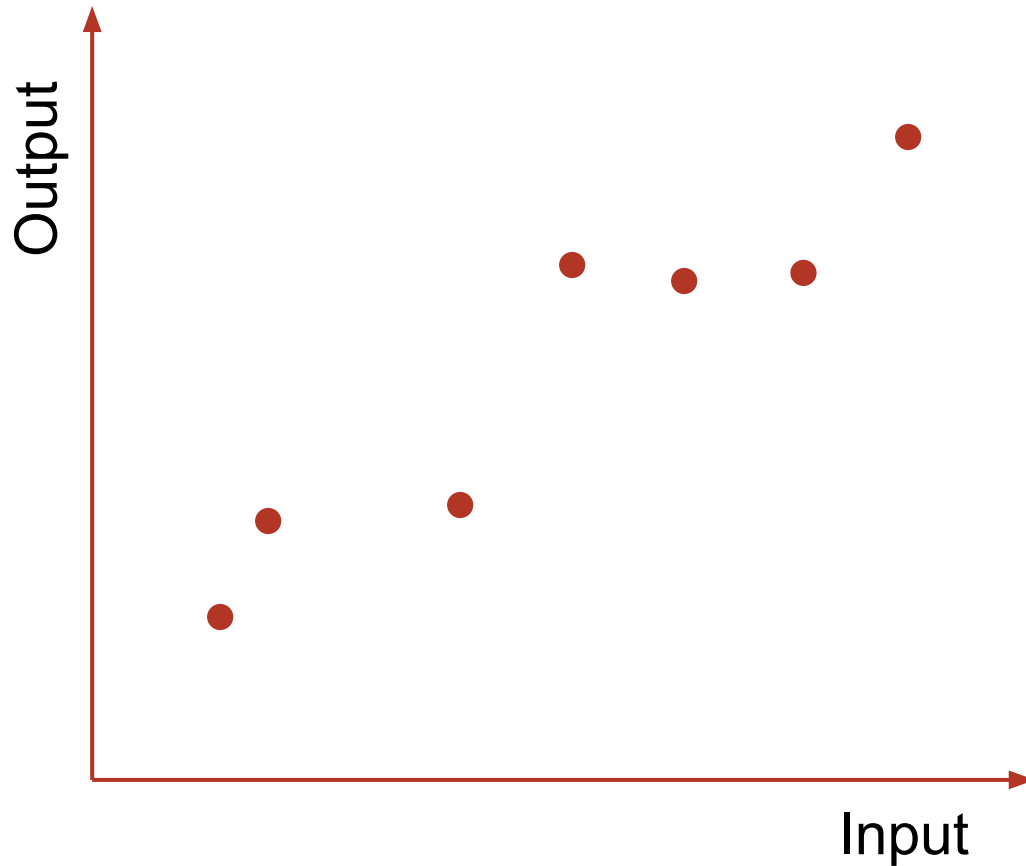
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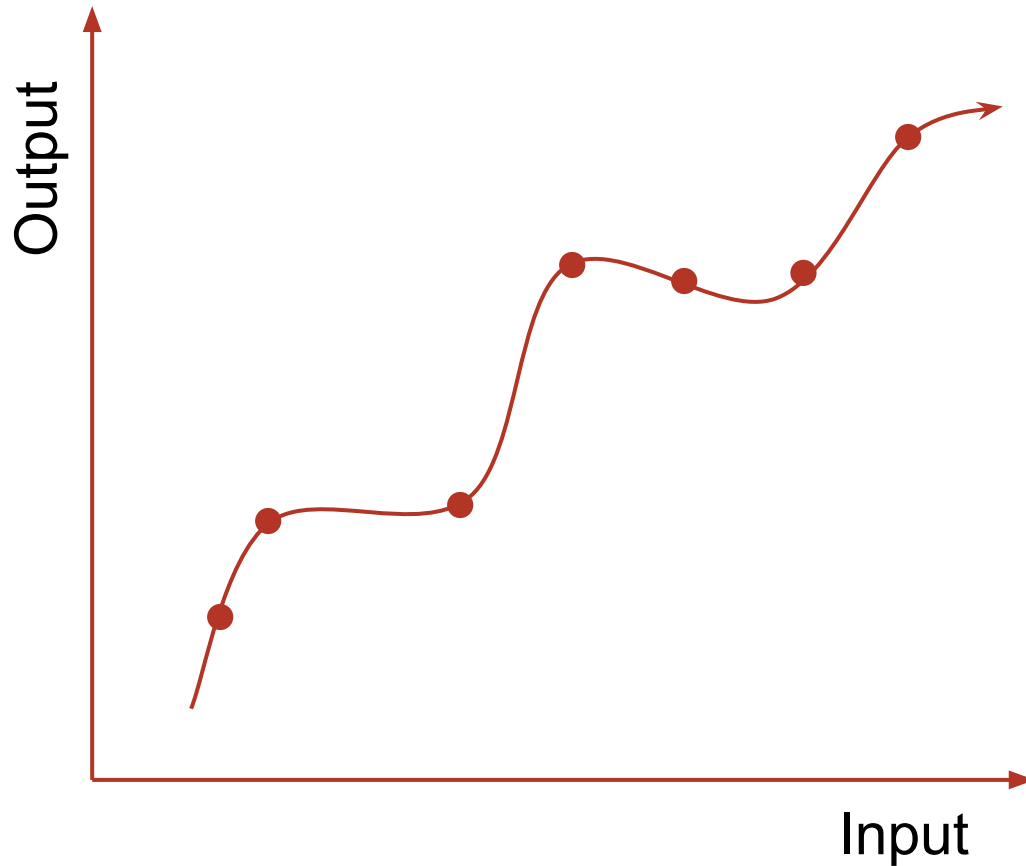
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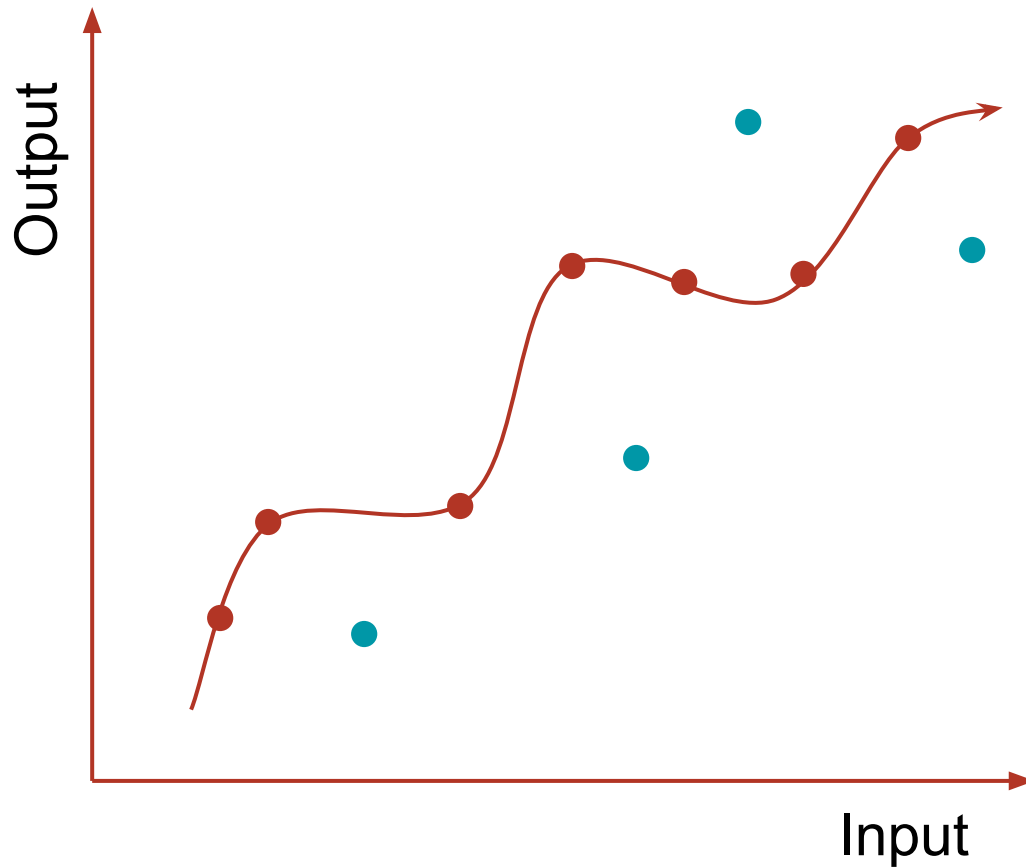
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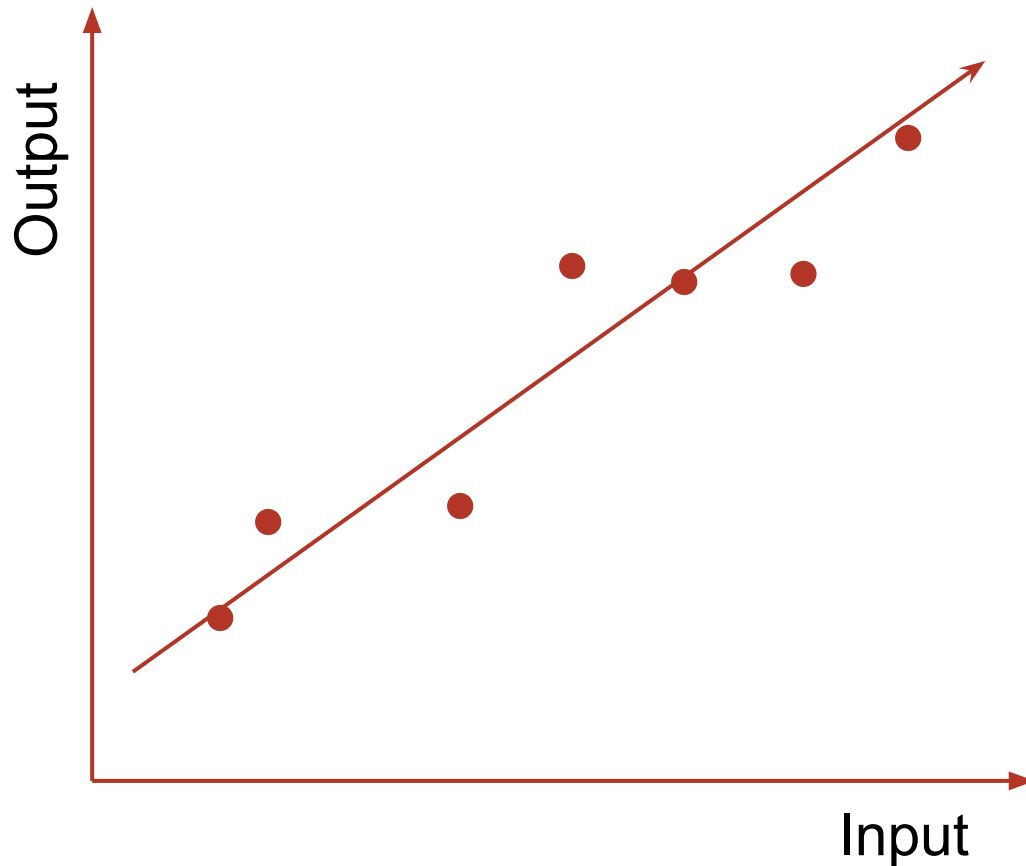
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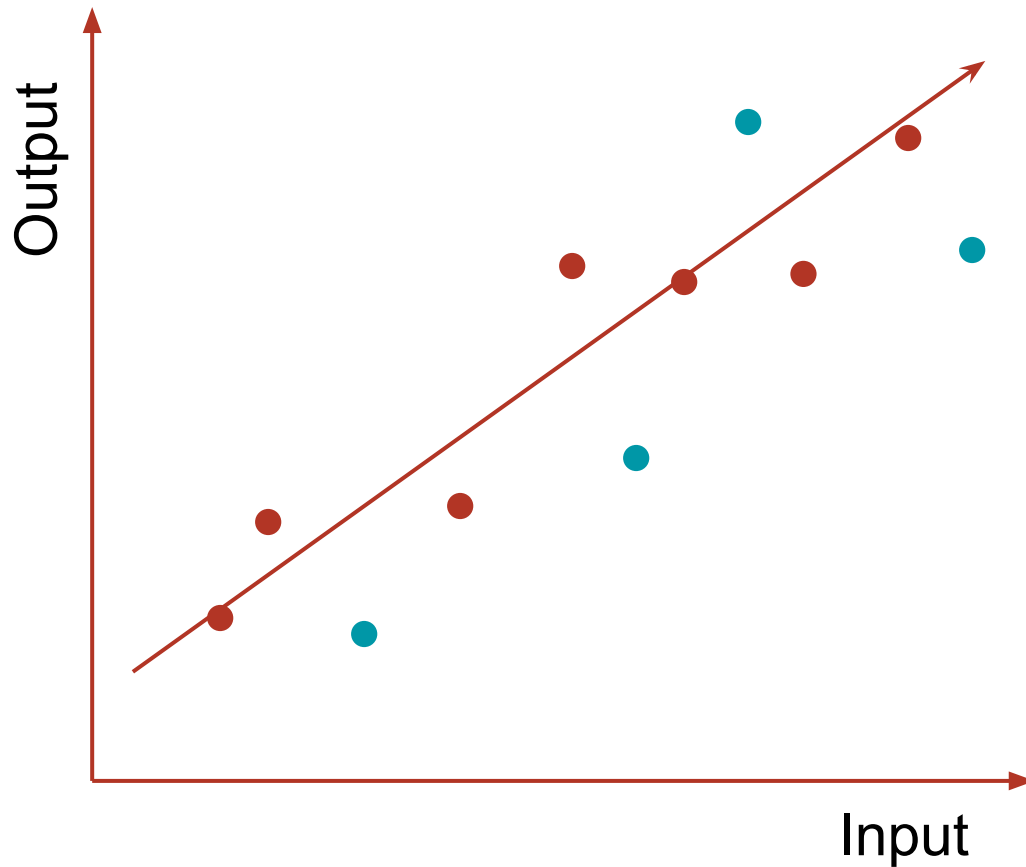
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Why is this Process Stochastic?

- ▶ Approximations are acceptable



How are the Functions?

How are the Functions?

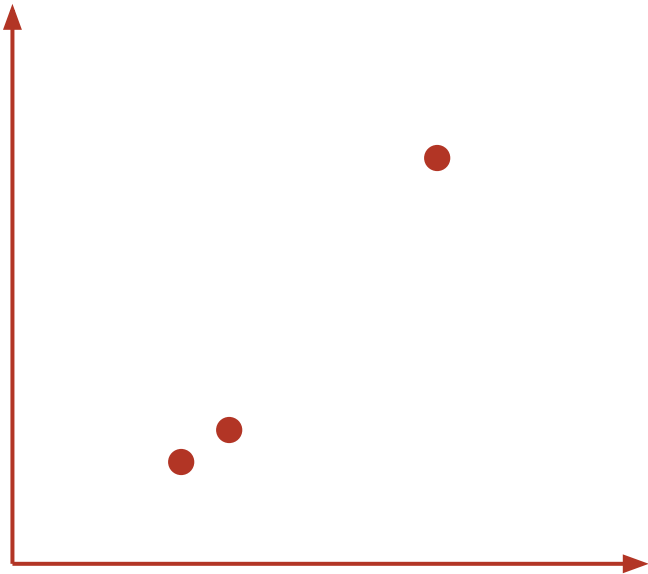
Regression

Classification

How are the Functions?

Regression

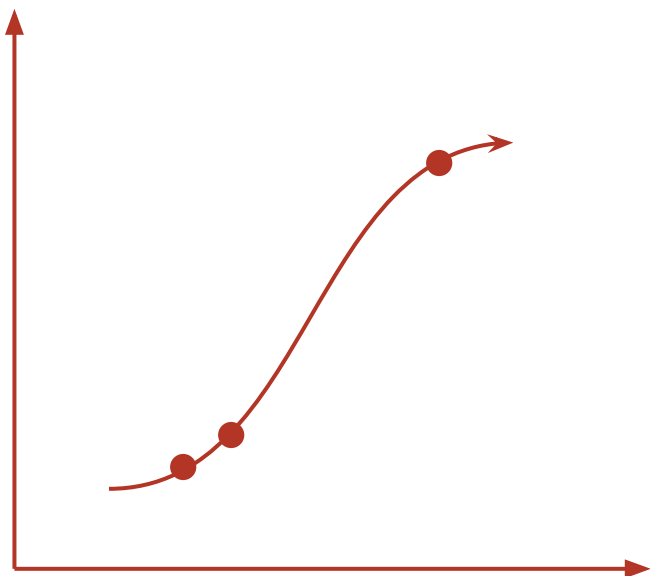
Classification



How are the Functions?

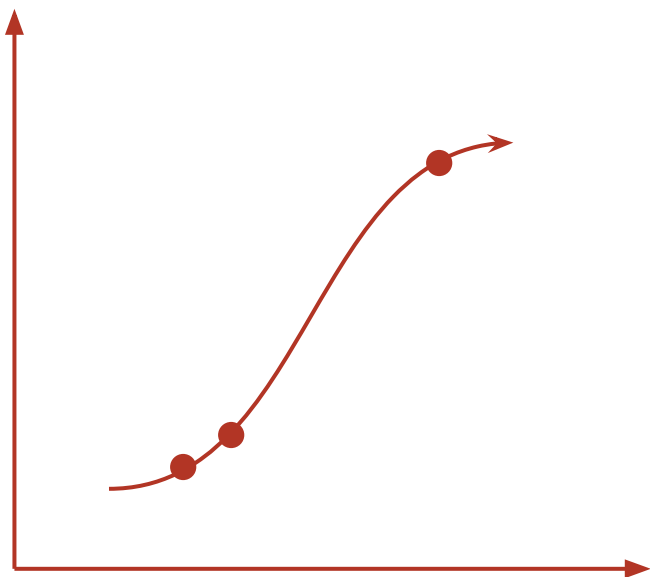
Regression

Classification

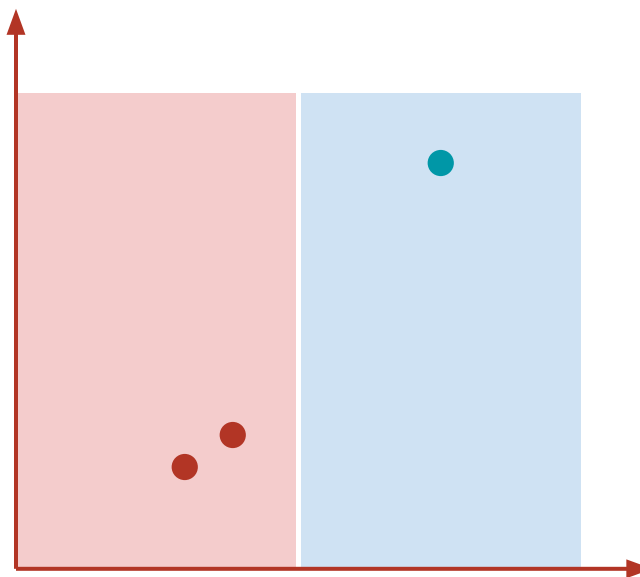


How are the Functions?

Regression



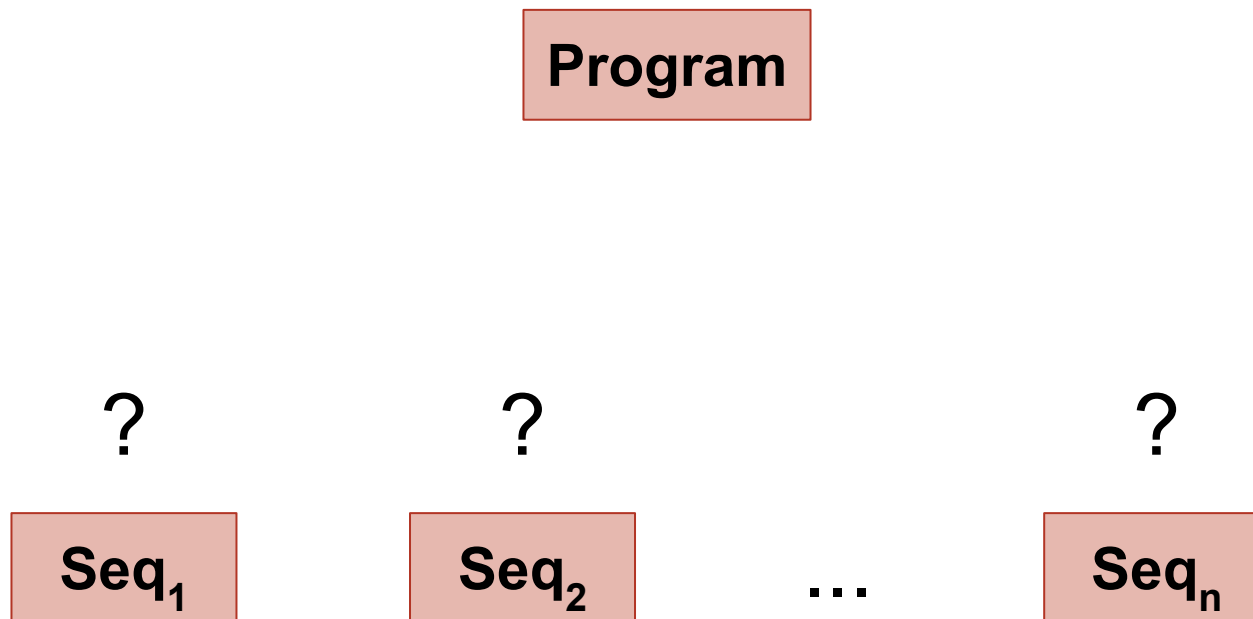
Classification



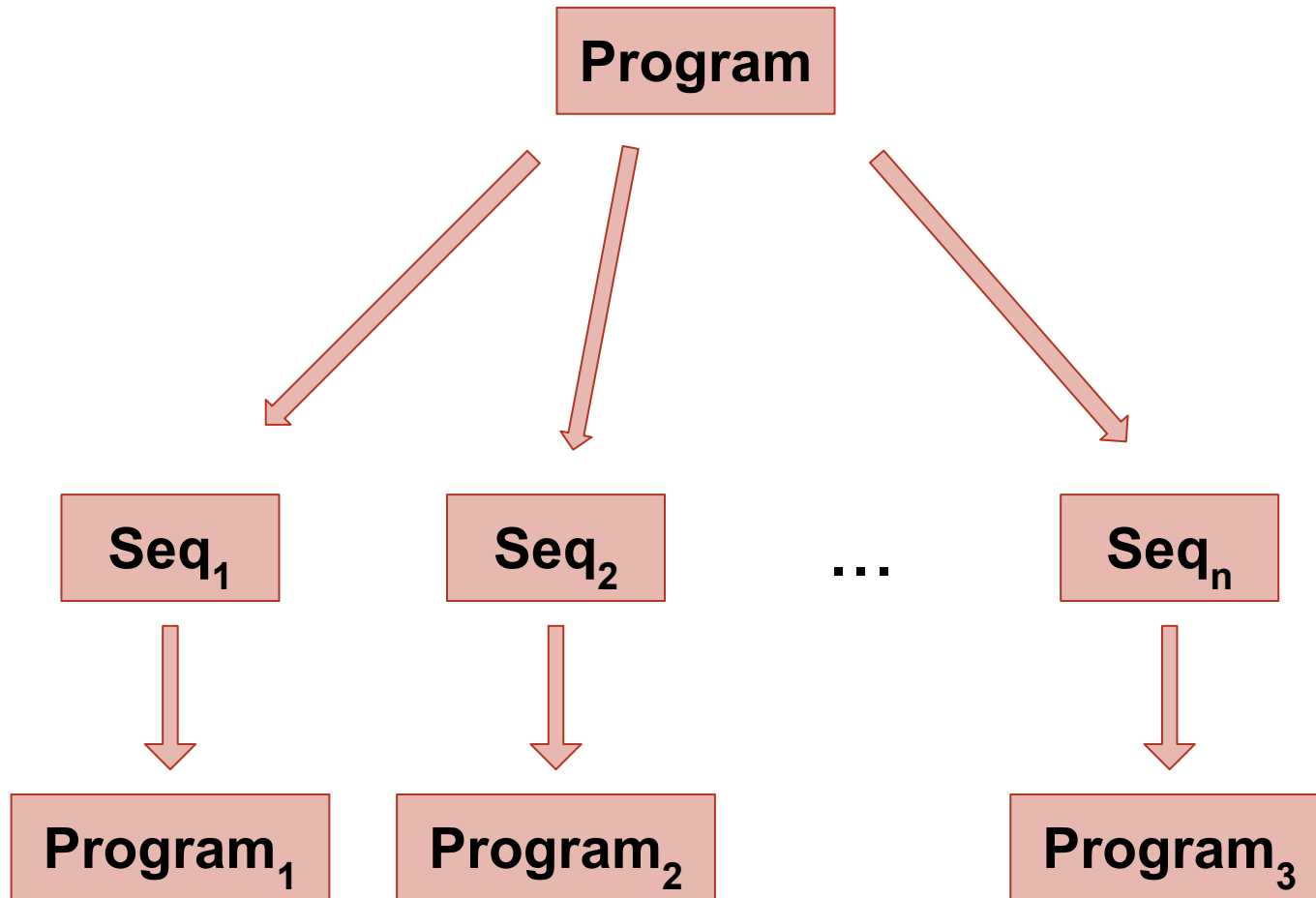
What to do with Compilers?

Example: Best Sequence of Optimizations

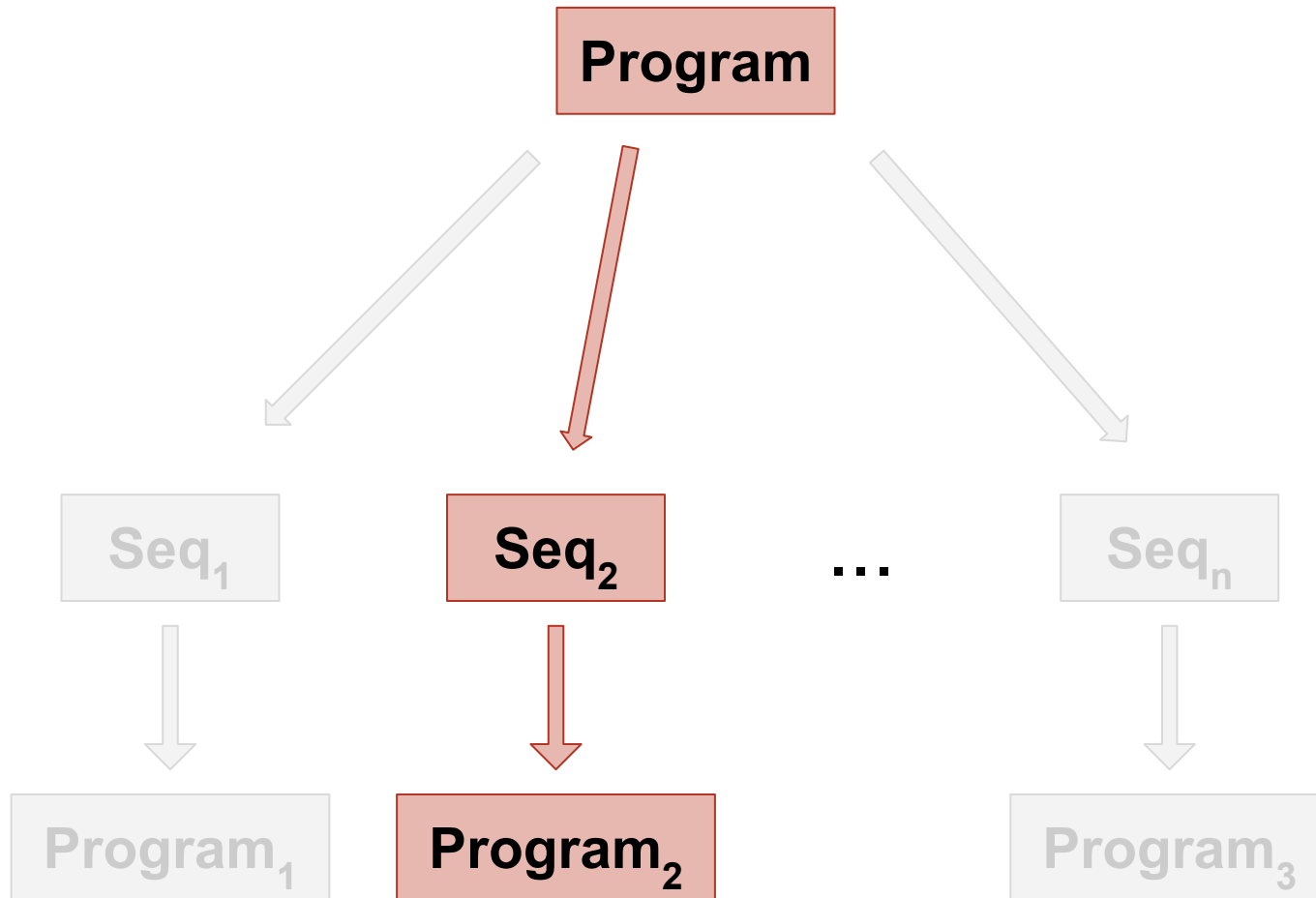
Example: Best Sequence of Optimizations



Example: Best Sequence of Optimizations



Example: Best Sequence of Optimizations



Example: Best Sequence of Optimizations

▶ Speed



Example: Best Sequence of Optimizations

► Size



Anderson Faustino da Silva, Bernardo N. B. de Lima, Fernando Magno Quintão Pereira:
Exploring the space of optimization sequences for code-size reduction: insights and tools.

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Example: Best Sequence of Optimizations

► Size

Seq₁

Seq₂

...

Seq_n

How would you get candidate sequences?

Anderson Faustino da Silva, Bernardo N. B. de Lima, Fernando Magno Quintão Pereira:
Exploring the space of optimization sequences for code-size reduction: insights and tools.

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Example: Best Sequence of Optimizations

Seq₅

Seq₄

Seq₃

Seq₂

Seq₁

How would you get
candidate sequences?

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Example: Best Sequence of Optimizations

Seq₅

-loop-rotate -sroa -correlated-propagation -indvars -gvn -tailcallelim -instcombine -jump-threading
-reassociate -simplifycfg -instcombine -early-cse-memssa

Seq₄

-loop-vectorize -sroa -gvn -instcombine -simplifycfg -instcombine -licm -gvn -correlated-propagation
-jump-threading -mldst-motion -early-cse-memssa -instcombine -simplifycfg -instsimplify

Seq₃

-mem2reg -early-cse-memssa -correlated-propagation -instcombine -reassociate -simplifycfg
-early-cse-memssa -instcombine -licm -jump-threading -simplifycfg -dse -reassociate -early-cse-memssa
-instcombine

Seq₂

-sroa -early-cse-memssa -reassociate -instcombine -simplifycfg -licm -speculative-execution
-jump-threading -early-cse-memssa -simplifycfg -instcombine -simplifycfg

Seq₁

-mem2reg -jump-threading -instcombine -early-cse-memssa -jump-threading -licm -early-cse-memssa
-sroa -simplifycfg -reassociate -instcombine -slp-vectorizer -early-cse-memssa

How would you get
candidate sequences?

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Example: Best Sequence of Optimizations



-mem2reg -jump-threading -instcombine -early-cse-memssa -jump-threading -licm -early-cse-memssa
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Example: Best Sequence of Optimizations



<https://llvm.org/docs/Passes.html>

-mem2reg -jump-threading -instcombine -early-cse-memssa -jump-threading -licm -early-cse-memssa
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Example: Best Sequence of Optimizations

Seq₅

Seq₄

Seq₃

Seq₂

Seq₁

Example: Best Optimization

Seq₅

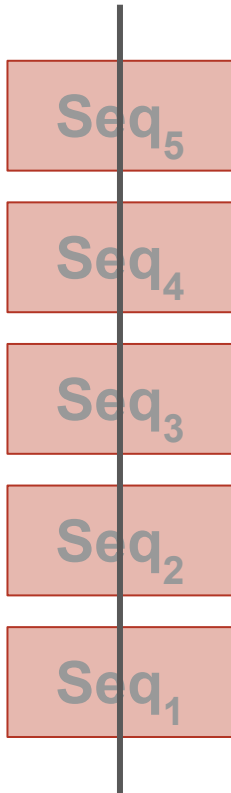
Seq₄

Seq₃

Seq₂

Seq₁

Example: Best Optimization



Opt₁

vs

Opt₂

Example: Best Optimization



Example: Best Optimization (Register Allocation)

**Linear
Scan** vs **Graph
Coloring**

John Cavazos, J. Eliot B. Moss, Michael F. P. O'Boyle:
Hybrid Optimizations: Which Optimization Algorithm to Use?

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Example: Best Optimization (Register Allocation)

Program

**Linear
Scan**

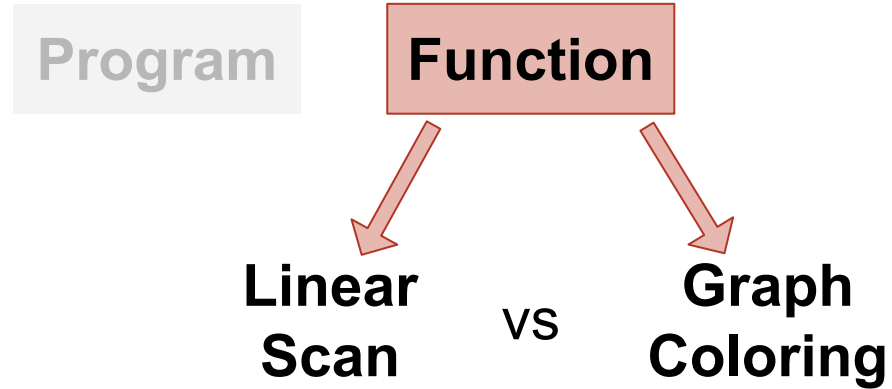
vs

**Graph
Coloring**

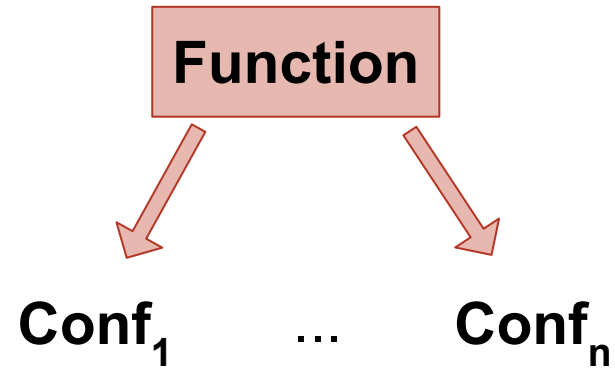
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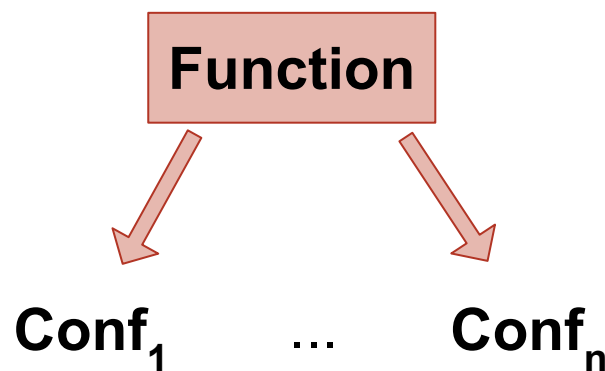
Example: Best Optimization (Register Allocation)



Example: Best Optimization (Program Scheduling)



Example: Best Optimization (Program Scheduling)

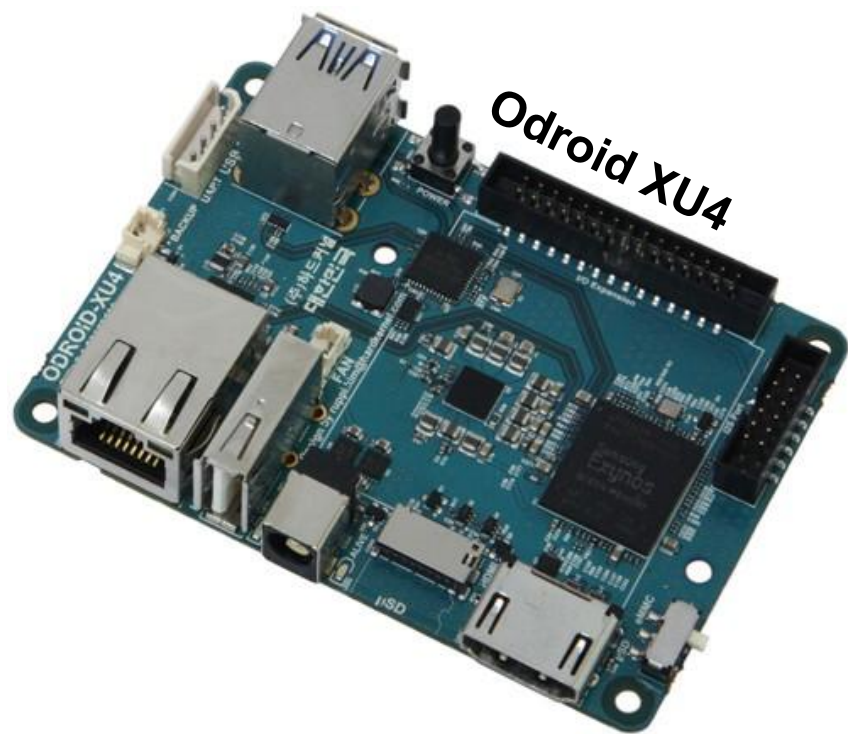


Junio C. R. da Silva, Lorena Leão, Vinicius Petrucci, Abdoulaye Gamatié, Fernando M. Q.

Pereira:

Mapping Computations in Heterogeneous Multicore Systems with Statistical Regression on Program Inputs. ACM Trans. Embed. Comput. Syst. 20(6): 112:1-112:35 (2021)

Example: Best Optimization (Program Scheduling)



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Mapping Computations in Heterogeneous Multicore Systems with Statistical Regression on Program Inputs. ACM Trans. Embed. Comput. Syst. 20(6): 112:1-112:35 (2021)

Example: Best Optimization (Program Scheduling)



big

0

1

2

3

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Example: Best Optimization (Program Scheduling)



big

LITTLE

0

0

1

1

2

2

3

3

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Example: Best Optimization (Program Scheduling)



big	Freq	LITTLE	Freq
0	200Khz	0	200Khz
1	300Khz	1	300Khz
2	...	2	...
3	1.9Ghz	3	1.7Ghz
	2.0Ghz		1.8Ghz

Junio C. R. da Silva, Lorena Leão, Vinicius Petrucci, Abdoulaye Gamatié, Fernando M. Q. Pereira:

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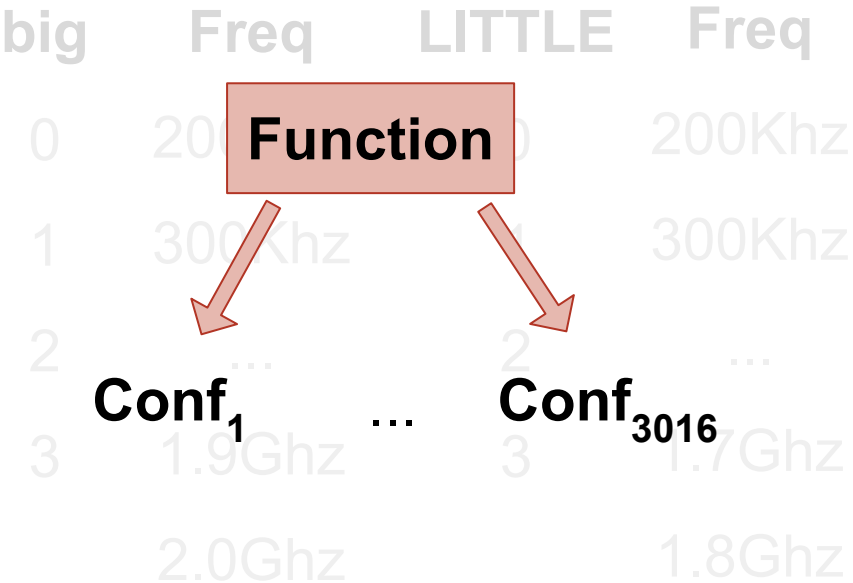
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3	1.9Ghz	3	1.7Ghz
	2.0Ghz		1.8Ghz

Configuration: 3 big cores at 1.8Ghz and 2 LITTLE cores at 1.0GHz

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Which Data to Use?

Which Data to Use?

▶ Program

Which Data to Use?

▶ Program

▶ Function

Which Data to Use?

▶ Program

▶ Function

Can you think about other granularities?

Which Data to Use?

- ▶ Program
- ▶ Function
- ▶ Instructions

Can you think about other granularities?

Which Data to Use?

- ▶ Program
- ▶ Function
- ▶ Instructions

What can you predict about instructions?

Can you think about other granularities?

Example: Silent Stores

Example: Silent Stores

- ▶ Store in memory a value already there

Example: Silent Stores

- ▶ Store in memory a value already there

How to guess if a store will be silent or not?

Example: Silent Stores

- ▶ Store in memory a value already there
- ▶ Regression

How to guess if a store will be silent or not?

Example: Silent Stores

- ▶ Store in memory a value already there

How to guess if a store
will be silent or not?

Example: Silent Stores

- ▶ Store in memory a value already there

$$a = a + b * c$$

How to guess if a store
will be silent or not?

Example: Silent Stores

- ▶ Store in memory a value already there

```
a = a + b * c
```

Example: Silent Stores

- ▶ Store in memory a value already there

`a = a + b * c`

Can you think about stores that are unlikely to be silent?

Example: Silent Stores

- ▶ Store in memory a value already there

```
a = ++a
```

Can you think about stores that are unlikely to be silent?

Can you think about other properties
to predict about instructions?

Example: Branch Prediction

Example: Branch Prediction

```
if (exp) {
```

```
    . . .
```

```
} else {
```

```
    . . .
```

```
}
```

Example: Branch Prediction

```
if (exp) {
```



```
  ...
```

```
} else {
```

```
  ...
```

```
}
```

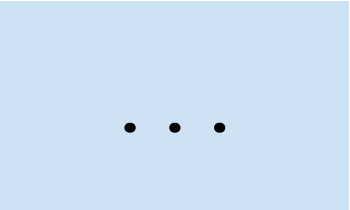
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...

```
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```



...

```
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```

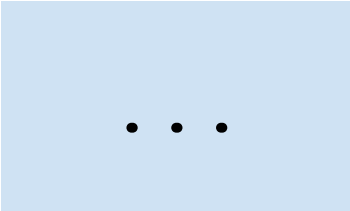
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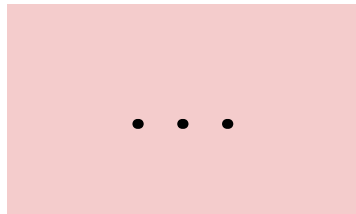
...

```
}
```

Classification ◀

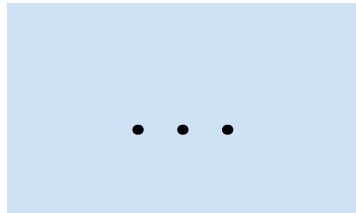
Example: Branch Prediction

```
if (exp) {
```



→ **Taken**

```
} else {
```



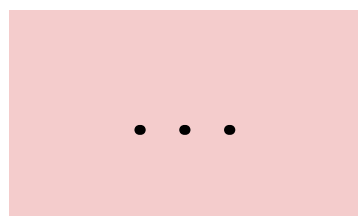
→ **Not Taken**

```
}
```

Classification ◀

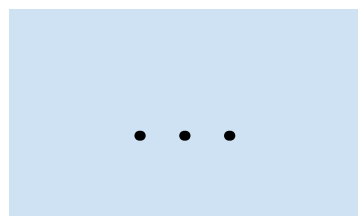
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```
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```



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```
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```



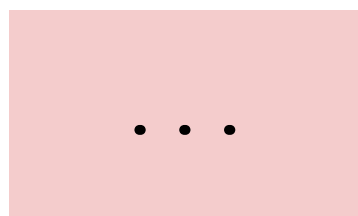
→ **Not Taken**

```
}
```

Classification ◀

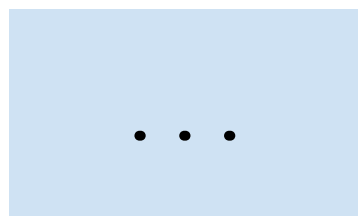
Example: Branch Prediction

```
if (exp) {
```



→ **Taken**

```
} else {
```



→ **Not Taken**

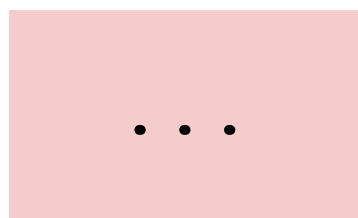
```
}
```

Classification ◀

What would be the related regression problem?

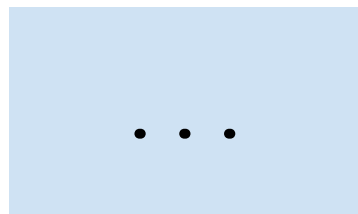
Example: Branch Prediction

```
if (exp) {
```



→ **87%**

```
} else {
```



→ **13%**

```
}
```

Regression ◀

Just the Beginning



Department of Computer Science
Universidade Federal de Minas Gerais
Federal University of Minas Gerais, Brazil

Wrapping Up

DCC888



Just the Beginning



Just the Beginning



Amir H. Ashouri, William Killian, John Cavazos, Gianluca Palermo, Cristina Silvano:
A Survey on Compiler Autotuning using Machine Learning.
ACM Comput. Surv. 51(5): 96:1-96:42 (2019)

John Cavazos



John Cavazos

▶ University of Delaware



John Cavazos

▶ University of Delaware

▶ Nov. 3, 2018



John Cavazos

▶ University of Delaware

▶ Nov. 3, 2018

▶ 49



Predictive Compilation

DCC888



Predicting the Impact of Optimizations



Predicting the Impact of Optimizations



John Cavazos, J. Eliot B. Moss, Michael F. P. O'Boyle:
Hybrid Optimizations: Which Optimization Algorithm to Use?

CC 2006: 124-138

Predicting the Impact of Optimizations

What is the improvement we can expect from a certain optimization?



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Predicting the Impact of Optimizations

What is the code-size reduction that we can expect from a certain optimization?



Measuring Code Size

How to measure
code size?



Measuring Code Size

How to measure
code size?

What is code
size?

Measuring Code Size

How to measure
code size?

What is code
size?

▶ Number of LLVM Instructions

Measuring Code Size

How to measure
code size?

What is code
size?

Number of LLVM Instructions

```
clang -Xclang -disable-OO-optnone -S -emit-llvm file.c -o file.ll
```

Measuring Code Size

How to measure
code size?

What is code
size?

Number of LLVM Instructions

```
clang -Xclang -disable-O0-optnone -S -emit-llvm file.c -o file.ll
```

```
opt -instcount -stats -disable-output file.ll
```

Measuring Code Size

How to measure
code size?

What is code
size?

▶ Number of LLVM Instructions

```
clang -Xclang -disable-O0-optnone -S -emit-llvm file.c -o file.ll
```

```
opt -instcount -stats -disable-output file.ll
```

```
2 instcount - Number of Add insts
5 instcount - Number of Alloca insts
...
1 instcount - Number of non-external functions
37 instcount - Number of instructions (of all types)
```

Measuring Code Size

How to measure
code size?

What is code
size?

▶ Size of the executable

Measuring Code Size

How to measure
code size?

What is code
size?

Size of the executable

```
clang file.c -o file.exe
```

```
ls -la file.exe
```

```
-rwxr-xr-x  1 fernando  staff  16818 Mar  3 13:38 ./a.out
```

Predicting the Impact of Optimizations

Predicting the Impact of Optimizations

What is the code-size reduction that we can expect from **clang -Oz**?

Predicting the Impact of Optimizations

What is the code-size reduction that we can expect from **clang -Oz**?

Predicting the Impact of Optimizations

▶ Median & Mean

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CC 2021: 47-58

Predicting the Impact of Optimizations

`http://cuda.dcc.ufmg.br/angha`

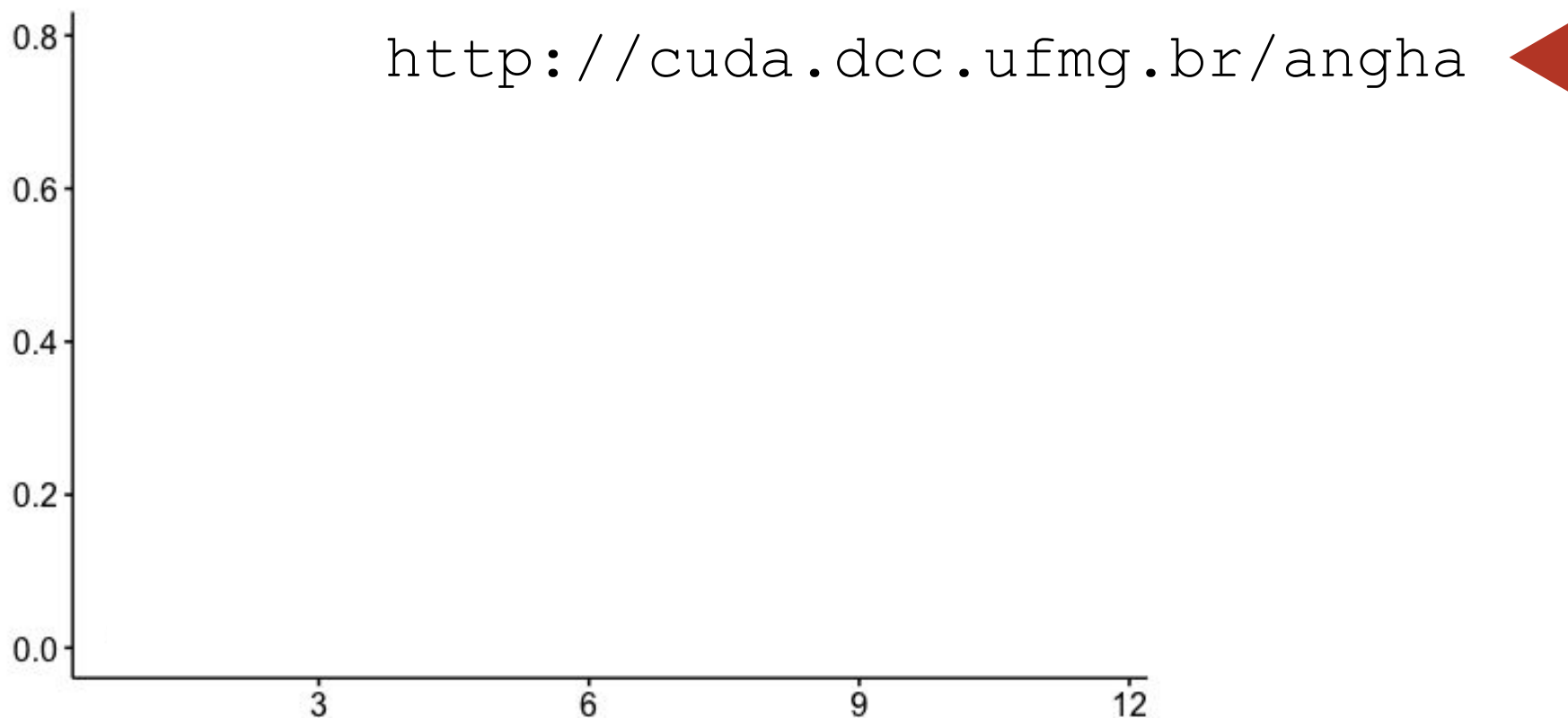


Predicting the Impact of Optimizations

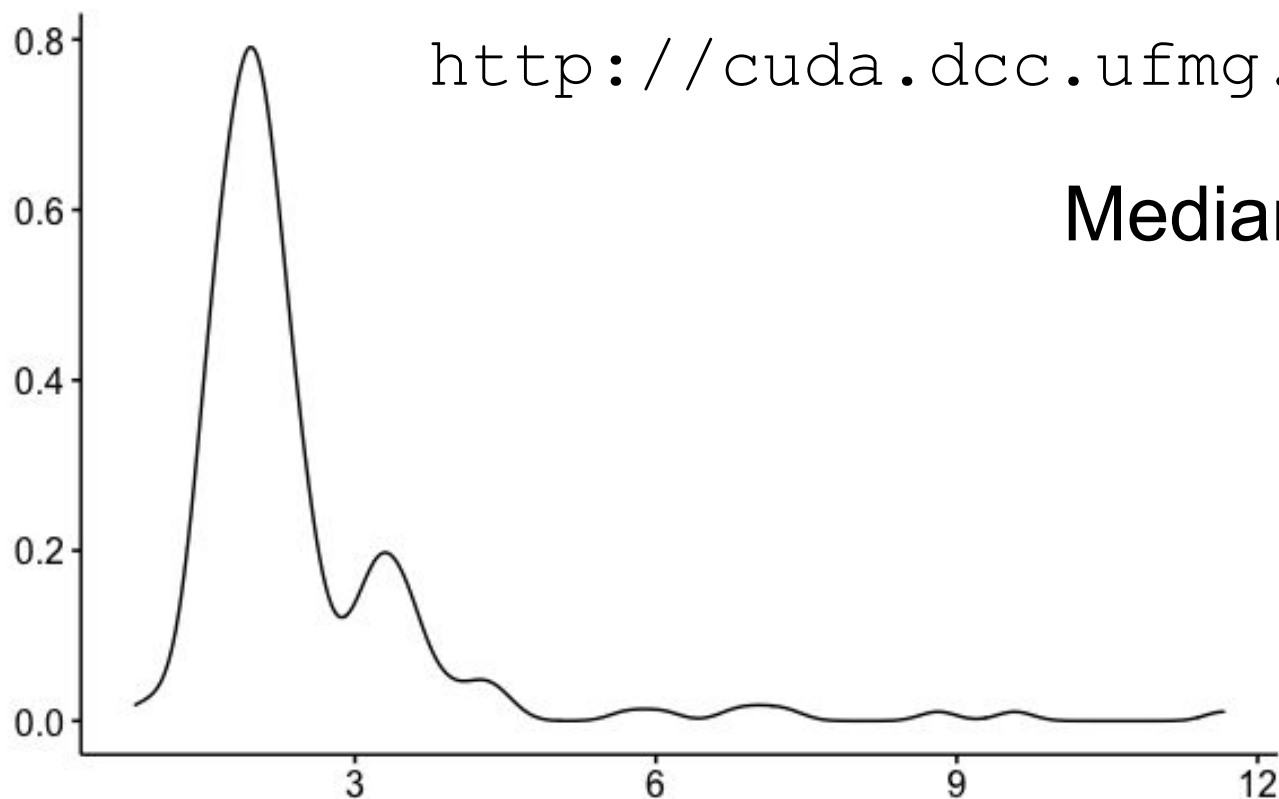
`http://cuda.dcc.ufmg.br/angha`



Predicting the Impact of Optimizations



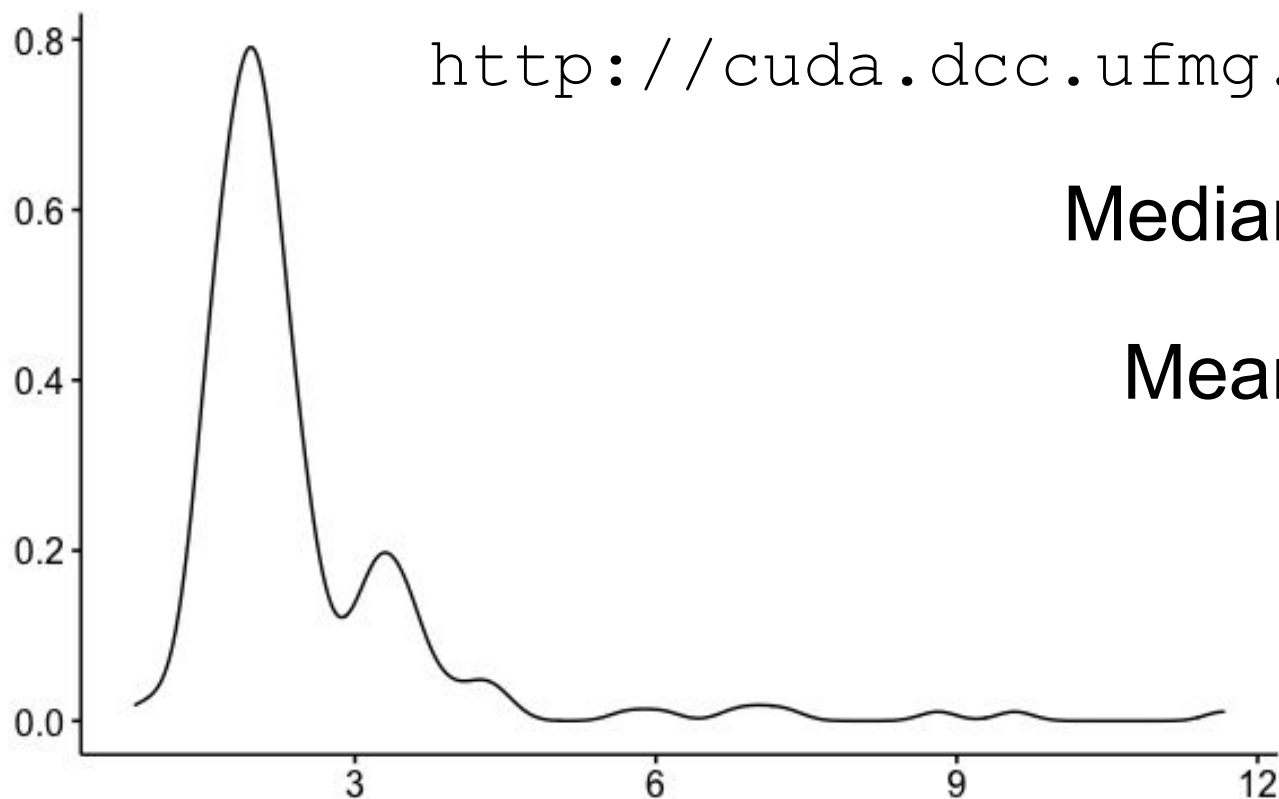
Predicting the Impact of Optimizations



A F Silva, B C Kind, J W S Magalhães, J N Rocha, B C F Guimarães, F M Q Pereira:
ANGHABENCH: A Suite with One Million Compilable C Benchmarks for Code-Size Reduction.

CGO 2021: 378-390

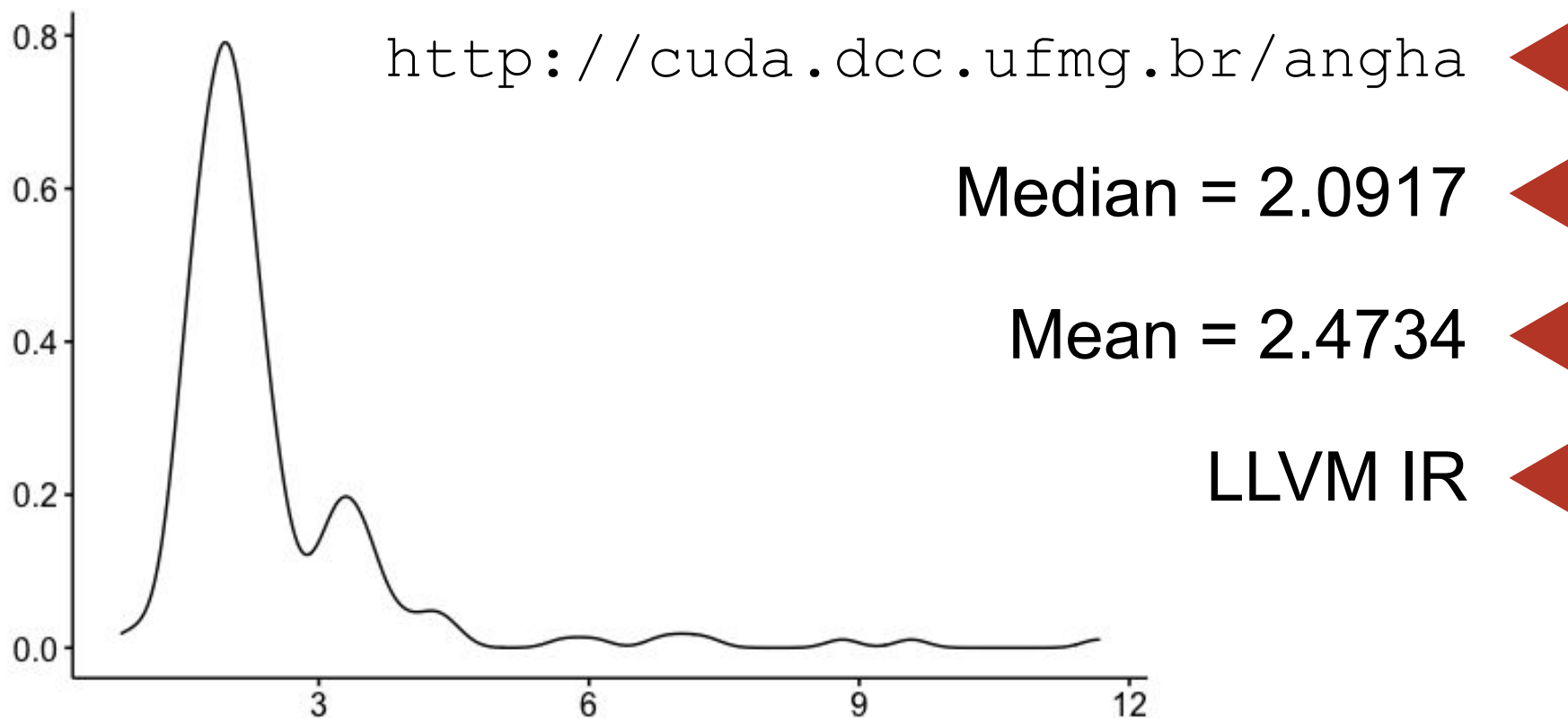
Predicting the Impact of Optimizations



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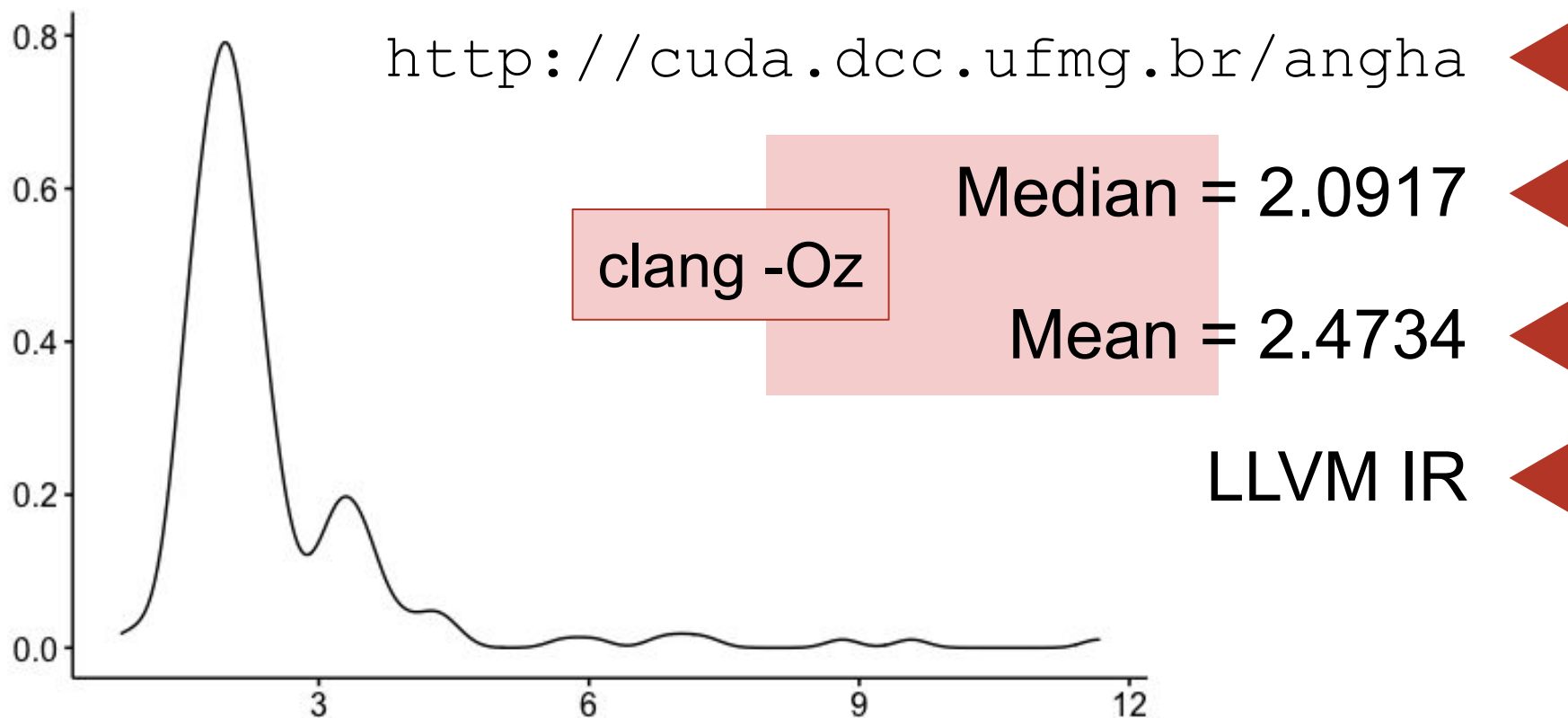
Predicting the Impact of Optimizations



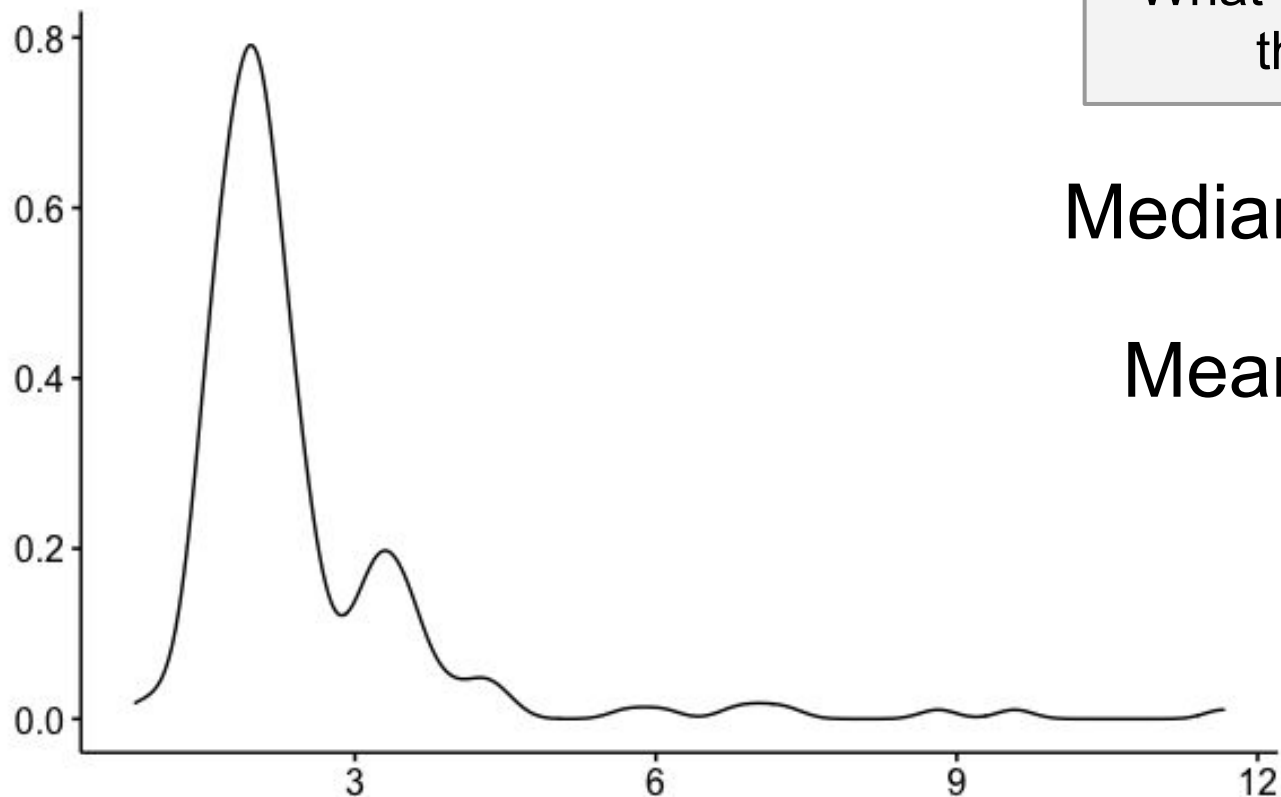
A F Silva, B C Kind, J W S Magalhães, J N Rocha, B C F Guimarães, F M Q Pereira:
ANGHABENCH: A Suite with One Million Compilable C Benchmarks for Code-Size Reduction.

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Predicting the Impact of Optimizations




Predicting the Impact of Optimizations



What is the problem with this approach?

Median = 2.0917 

Mean = 2.4734 

LLVM IR 

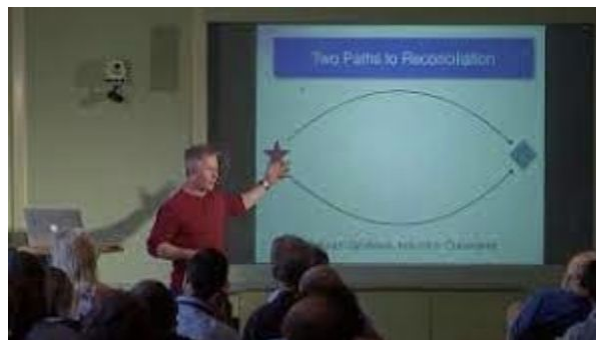
Predictive Compilation

Predictive Compilation



Reiji Suda, Ken Naono, Keita Teranishi, John Cavazos:
*Software Automatic Tuning: Concepts and State-of-the-Art Results. Software Automatic
Tuning, From Concepts to State-of-the-Art Results 2010: 3-15*

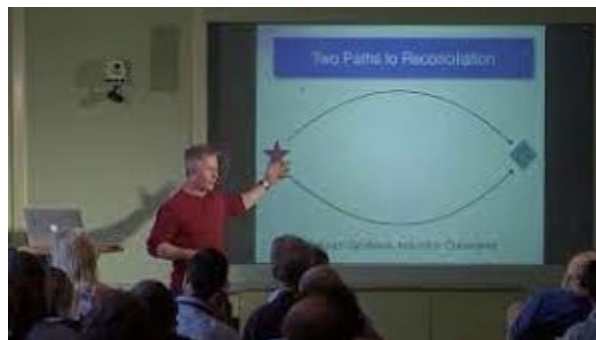
Predictive Compilation



Shun Long, Michael F. P. O'Boyle:
Adaptive Java optimisation using instance-based learning.
ICS 2004: 237-246

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Predictive Compilation



C Dubach, J Cavazos, B Franke, G Fursin, M O'Boyle, O Temam:
Fast compiler optimisation evaluation using code-feature based performance prediction.
Conf. Computing Frontiers 2007: 131-142

Shun Long, Michael F. P. O'Boyle:
Adaptive Java optimisation using instance-based learning.
ICS 2004: 237-246

Reiji Suda, Ken Naono, Keita Teranishi, John Cavazos:
Software Automatic Tuning: Concepts and State-of-the-Art Results. Software Automatic Tuning, From Concepts to State-of-the-Art Results 2010: 3-15

Predictive Compilation

P_A

P_B

Predictive Compilation

P_A

Seq₅

-loop-rotate -sroa -correlated-propagation -indvars -gvn -tailcallelim -instcombine -jump-threading
-reassociate -simplifycfg -instcombine -early-cse-memssa

P_B

Seq₄

-loop-vectorize -sroa -gvn -instcombine -simplifycfg -instcombine -licm -gvn -correlated-propagation
-jump-threading -mldst-motion -early-cse-memssa -instcombine -simplifycfg -instsimplify

Anderson Faustino da Silva, Bernardo N. B. de Lima, Fernando Magno Quintão Pereira:
Exploring the space of optimization sequences for code-size reduction: insights and tools.

CC 2021: 47-58

Predictive Compilation

P_A

Seq₅

-loop-rotate -sroa -correlated-propagation -indvars -gvn -tailcallelim -instcombine -jump-threading
-reassociate -simplifycfg -instcombine -early-cse-memssa

P_B

Seq₄

-loop-vectorize -sroa -gvn -instcombine -simplifycfg -instcombine -licm -gvn -correlated-propagation
-jump-threading -mldst-motion -early-cse-memssa -instcombine -simplifycfg -instsimplify

Seq₃

-mem2reg -early-cse-memssa -correlated-propagation -instcombine -reassociate -simplifycfg
-early-cse-memssa -instcombine -licm -jump-threading -simplifycfg -dse -reassociate -early-cse-memssa
-instcombine

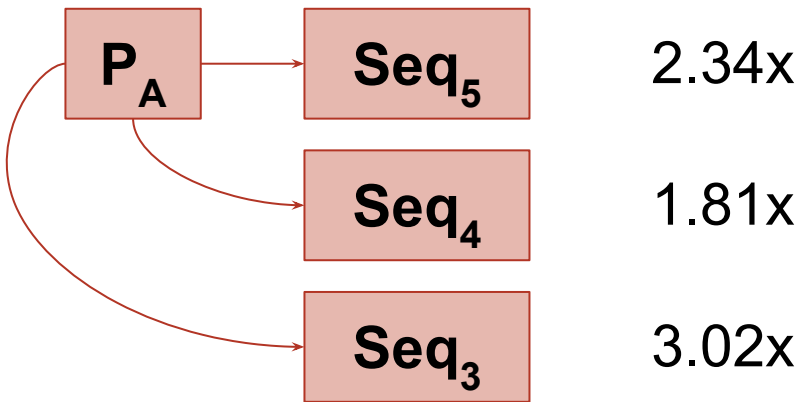
Seq₂

-sroa -early-cse-memssa -reassociate -instcombine -simplifycfg -licm -speculative-execution
-jump-threading -early-cse-memssa -simplifycfg -instcombine -simplifycfg

Seq₁

-mem2reg -jump-threading -instcombine -early-cse-memssa -jump-threading -licm -early-cse-memssa
-sroa -simplifycfg -reassociate -instcombine -slp-vectorizer -early-cse-memssa

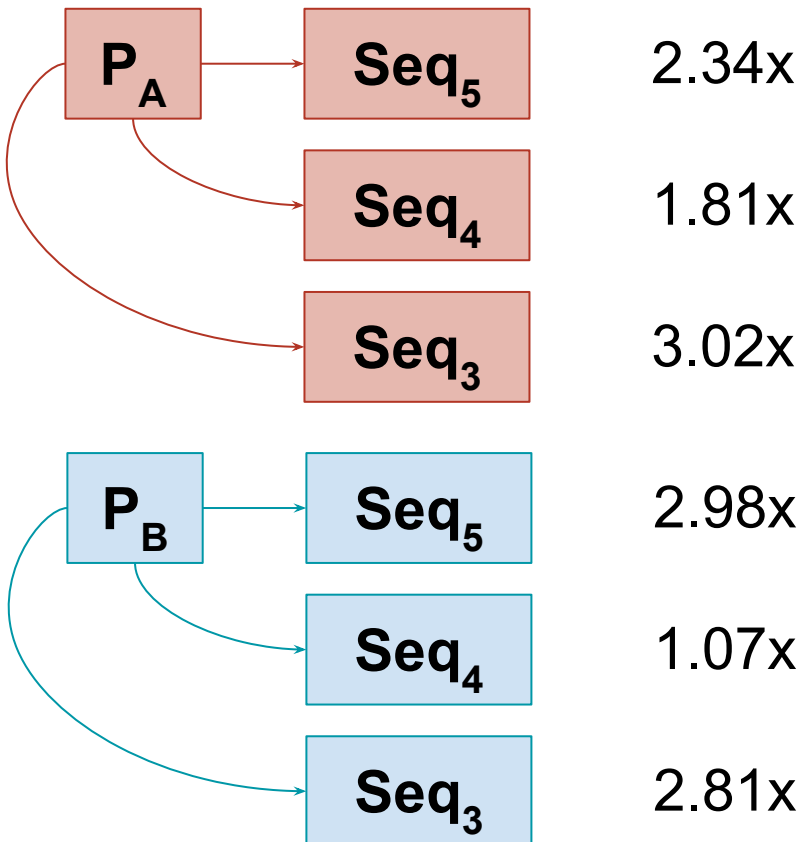
Predictive Compilation



Anderson Faustino da Silva, Bernardo N. B. de Lima, Fernando Magno Quintão Pereira:
Exploring the space of optimization sequences for code-size reduction: insights and tools.

CC 2021: 47-58

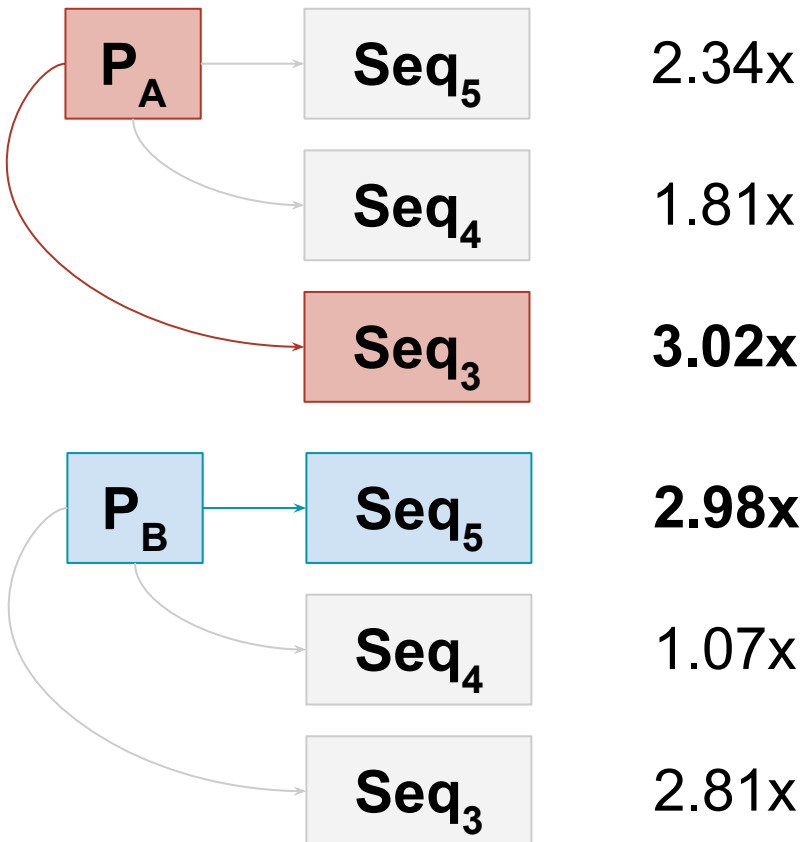
Predictive Compilation



Anderson Faustino da Silva, Bernardo N. B. de Lima, Fernando Magno Quintão Pereira:
Exploring the space of optimization sequences for code-size reduction: insights and tools.

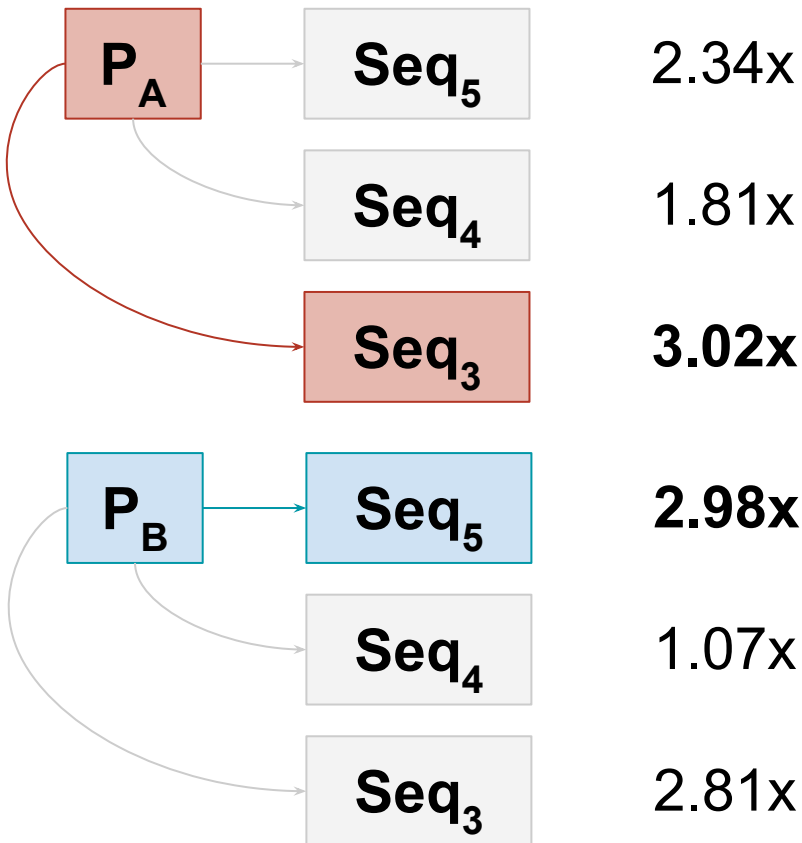
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Predictive Compilation



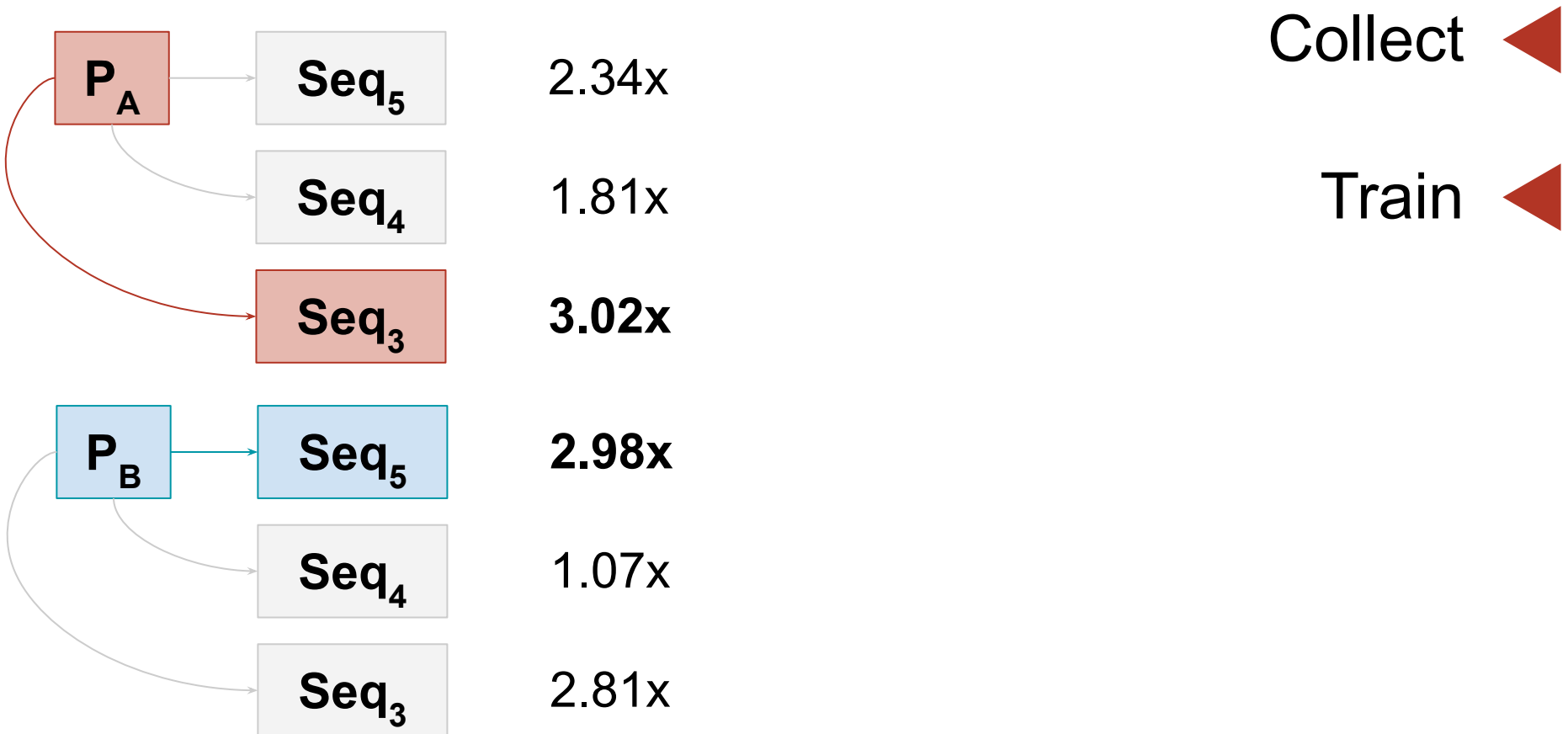
Anderson Faustino da Silva, Bernardo N. B. de Lima, Fernando Magno Quintão Pereira:
Exploring the space of optimization sequences for code-size reduction: insights and tools.

Predictive Compilation



Collect ◀

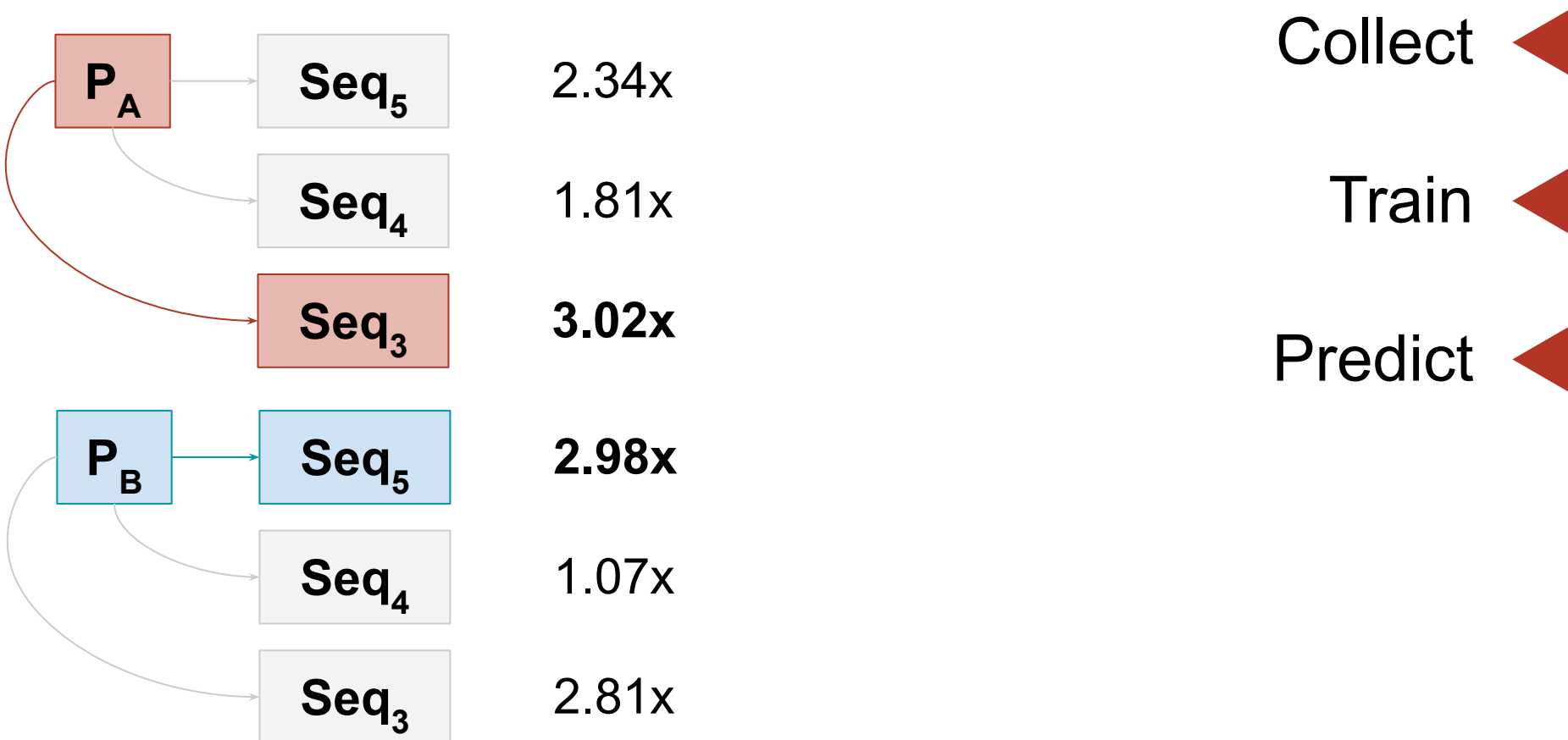
Predictive Compilation



Anderson Faustino da Silva, Bernardo N. B. de Lima, Fernando Magno Quintão Pereira:
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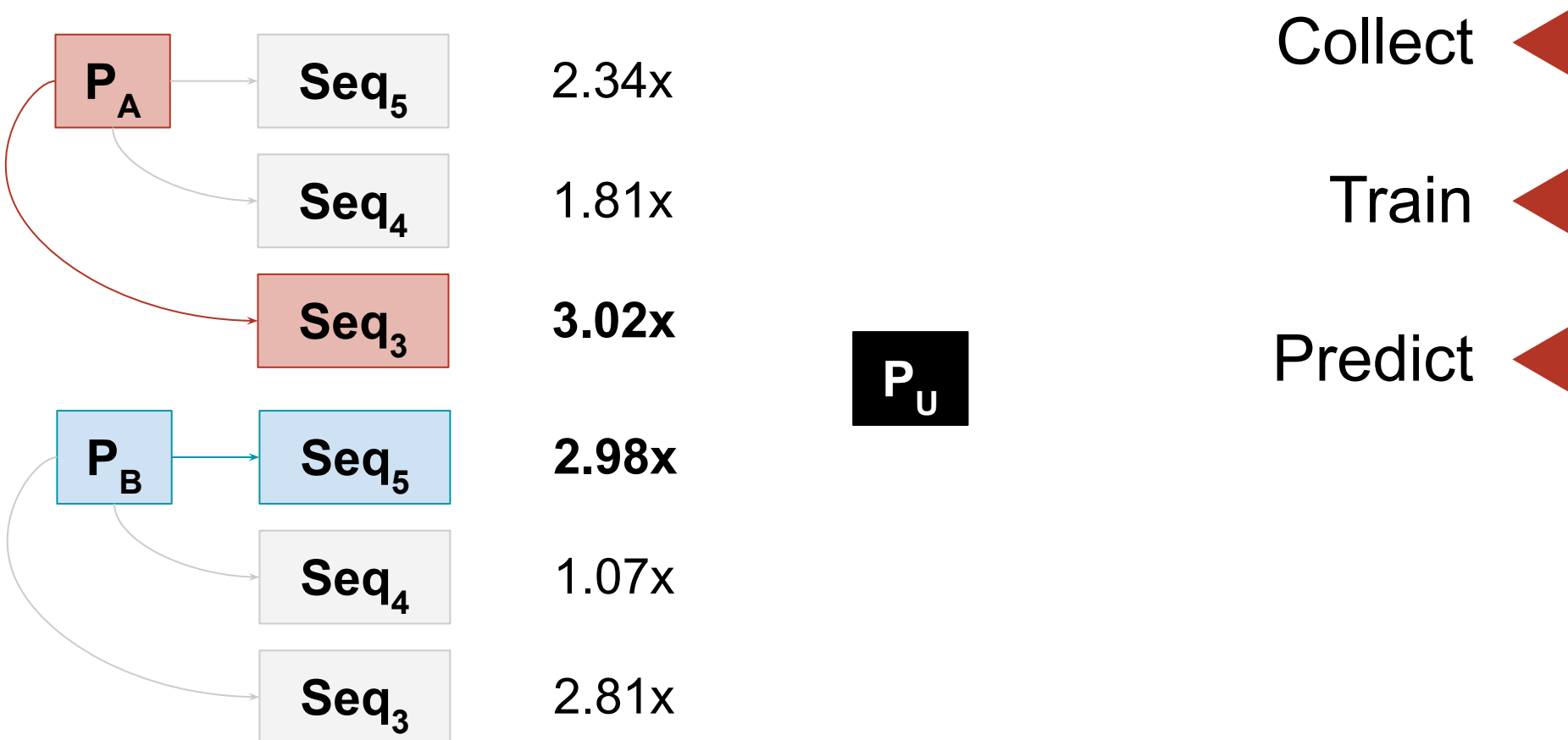
CC 2021: 47-58

Predictive Compilation



Anderson Faustino da Silva, Bernardo N. B. de Lima, Fernando Magno Quintão Pereira:
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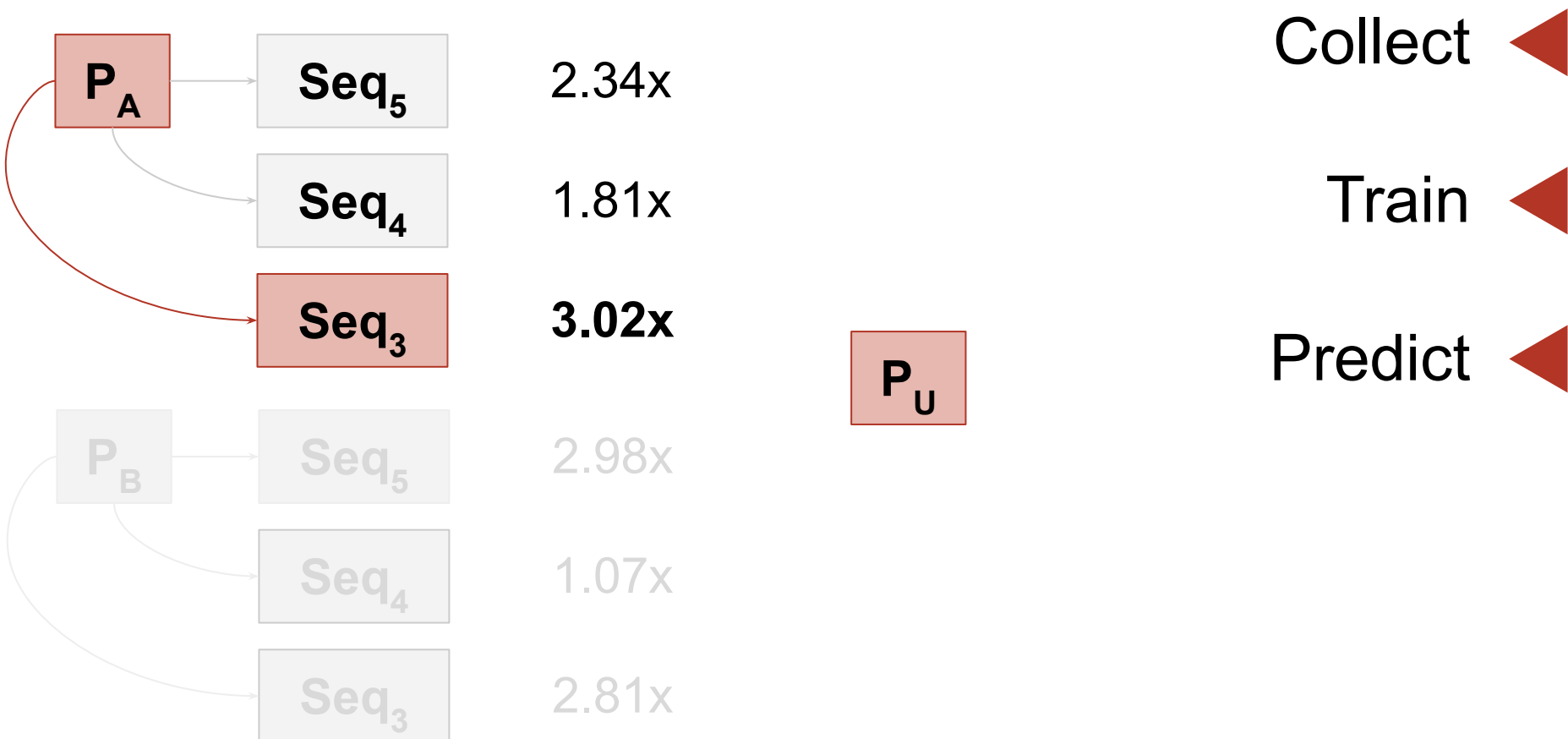
Predictive Compilation



Anderson Faustino da Silva, Bernardo N. B. de Lima, Fernando Magno Quintão Pereira:
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Predictive Compilation



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Predictive Compilation

P_A

Collect ◀

Train ◀

Predict ◀

Seq₃

3.02x

P_U

P_B

Seq₅

2.98x

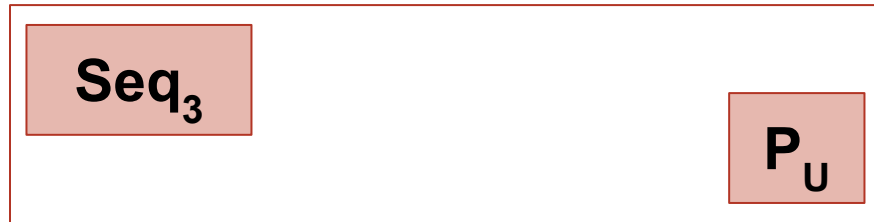
Seq₄

1.07x

Seq₃

2.81x

Predictive Compilation



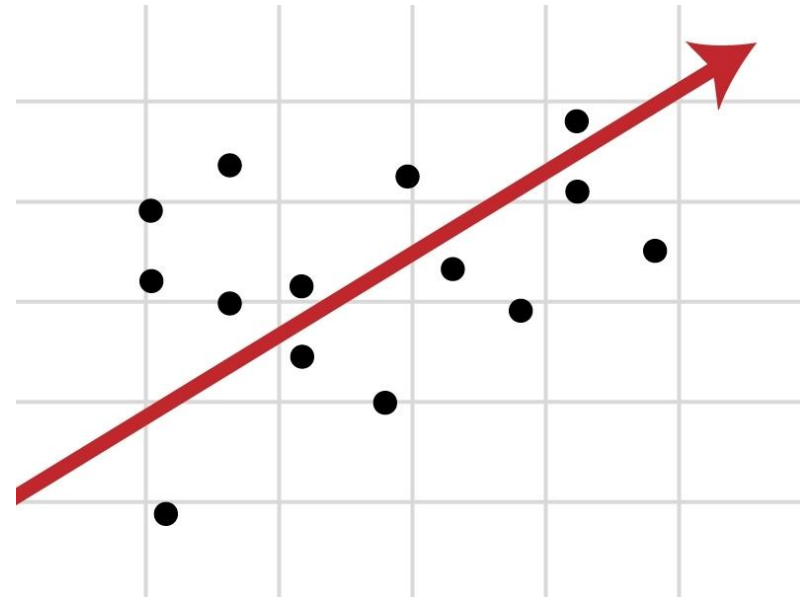
Collect ◀

Train ◀

Predict ◀

Regression

DCC888



Predictive Compilation

Predictive Compilation

- ▶ Estimate Code-Size Reduction

Predictive Compilation

▶ Estimate Code-Size Reduction

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Program Characteristics

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Program Characteristics Numeric Vectors

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Program Characteristics Numeric Vectors

P_A

P_B

Program Characteristics Numeric Vectors

P_A

34	25	18	61
40	19	27	72
13	37	20	51
7	0	1	15

P_B

15	23	19	73
35	14	19	64
23	33	28	49
9	3	0	17

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Exploring the space of optimization sequences for code-size reduction: insights and tools.

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Program Characteristics Numeric Vectors

P_A

34	25	18	61
----	----	----	----

P_B

15	23	19	73
----	----	----	----

Program Characteristics Numeric Vectors

P_A

34

P_B

15

Program Characteristics Numeric Vectors

P_A

34

How to transform a program in numbers?

P_B

15

Program Characteristics Numeric Vectors

P_A

34

How to transform a program in numbers?

P_B

15

Polynomial Time 

Program Characteristics Numeric Vectors

P_A

34

How to transform a program in numbers?

Polynomial Time 

P_B

15

Deterministic 

Program Characteristics Numeric Vectors

P_A

34

How to transform a program in numbers?

Polynomial Time 

P_B

15

Deterministic 

Collisions are Acceptable 

Program Characteristics Numeric Vectors

P_A

34

How to transform a program in numbers?

Polynomial Time 

P_B

15

Deterministic 

Collisions are Acceptable 

One way 

Embedding Function

P_A

34

P_B

15

Polynomial Time 

Deterministic 

Collisions are Acceptable 

One way 

Embedding Function

P_A

34

P_B

15

Polynomial Time



Deterministic



Collisions are Acceptable



One way



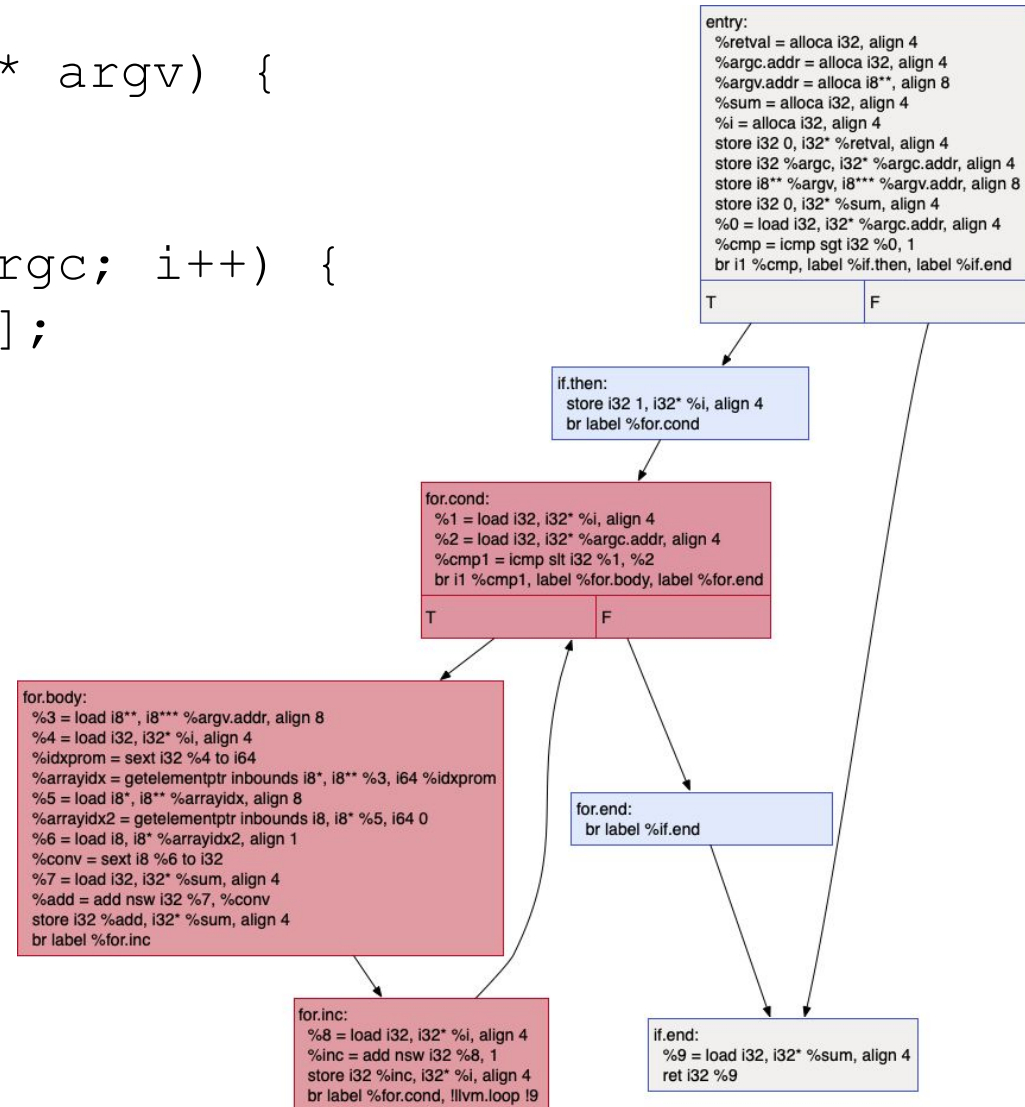
Histograms

Histograms

```
int main(int argc, char** argv) {
    int sum = 0;
    if (argc > 1) {
        for (int i = 1; i < argc; i++) {
            sum += (int)argv[i][0];
        }
    }
    return sum;
}
```

Histograms

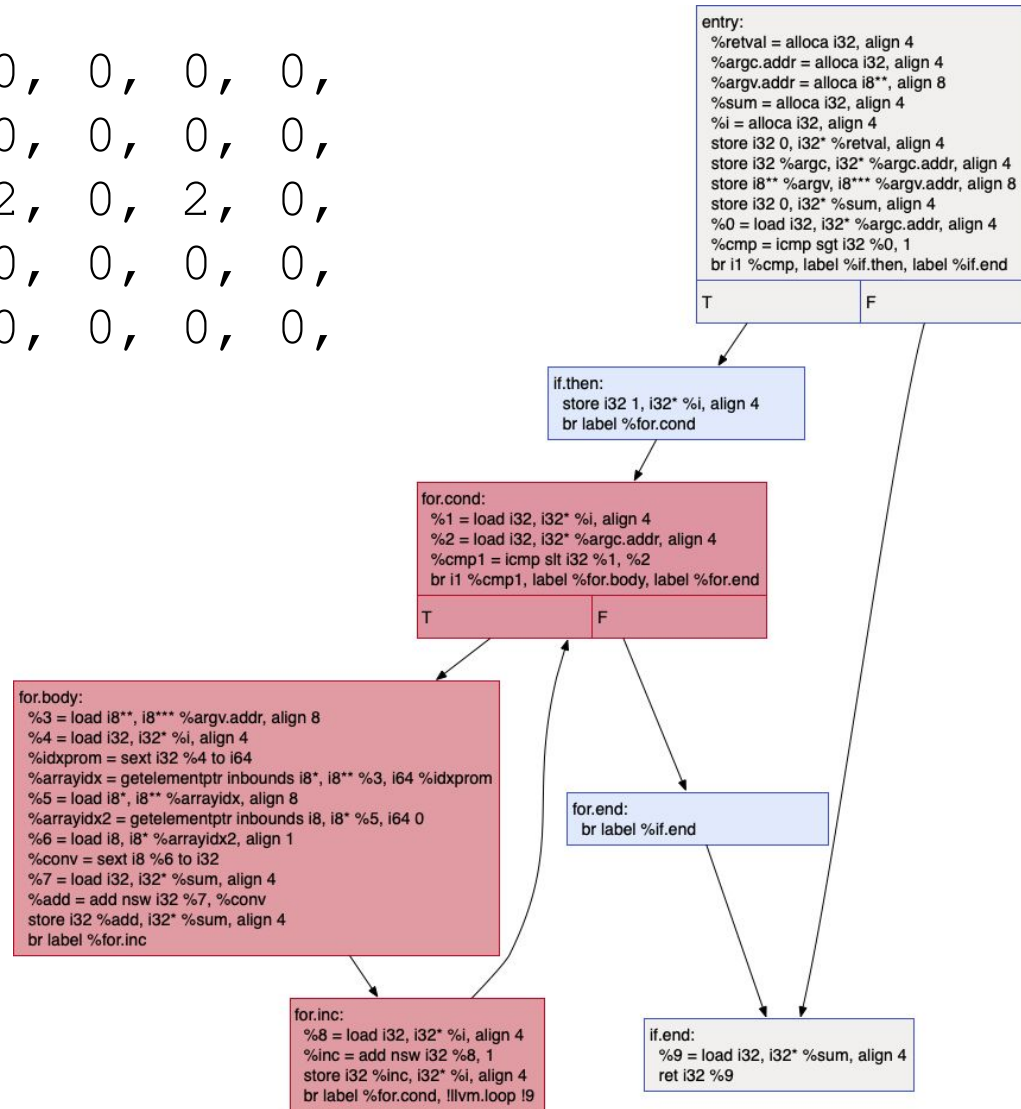
```
int main(int argc, char** argv) {  
    int sum = 0;  
    if (argc > 1) {  
        for (int i = 1; i < argc; i++) {  
            sum += (int)argv[i][0];  
        }  
    }  
    return sum;  
}
```



Histograms

```

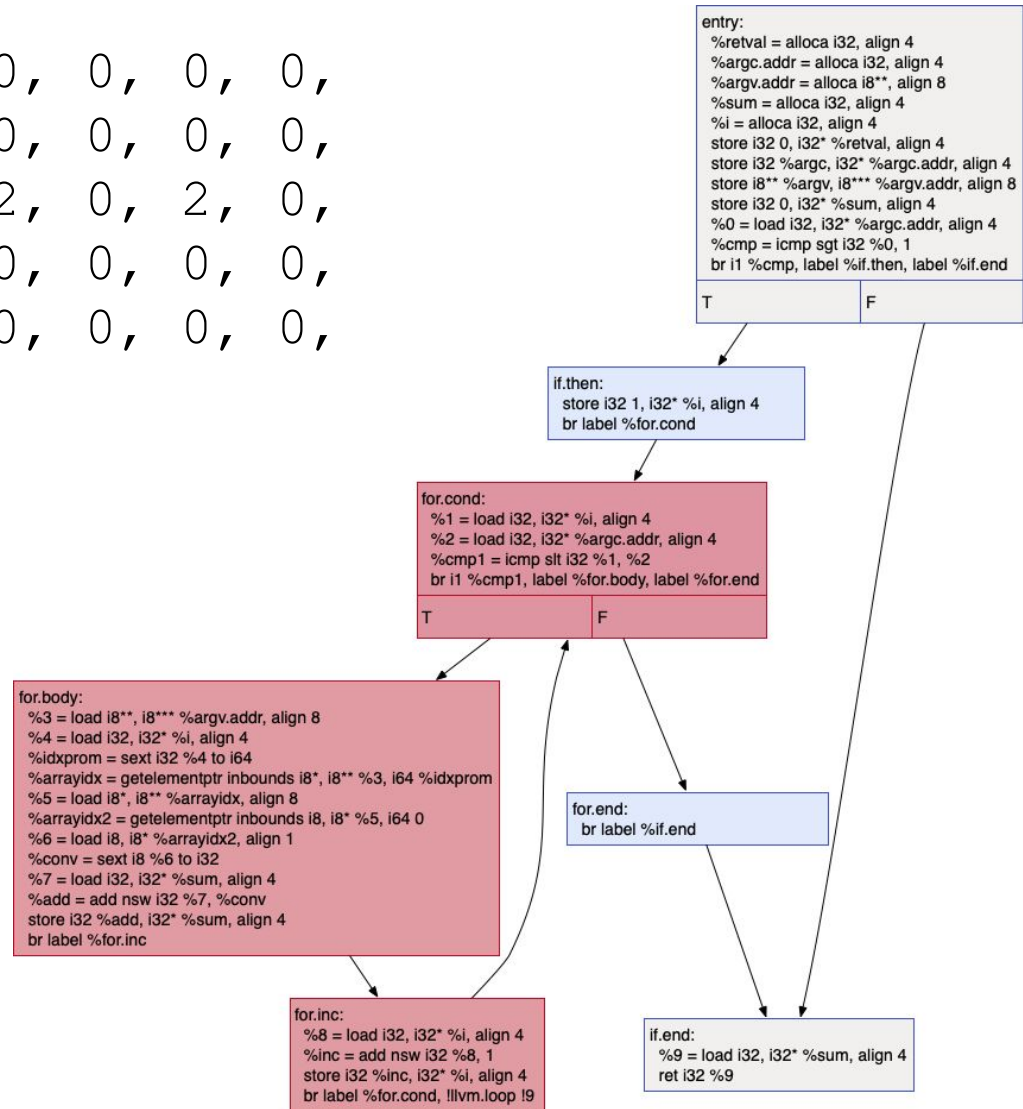
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0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
  
```



Histograms

```

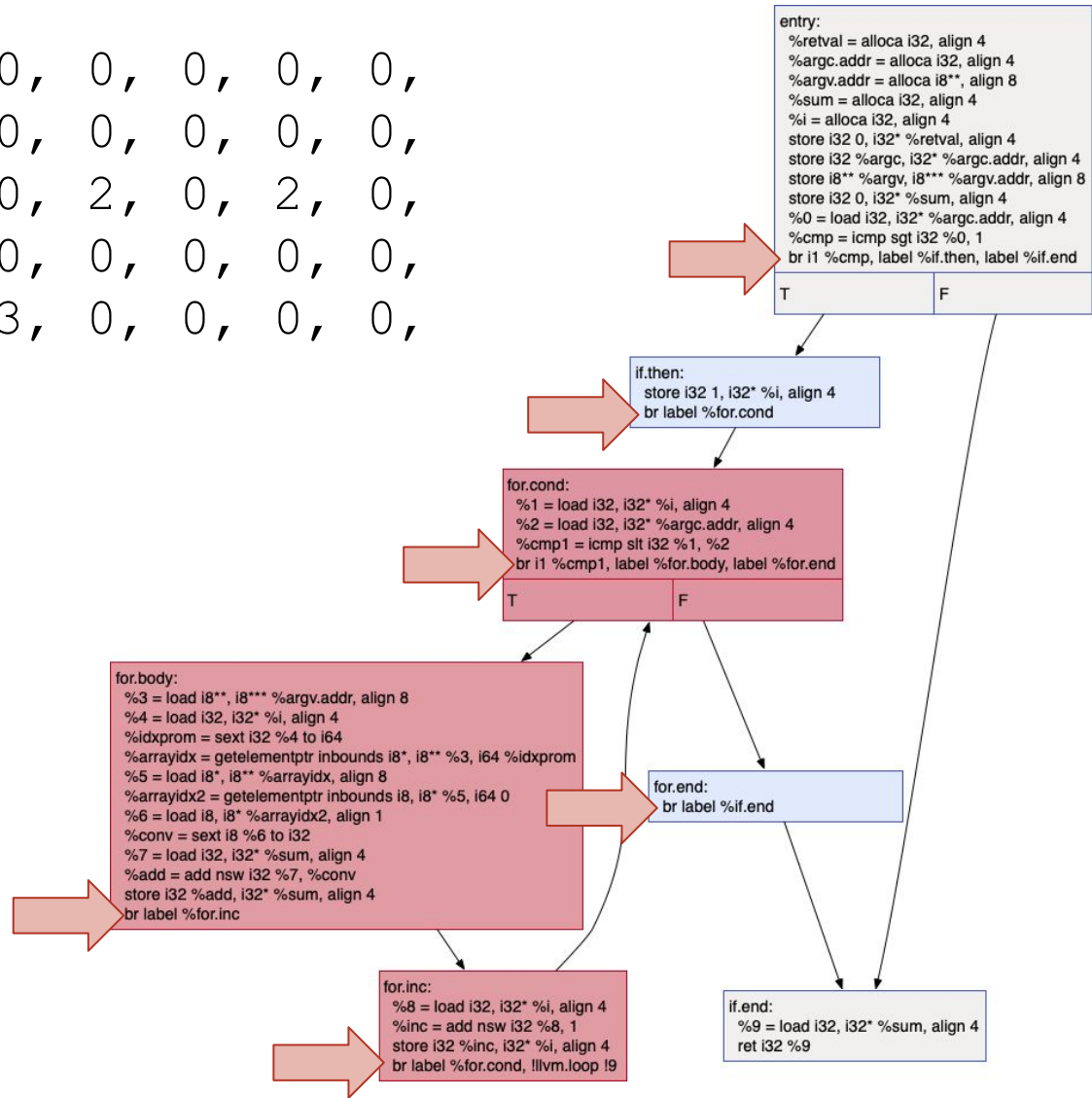
0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
  
```



Histograms

```

0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
    
```



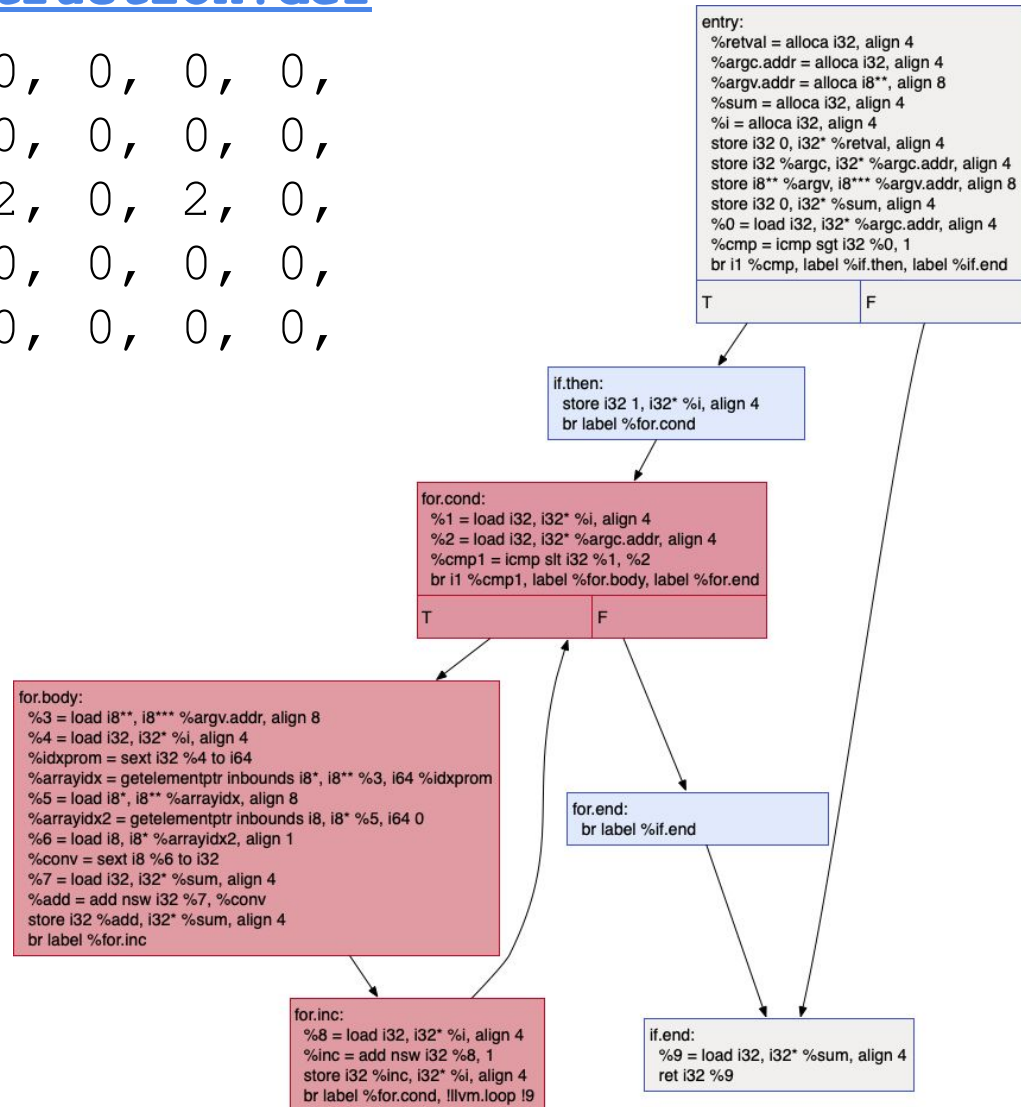
Histograms

[llvm/include/llvm/IR/Instruction.def](#)

```

0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,

```

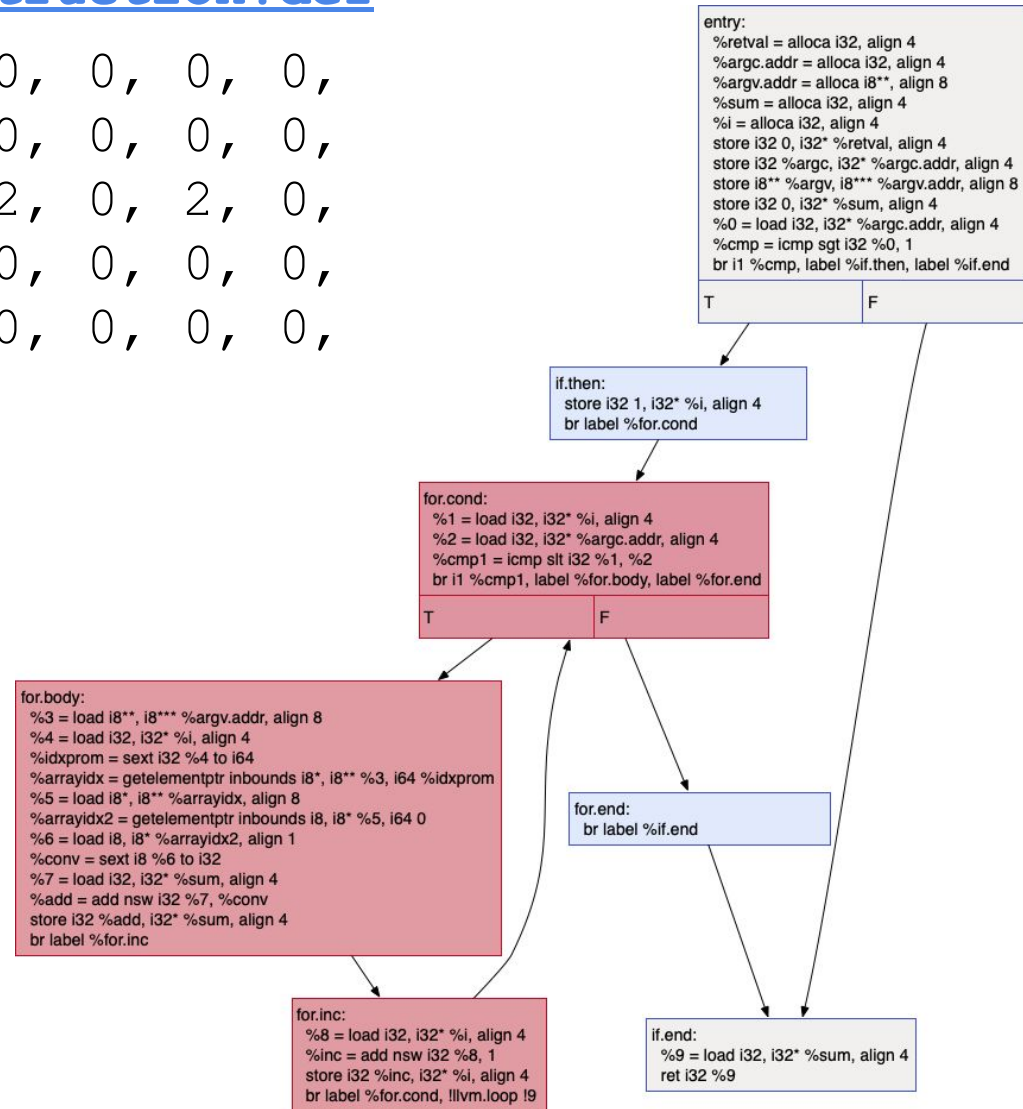


Histograms

[llvm/include/llvm/IR/Instruction.def](#)

```
0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
```

How to use the histogram to predict the best sequence of optimizations for a program?

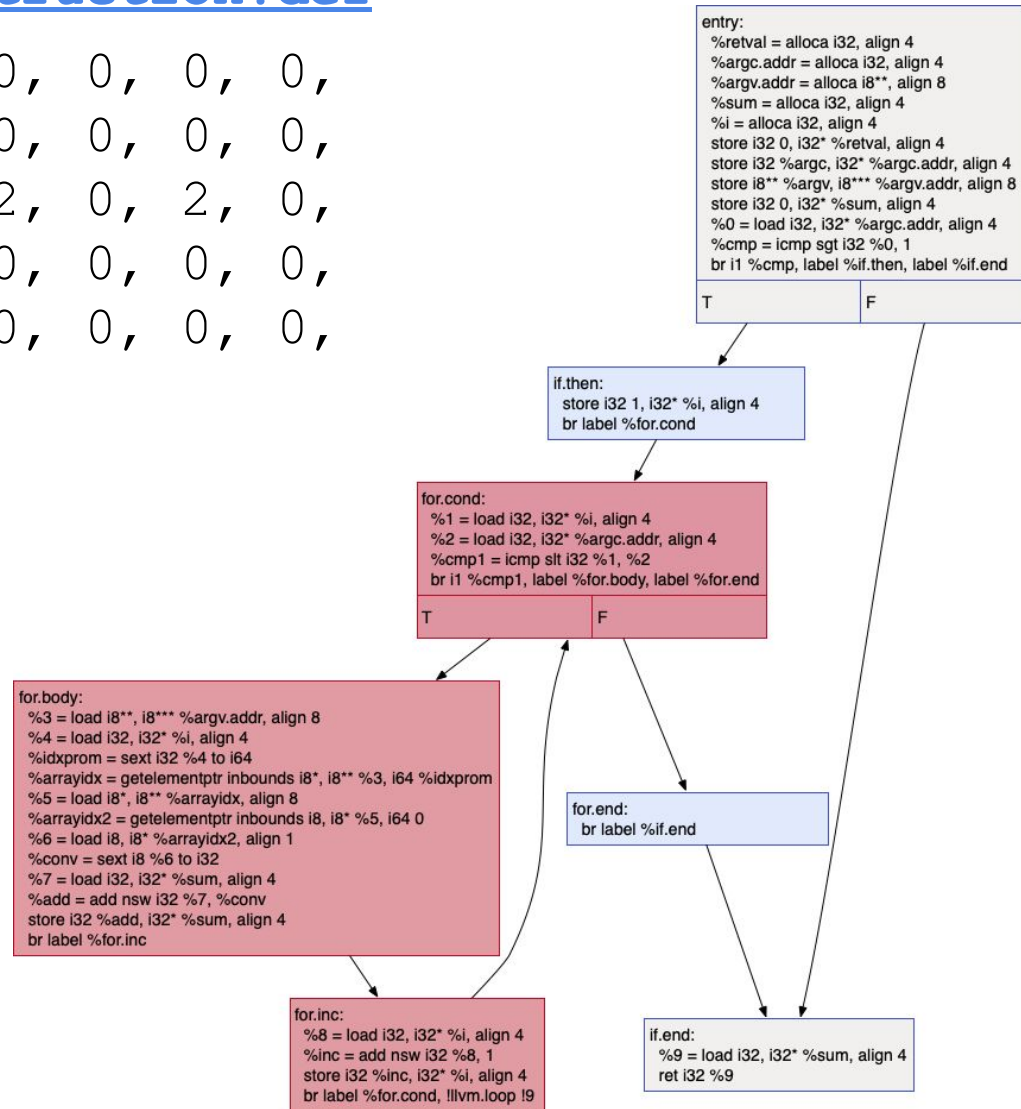


Histograms

[llvm/include/llvm/IR/Instruction.def](#)

```
0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
```

How to use the histogram to predict the effect of a sequence of optimizations on a program?



Input:

```
0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,  
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0
```

```
-mem2reg -jump-threading -instcombine -early-cse-memssa -jump-threading -licm -early-cse-memssa  
-sroa -simplifycfg -reassociate -instcombine -slp-vectorizer -early-cse-memssa
```

Input:

```
0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,  
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0
```

```
-mem2reg -jump-threading -instcombine -early-cse-memssa -jump-threading -licm -early-cse-memssa  
-sroa -simplifycfg -reassociate -instcombine -slp-vectorizer -early-cse-memssa
```

Output:

13 instructions

Input:

```
0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0
```

Br

Switch

FAdd

FSub

Or

Xor

Store

GetElementPtr

FPToUI

Feature Engineering

```
0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,  
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0
```

Br

Switch

FAdd

FSub

Or

Xor

Store

GetElementPtr

FPToUI

Feature Engineering

0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0

Embedding: (6, 0, 2, 0, 0, 0, 0, 2, 0)

Br

Switch

FAdd

FSub

Or

Xor

Store

GetElementPtr

FPToUI

Feature Engineering

0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0

Embedding: (6, 0, 2, 0, 0, 0, 0, 2, 0)

$$N_{seq} = C_{br} Br + C_{switch} Switch + C_{FAdd} FAdd + C_{FSub} FSub + C_{Or} Or + C_{Xor} Xor \\ + C_{Store} Store + C_{GetElementPtr} GetElementPtr + C_{FPToUI} FPToUI + C$$

Feature Engineering

0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0

Embedding: (6, 0, 2, 0, 0, 0, 0, 2, 0)

N_{seq}

Linear Model

0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0

Embedding: (6, 0, 2, 0, 0, 0, 0, 2, 0)

$$N_{\text{seq}} = C_{\text{br}} \text{Br} + C_{\text{switch}} \text{Switch} + C_{\text{FAdd}} \text{FAdd} + C_{\text{FSub}} \text{FSub} + C_{\text{Or}} \text{Or} + C_{\text{Xor}} \text{Xor} \\ + C_{\text{Store}} \text{Store} + C_{\text{GetElementPtr}} \text{GetElementPtr} + C_{\text{FPToUI}} \text{FPToUI} + C$$

Linear Model

0,	1,	6,	0,	0,	0,	0,	0,	0,	0,	0,	0,	0,
0,	2,	0,	0,	0,	0,	0,	0,	0,	0,	0,	0,	0,
0,	0,	0,	0,	0,	0,	0,	0,	2,	0,	2,	0,	0,
0,	0,	0,	0,	2,	0,	0,	0,	0,	0,	0,	0,	0,
0,	0,	0,	0,	0,	2,	0,	3,	0,	0,	0,	0,	0,
0,	0,	0,	0,	0,	0,							

Embedding: (6, 0, 2, 0, 0, 0, 0, 2, 0)

$$N_{\text{seq}} = C_{\text{br}} \text{Br} + C_{\text{switch}} \text{Switch} + C_{\text{FAdd}} \text{FAdd} + C_{\text{FSub}} \text{FSub} + C_{\text{Or}} \text{Or} + C_{\text{Xor}} \text{Xor} \\ + C_{\text{Store}} \text{Store} + C_{\text{GetElementPtr}} \text{GetElementPtr} + C_{\text{FPToUI}} \text{FPToUI} + C$$

Linear Regression

$$N_{\text{seq}} = C_{\text{br}} \text{Br} + C_{\text{switch}} \text{Switch} + C_{\text{FAdd}} \text{FAdd} + C_{\text{FSub}} \text{FSub} + C_{\text{Or}} \text{Or} + C_{\text{Xor}} \text{Xor} \\ + C_{\text{Store}} \text{Store} + C_{\text{GetElementPtr}} \text{GetElementPtr} + C_{\text{FPToUI}} \text{FPToUI} + C$$

Linear Regression

And how do we find all these constants?

$$N_{\text{seq}} = C_{\text{br}} \text{Br} + C_{\text{switch}} \text{Switch} + C_{\text{FAdd}} \text{FAdd} + C_{\text{FSub}} \text{FSub} + C_{\text{Or}} \text{Or} + C_{\text{Xor}} \text{Xor} \\ + C_{\text{Store}} \text{Store} + C_{\text{GetElementPtr}} \text{GetElementPtr} + C_{\text{FPToUI}} \text{FPToUI} + C$$

Training!

$$N_{\text{seq}} = C_{\text{br}} \text{Br} + C_{\text{switch}} \text{Switch} + C_{\text{FAdd}} \text{FAdd} + C_{\text{FSub}} \text{FSub} + C_{\text{Or}} \text{Or} + C_{\text{Xor}} \text{Xor} \\ + C_{\text{Store}} \text{Store} + C_{\text{GetElementPtr}} \text{GetElementPtr} + C_{\text{FPToUI}} \text{FPToUI} + C$$

Training!

► Data

$$N_{\text{seq}} = C_{\text{br}} \text{Br} + C_{\text{switch}} \text{Switch} + C_{\text{FAdd}} \text{FAdd} + C_{\text{FSub}} \text{FSub} + C_{\text{Or}} \text{Or} + C_{\text{Xor}} \text{Xor} \\ + C_{\text{Store}} \text{Store} + C_{\text{GetElementPtr}} \text{GetElementPtr} + C_{\text{FPToUI}} \text{FPToUI} + C$$

Training!

► Data - Programs

$$N_{\text{seq}} = C_{\text{br}} \text{Br} + C_{\text{switch}} \text{Switch} + C_{\text{FAdd}} \text{FAdd} + C_{\text{FSub}} \text{FSub} + C_{\text{Or}} \text{Or} + C_{\text{Xor}} \text{Xor} \\ + C_{\text{Store}} \text{Store} + C_{\text{GetElementPtr}} \text{GetElementPtr} + C_{\text{FPToUI}} \text{FPToUI} + C$$

Training!

► Data - Programs - Histograms

$$N_{\text{seq}} = C_{\text{br}} \text{Br} + C_{\text{switch}} \text{Switch} + C_{\text{FAdd}} \text{FAdd} + C_{\text{FSub}} \text{FSub} + C_{\text{Or}} \text{Or} + C_{\text{Xor}} \text{Xor} \\ + C_{\text{Store}} \text{Store} + C_{\text{GetElementPtr}} \text{GetElementPtr} + C_{\text{FPToUI}} \text{FPToUI} + C$$

Training!

▶ Data - Programs - Histograms

Br

Switch

FAdd

FSub

Or

Xor

Store

GetElementPtr

FPToUI

Training!

Data - Programs - Histograms

```
bool Histogram::runOnFunction(llvm::Function& function) {
    llvm::DenseMap<unsigned, unsigned> hist;
    hist.init(NUM_OPCODES);
    for (llvm::Instruction &inst: llvm::instructions(function)) {
        const unsigned op_code = inst.getOpcode();
        hist[op_code]++;
    }
}
```

Training!

▶ Data - Programs - Histograms

▶ Calibrate a Linear Model

Example: Linear Model in R

- ▶ Data - Programs - Histograms
- ▶ Calibrate a Linear Model



Example: Linear Model in R

https://www.dcc.ufmg.br/~fernando/classes/dcc888/ementa/data_ml/leaf_functions_angha.csv

Example: Linear Model in R

```
file_name = "~/Downloads/leaf_functions_angha.csv"
```



Example: Linear Model in R

```
file_name = "~/Downloads/leaf_functions_angha.csv"
```

```
data <- data[sample(1:nrow(data)), ]
```



Example: Linear Model in R

```
file_name = "~/Downloads/leaf_functions_angha.csv"
```

```
data <- data[sample(1:nrow(data)), ]
```

```
train_size <- ceiling(0.8*nrow(data))
```

```
train <- data[1:train_size,]
```



Example: Linear Model in R

```
file_name = "~/Downloads/leaf_functions_angha.csv"
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data <- data[sample(1:nrow(data)), ]
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train <- data[1:train_size,]
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Example: Linear Model in R

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file_name = "~/Downloads/leaf_functions_angha.csv"

data <- data[sample(1:nrow(data)), ]

train_size <- ceiling(0.8*nrow(data))

train <- data[1:train_size,]

model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor
+ Store + GetElementPtr + FPToUI, data=train)
```



Example: Linear Model in R

```
file_name = "~/Downloads/leaf_functions_angha.csv"

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Example: Linear Model in R

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Example: Linear Model in R

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Example: Linear Model in R

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```
model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor  
+ Store + GetElementPtr + FPToUI, data=train)
```

Benchmark	Zero	Ret	Br	Switch	IndirectBr	Inoke	mem2reg	O0	Os	Oz
extr_BGAQRCode-A	0	1	145	0	0	0	289	366	83	83
extr_BGAQRCode-A	0	1	62	0	0	0	238	327	99	99
extr_BGAQRCode-A	0	1	126	0	0	0	299	383	99	99

...

mem2reg	O0	Os	Oz
289	366	83	83
238	327	99	99
299	383	99	99

Example: Linear Model in R

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+ Store + GetElementPtr + FPToUI, data=train)
```

$$\begin{aligned} \text{Os} = & C_{\text{br}} \text{Br} + C_{\text{switch}} \text{Switch} + C_{\text{FAdd}} \text{FAdd} + C_{\text{FSub}} \text{FSub} + C_{\text{Or}} \text{Or} + C_{\text{Xor}} \text{Xor} \\ & + C_{\text{Store}} \text{Store} + C_{\text{GetElementPtr}} \text{GetElementPtr} + C_{\text{FPToUI}} \text{FPToUI} + C \end{aligned}$$



Example: Linear Model in R

```
file_name = "~/Downloads/leaf_functions_angha.csv"

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train_size <- ceiling(0.8*nrow(data))

train <- data[1:train_size,]

model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor
+ Store + GetElementPtr + FPToUI, data=train)

test <- data[(train_size+1):nrow(data),]

results <- predict(model, newdata = test)
```



Example: Linear Model in R

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Example: Linear Model in R

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train <- data[1:train_size,]

model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor
+ Store + GetElementPtr + FPToUI, data=train)

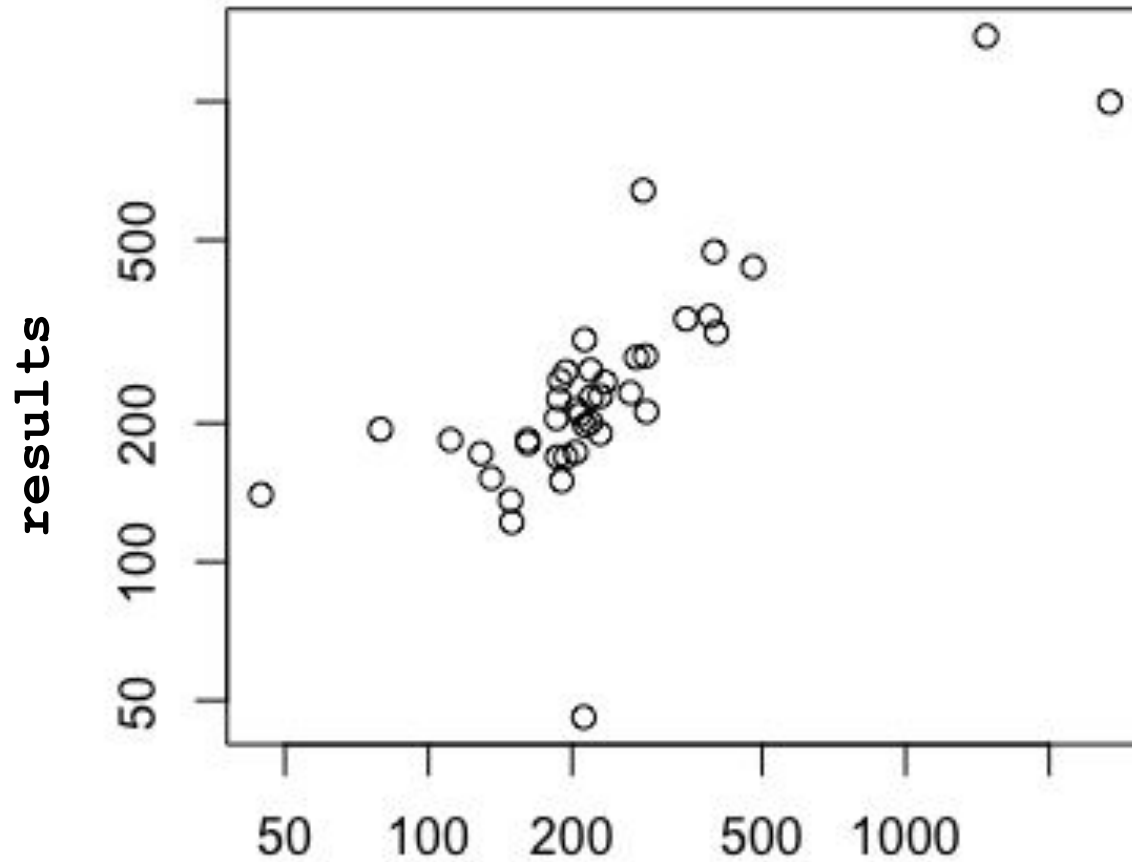
test <- data[(train_size+1):nrow(data),]

results <- predict(model, newdata = test)

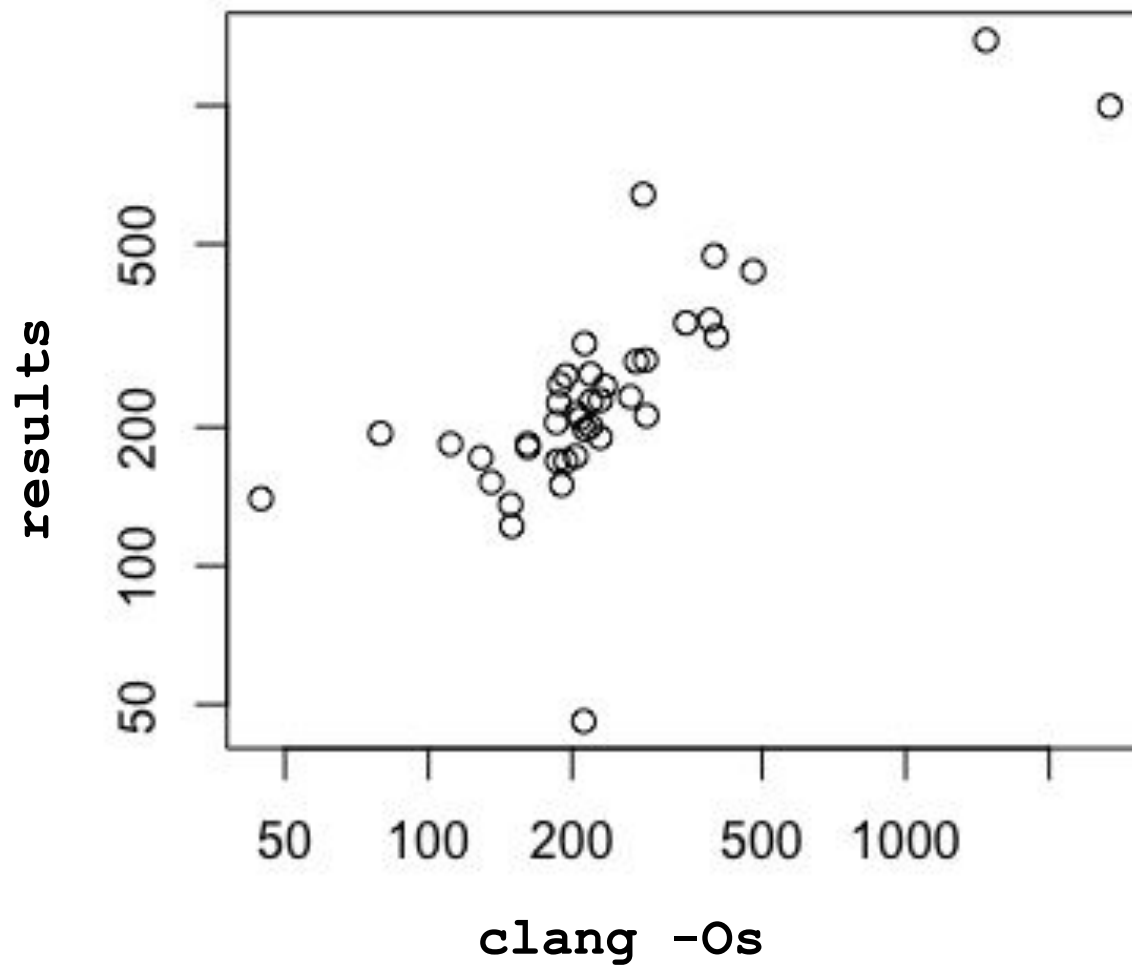
plot(test$Os ~ results, log = 'xy')
```



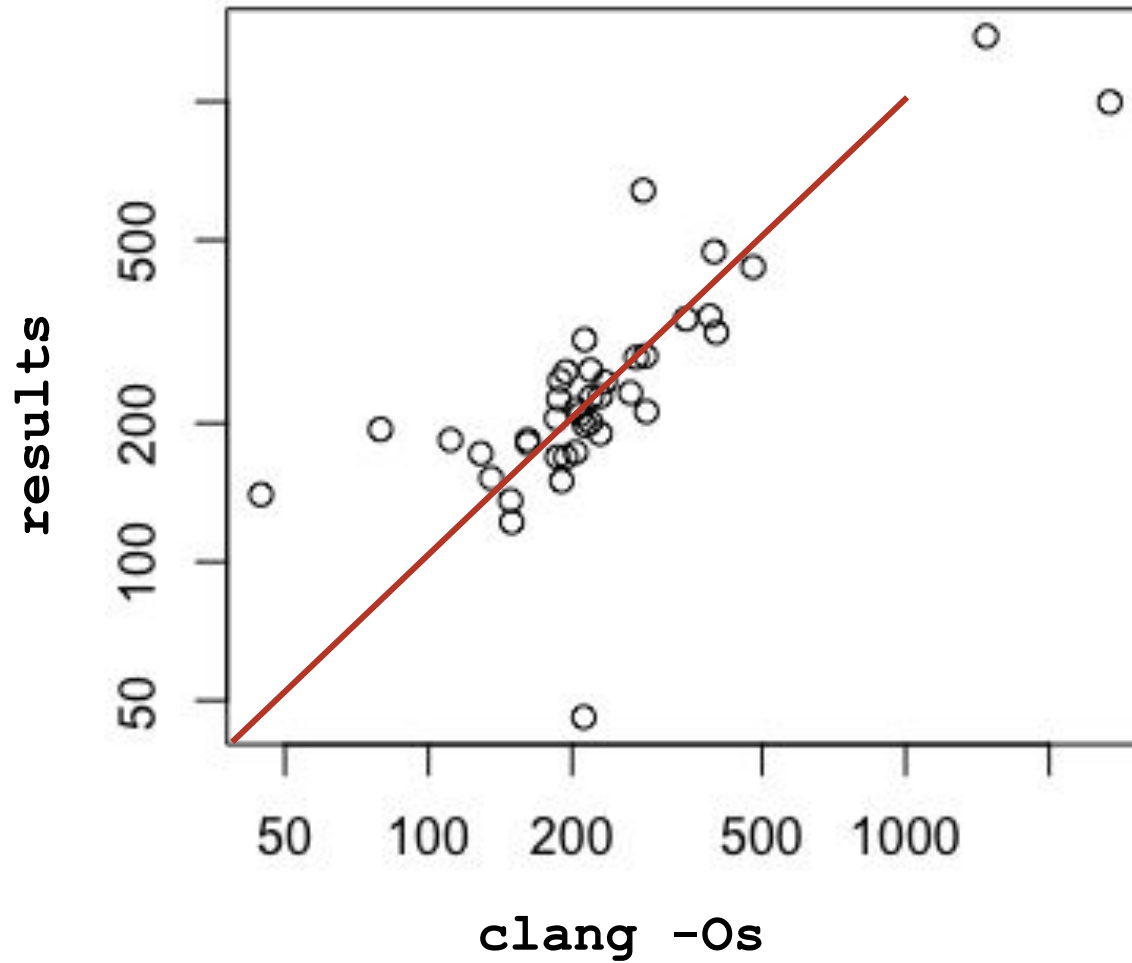
Example: Linear Model in R



Example: Linear Model in R



Example: Linear Model in R



Understanding the Model

```
model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor  
+ Store + GetElementPtr + FPToUI, data=train)
```



Understanding the Model

```
model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor  
+ Store + GetElementPtr + FPToUI, data=train)
```

$$N_{\text{seq}} = C_{\text{br}} \text{Br} + C_{\text{switch}} \text{Switch} + C_{\text{FAdd}} \text{FAdd} + C_{\text{FSub}} \text{FSub} + C_{\text{Or}} \text{Or} + C_{\text{Xor}} \text{Xor} \\ + C_{\text{Store}} \text{Store} + C_{\text{GetElementPtr}} \text{GetElementPtr} + C_{\text{FPToUI}} \text{FPToUI} + C$$

Understanding the Model

```
model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor  
+ Store + GetElementPtr + FPToUI, data=train)
```

```
summary(model)
```

$$N_{\text{seq}} = C_{\text{br}} \text{Br} + C_{\text{switch}} \text{Switch} + C_{\text{FAdd}} \text{FAdd} + C_{\text{FSub}} \text{FSub} + C_{\text{Or}} \text{Or} + C_{\text{Xor}} \text{Xor} \\ + C_{\text{Store}} \text{Store} + C_{\text{GetElementPtr}} \text{GetElementPtr} + C_{\text{FPToUI}} \text{FPToUI} + C$$

Understanding the Model

```
model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor  
+ Store + GetElementPtr + FPToUI, data=train)
```

```
summary(model)
```

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	-0.8488	12.4278	-0.068	0.945638
Br	1.0078	0.1318	7.645	2.10e-12 ***
Switch	-13.5785	6.6421	-2.044	0.042627 *
FAdd	2.0047	0.3191	6.283	3.25e-09 ***
FSub	-0.4547	0.4290	-1.060	0.290803
Or	2.1505	0.5011	4.292	3.12e-05 ***
Xor	1.1496	1.2677	0.907	0.365881
Store	1.1631	0.1323	8.794	2.71e-15 ***
GetElementPtr	2.0685	0.1940	10.663	< 2e-16 ***
FPToUI	0.8268	0.2223	3.719	0.000279 ***

$$N_{seq} = C_{br} Br + C_{switch} Switch + C_{FAdd} FAdd + C_{FSub} FSub + C_{Or} Or + C_{Xor} Xor \\ + C_{Store} Store + C_{GetElementPtr} GetElementPtr + C_{FPToUI} FPToUI + C$$

Understanding the Model

```
model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor  
+ Store + GetElementPtr + FPToUI, data=train)
```

```
summary(model)
```



Br 1.0078

$$N_{\text{seq}} = C_{\text{br}} \text{Br} + C_{\text{switch}} \text{Switch} + C_{\text{FAdd}} \text{FAdd} + C_{\text{FSub}} \text{FSub} + C_{\text{Or}} \text{Or} + C_{\text{Xor}} \text{Xor} \\ + C_{\text{Store}} \text{Store} + C_{\text{GetElementPtr}} \text{GetElementPtr} + C_{\text{FPToUI}} \text{FPToUI} + C$$

Understanding the Model

```
model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor  
+ Store + GetElementPtr + FPToUI, data=train)
```

```
summary(model)
```

(Intercept) -0.8488

$$N_{\text{seq}} = C_{\text{br}} \text{Br} + C_{\text{switch}} \text{Switch} + C_{\text{FAdd}} \text{FAdd} + C_{\text{FSub}} \text{FSub} + C_{\text{Or}} \text{Or} + C_{\text{Xor}} \text{Xor} \\ + C_{\text{Store}} \text{Store} + C_{\text{GetElementPtr}} \text{GetElementPtr} + C_{\text{FPToUI}} \text{FPToUI} + C$$

Understanding the Model

```
model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor  
+ Store + GetElementPtr + FPToUI, data=train)
```

```
summary(model)
```

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	-0.8488	12.4278	-0.068	0.945638	
Br	1.0078	0.1318	7.645	2.10e-12	***
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FPToUI	0.8268	0.2223	3.719	0.000279	***

$$N_{\text{seq}} = 1.0078\text{Br} - 13.5785\text{Switch} + 2.0047\text{FAdd} - 0.4547\text{FSub} + 2.1505\text{Or} \\ + 1.1496\text{Xor} + 1.1631\text{Store} + 2.0685\text{GetElementPtr} + 0.8268\text{FPToUI} \\ - 0.8488$$

Using the Model

```
model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor  
+ Store + GetElementPtr + FPToUI, data=train)
```

```
summary(model)
```

```
int main(int argc, char** argv) {  
    int sum = 0;  
    if (argc > 1) {  
        for (int i = 1; i < argc; i++) {  
            sum += (int)argv[i][0];  
        }  
    }  
    return sum;  
}
```

Using the Model

```
model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor  
+ Store + GetElementPtr + FPToUI, data=train)
```

```
summary(model)
```

```
0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,  
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0
```

Using the Model

```
model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor  
+ Store + GetElementPtr + FPToUI, data=train)
```

```
summary(model)
```

```
hf <- data.frame(Br = c(6), Switch = c(0), FAdd =  
c(2), FSub = c(0), Or = c(0), Xor = c(0), Store =  
c(0), GetElementPtr = c(2), FPToUI = c(0))
```

```
0, 1, 6, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 2, 0,  
0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 2, 0, 3, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0
```

Using the Model

```
model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor  
+ Store + GetElementPtr + FPToUI, data=train)
```

```
summary(model)
```

```
hf <- data.frame(Br = c(6), Switch = c(0), FAdd =  
c(2), FSub = c(0), Or = c(0), Xor = c(0), Store =  
c(0), GetElementPtr = c(2), FPToUI = c(0))
```

```
predict(model, newdata = hf)
```

```
13.34451
```

Using the Model

```
coefs <- c(1.0078, -13.5785, 2.0047, -0.4547, 2.1505,  
1.1496, 1.1631, 2.0685, 0.8268)
```

```
predict(model, newdata = hf)  
13.34451
```

Using the Model

```
coefs <- c(1.0078, -13.5785, 2.0047, -0.4547, 2.1505,  
1.1496, 1.1631, 2.0685, 0.8268)
```

```
histg <- c(6, 0, 2, 0, 0, 0, 0, 2, 0)
```

```
predict(model, newdata = hf)  
13.34451
```

Using the Model

```
coefs <- c(1.0078, -13.5785, 2.0047, -0.4547, 2.1505,  
1.1496, 1.1631, 2.0685, 0.8268)
```

```
histg <- c(6, 0, 2, 0, 0, 0, 0, 2, 0)
```

```
coefs %*% histg - 0.8488
```

```
      [,1]  
[1,] 13.3444
```

```
predict(model, newdata = hf)
```

```
13.34451
```

Using the Model

```
model <- lm(Os ~ Br + Switch + FAdd + FSub + Or + Xor  
+ Store + GetElementPtr + FPToUI, data=train)
```

```
summary(model)
```

```
hf <- data.frame(Br = c(6), Switch = c(0), FAdd =  
c(2), FSub = c(0), Or = c(0), Xor = c(0), Store =  
c(0), GetElementPtr = c(2), FPToUI = c(0))
```

```
predict(model, newdata = hf)  
13.34451
```

How would you check the number of instructions in the actual program, optimized with clang -Os?

Using the Model

```
clang -S -emit-llvm -Os file.c -o file.opt.ll
```

```
opt -instcount -stats -disable-output file.opt.ll
```

```
predict(model, newdata = hf)  
13.34451
```

How would you check the number of instructions in the actual program, optimized with clang -Os?

Using the Model

```
clang -S -emit-llvm -Os file.c -o file.opt.ll
```

```
opt -instcount -stats -disable-output file.opt.ll
```

```
2 instcount - Number of Add insts  
3 instcount - Number of Br insts  
...  
1 instcount - Number of non-external functions  
16 instcount - Number of instructions (of all types)
```

```
predict(model, newdata = hf)  
13.34451
```

How would you check the number of instructions in the actual program, optimized with clang -Os?

Using the Model

```
clang -S -emit-llvm -O0 file.c -o file.opt.ll
```

```
opt -instcount -stats -disable-output file.opt.ll
```

```
2 instcount - Number of Add insts  
5 instcount - Number of Br insts  
...  
1 instcount - Number of non-external functions  
37 instcount - Number of instructions (of all types)
```

```
predict(model, newdata = hf)
```

```
13.34451
```

Other Examples

Other Examples

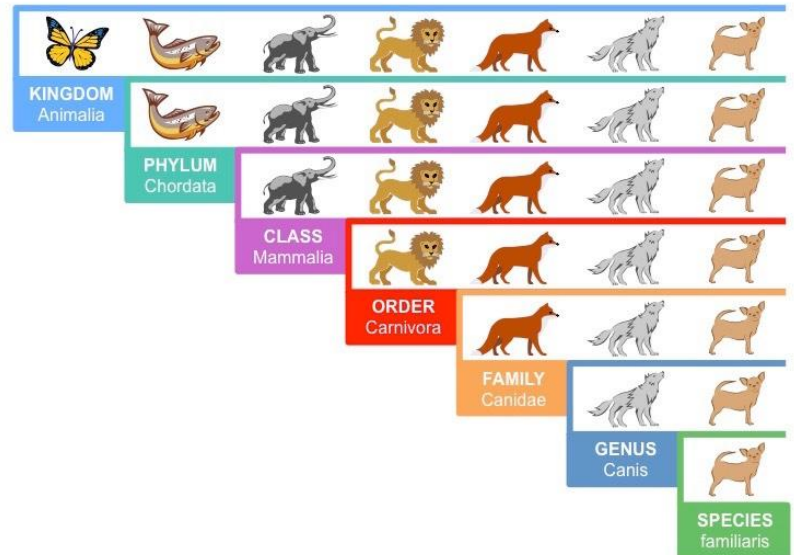
Fernando Magno Quintão Pereira, Guilherme V. Leobas, Abdoulaye Gamatié:
Static Prediction of Silent Stores.
ACM Trans. Archit. Code Optim. 15(4): 44:1-44:26 (2019)

Other Examples

Junio R. da Silva, Lorena Leão, Vinicius Petrucci, Abdoulaye Gamatié, Fernando M. Q. Pereira:
Mapping Computations in Heterogeneous Multicore Systems with Statistical Regression on Program Inputs. ACM Trans. Embed. Comput. Syst. 20(6): 112:1-112:35 (2021)

Fernando Magno Quintão Pereira, Guilherme V. Leobas, Abdoulaye Gamatié:
Static Prediction of Silent Stores.
ACM Trans. Archit. Code Optim. 15(4): 44:1-44:26 (2019)

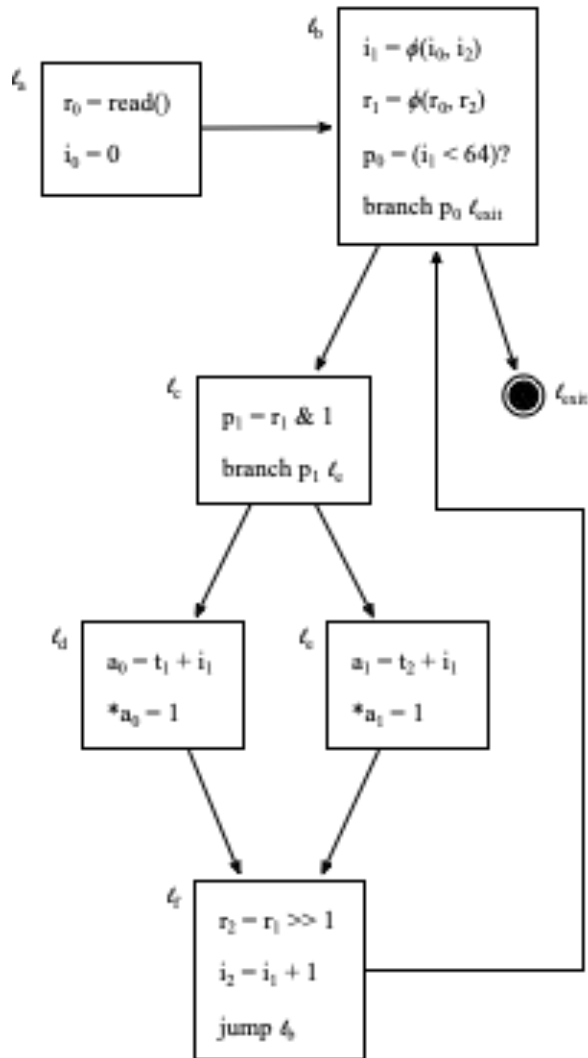
Classification



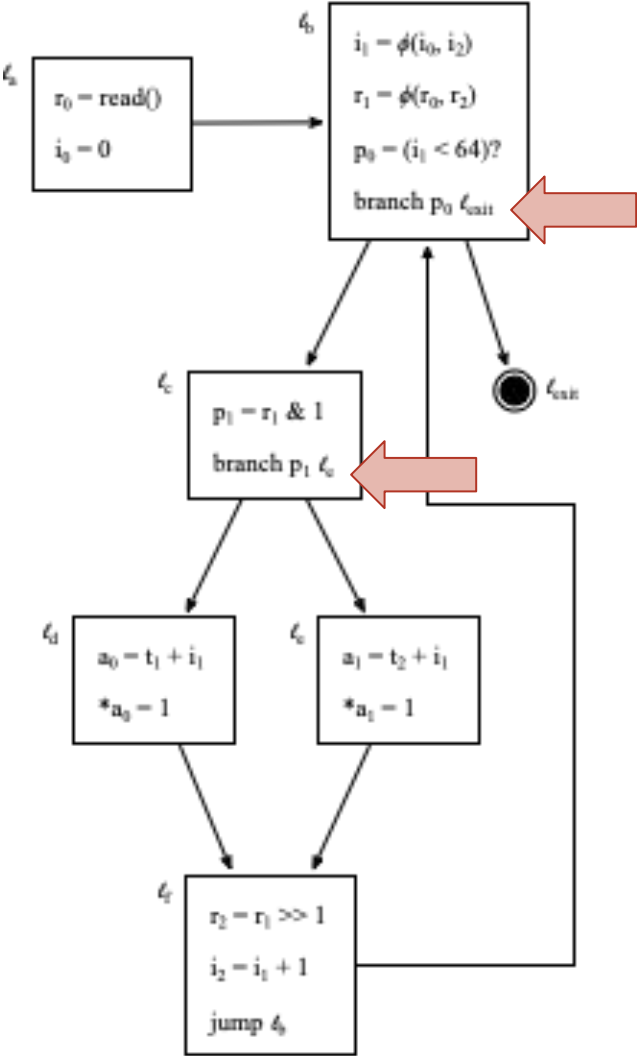
DCC888

Branches

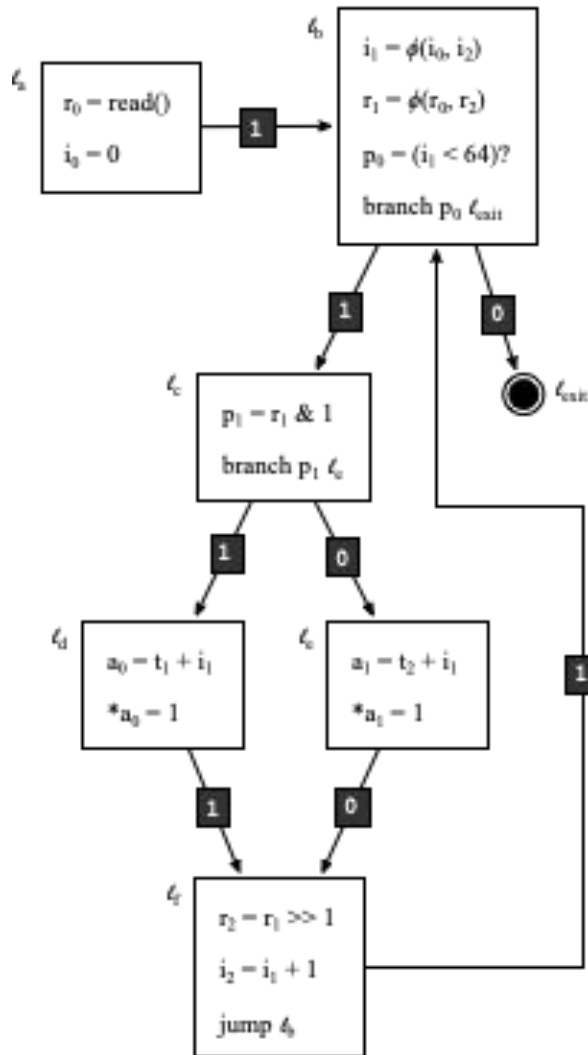
Branches



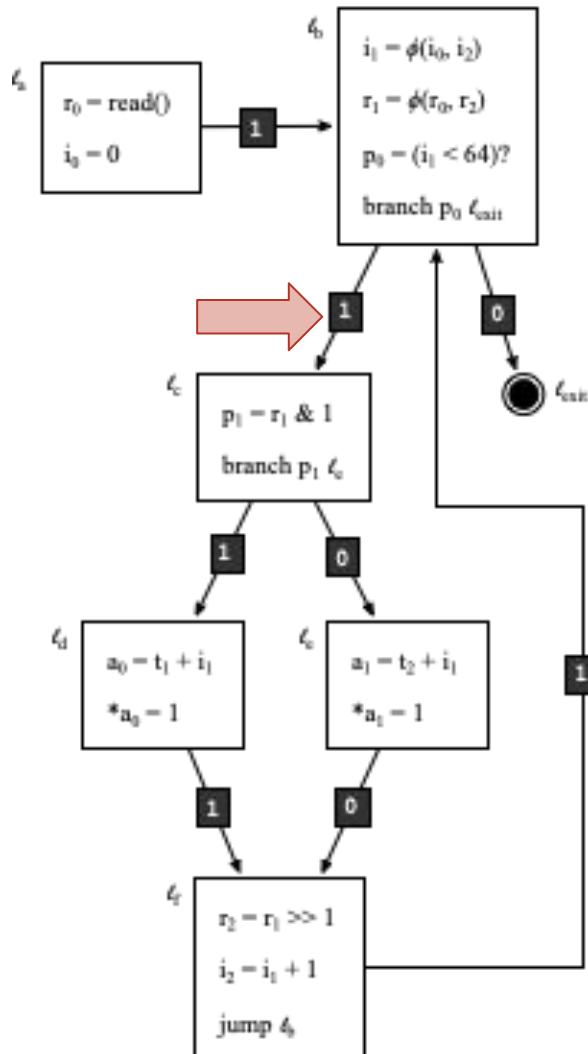
Branches



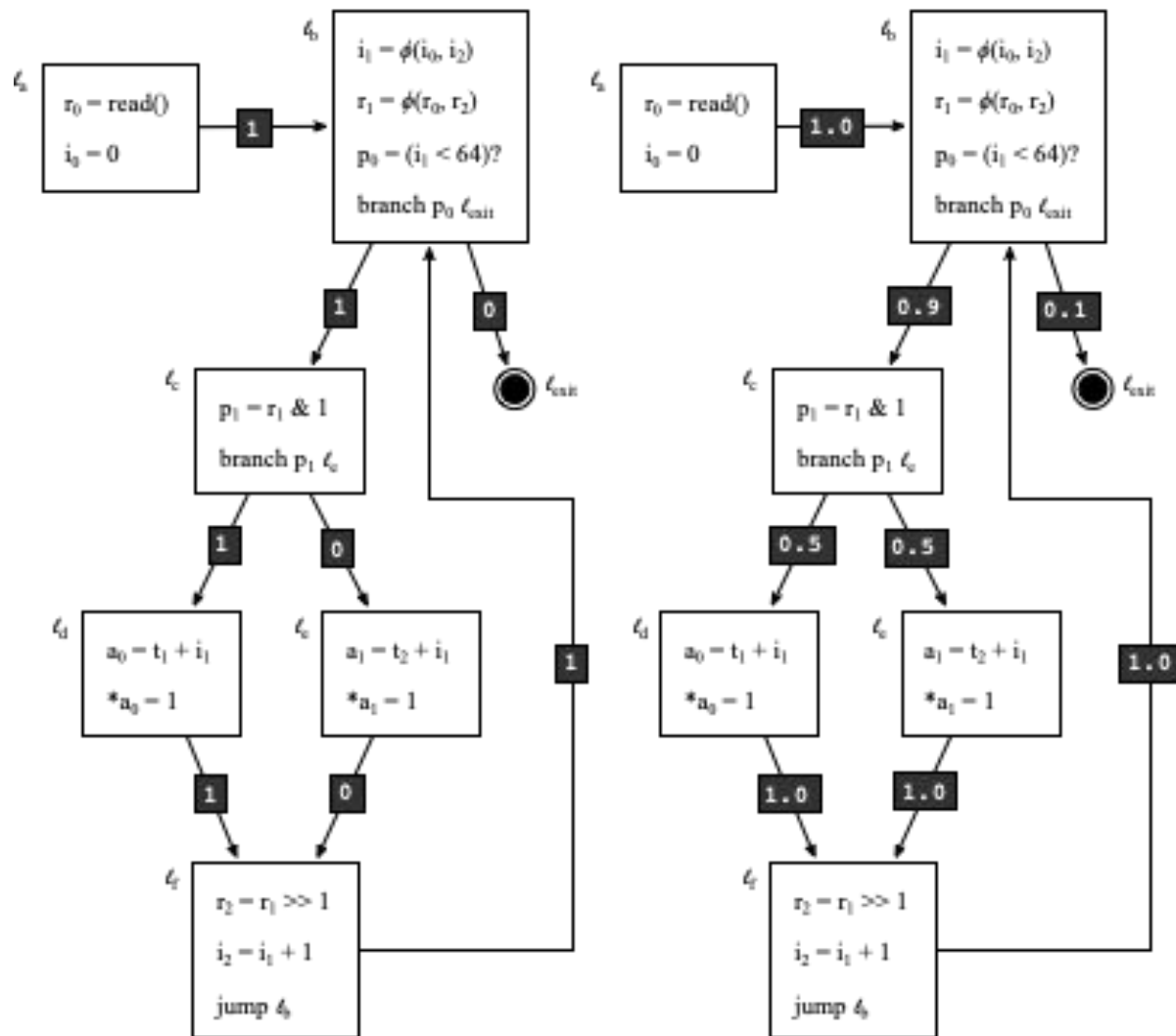
The Classification Problem



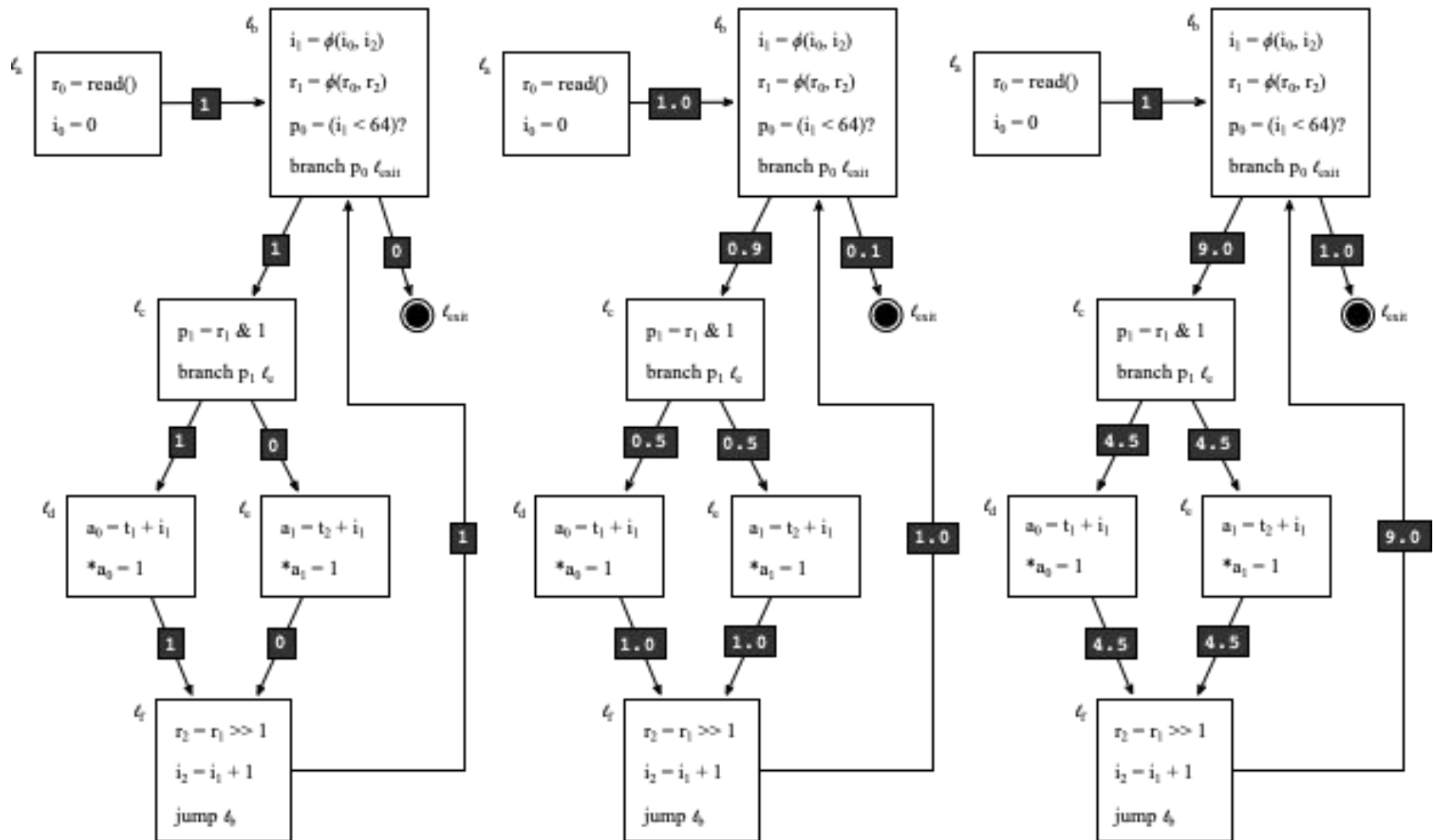
The Classification Problem



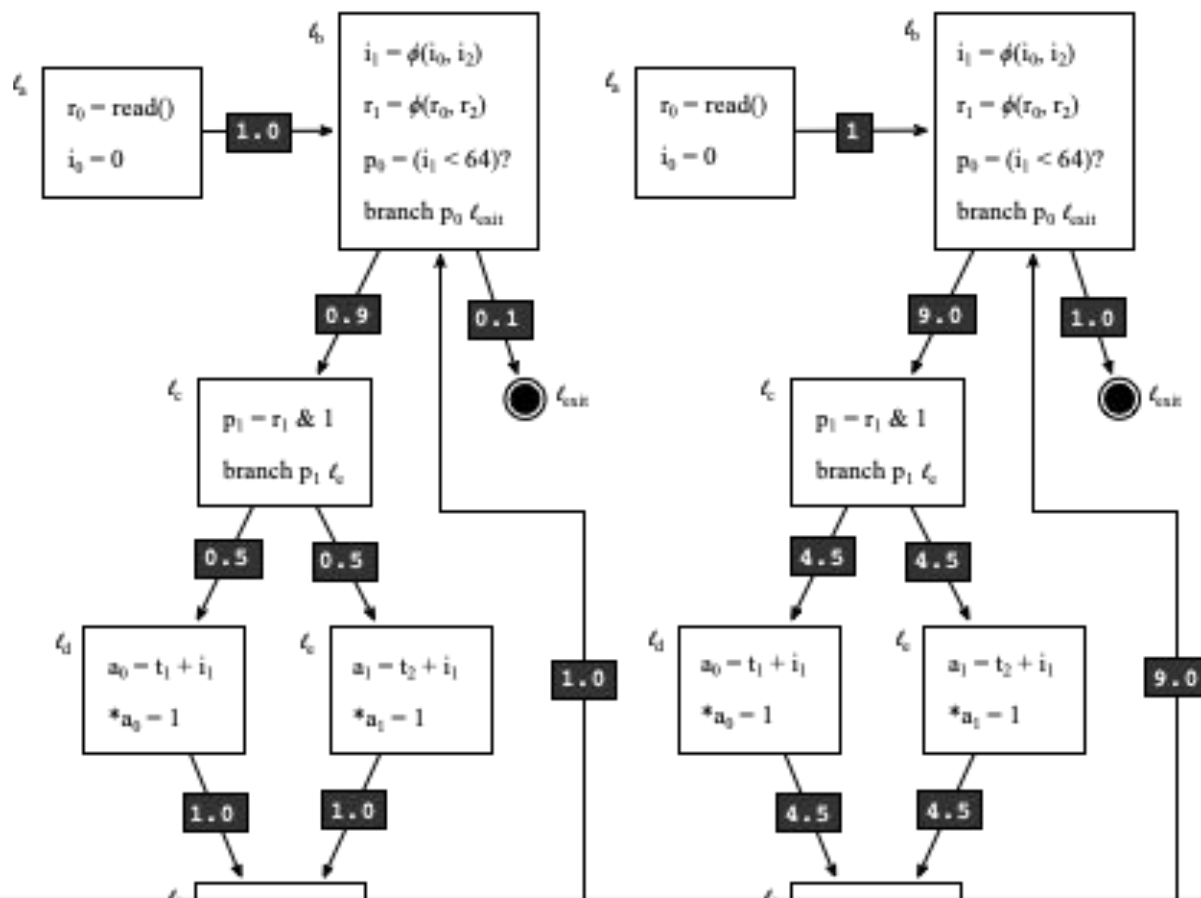
Probabilities



Regression Problems

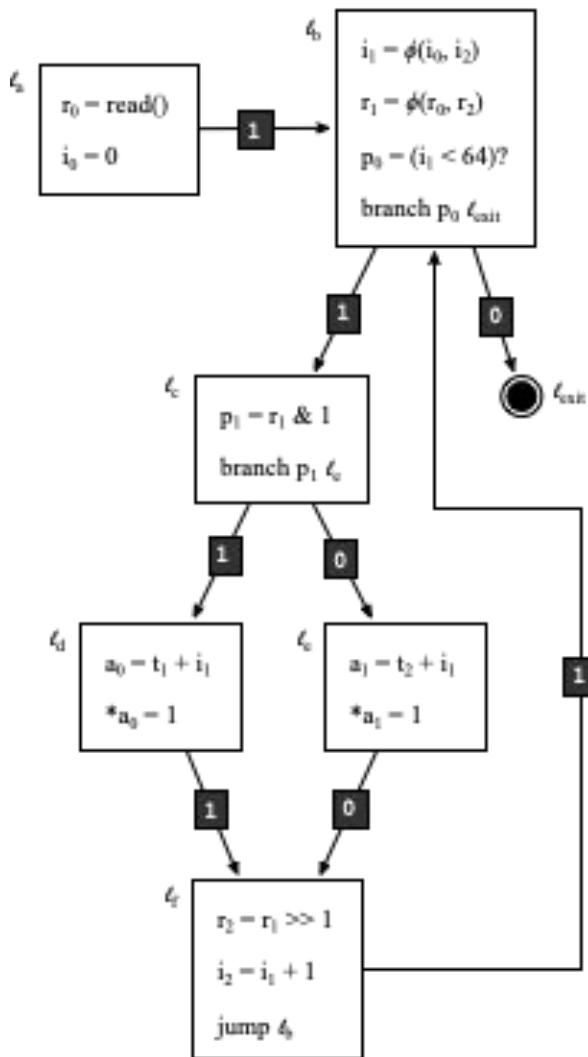


Regression Problems

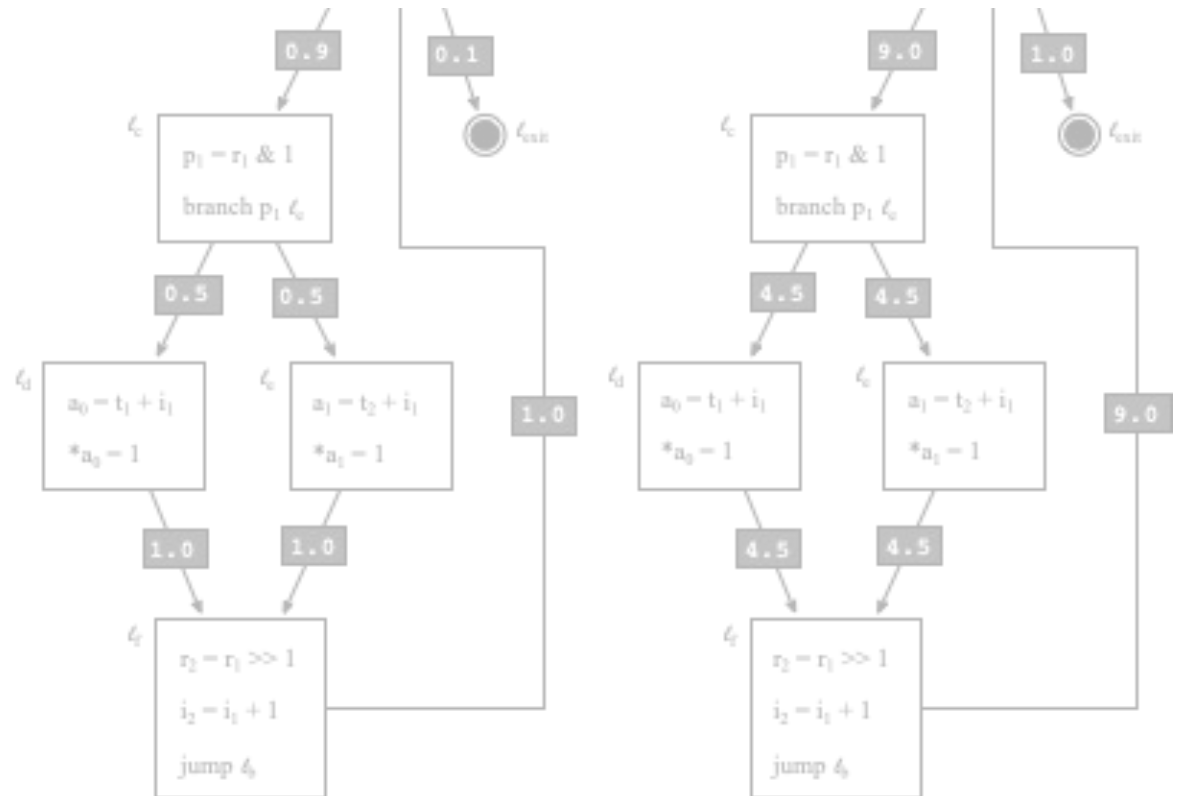


Angélica Aparecida Moreira, Guilherme Ottoni, Fernando Magno Quintão Pereira:
VESPA: static profiling for binary optimization.
 Proc. ACM Program. Lang. 5(OOPSLA): 1-28 (2021)

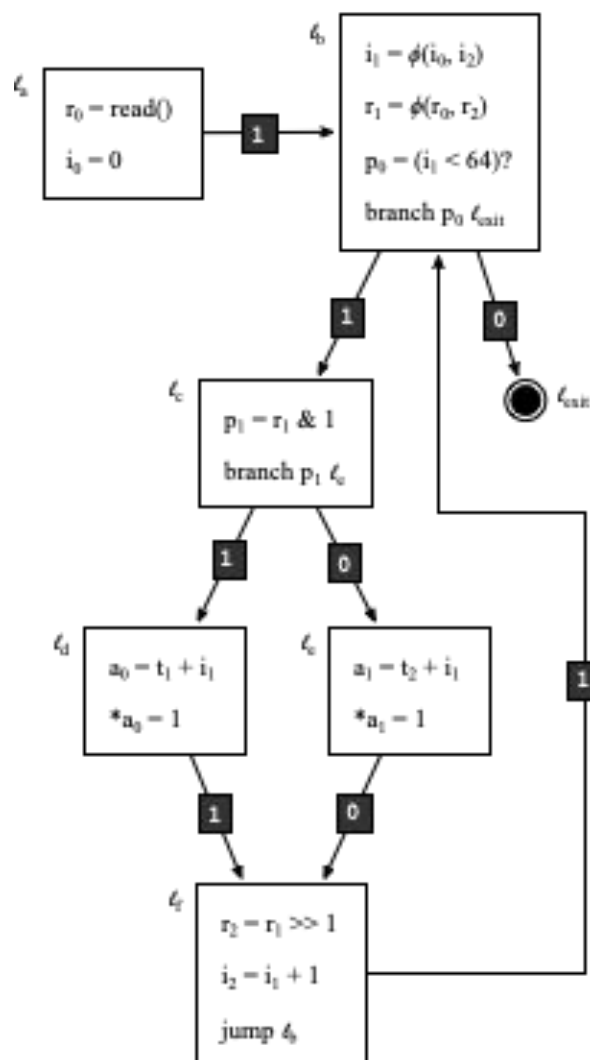
Predicting Branches



Brad Calder, Dirk Grunwald, M. Jones, Donald Lindsay, James Martin, Michael Mozer, B. Zorn:
Evidence-Based Static Branch Prediction Using Machine Learning.
 ACM Trans. Program. Lang. Syst. 19(1): 188-222 (1997)



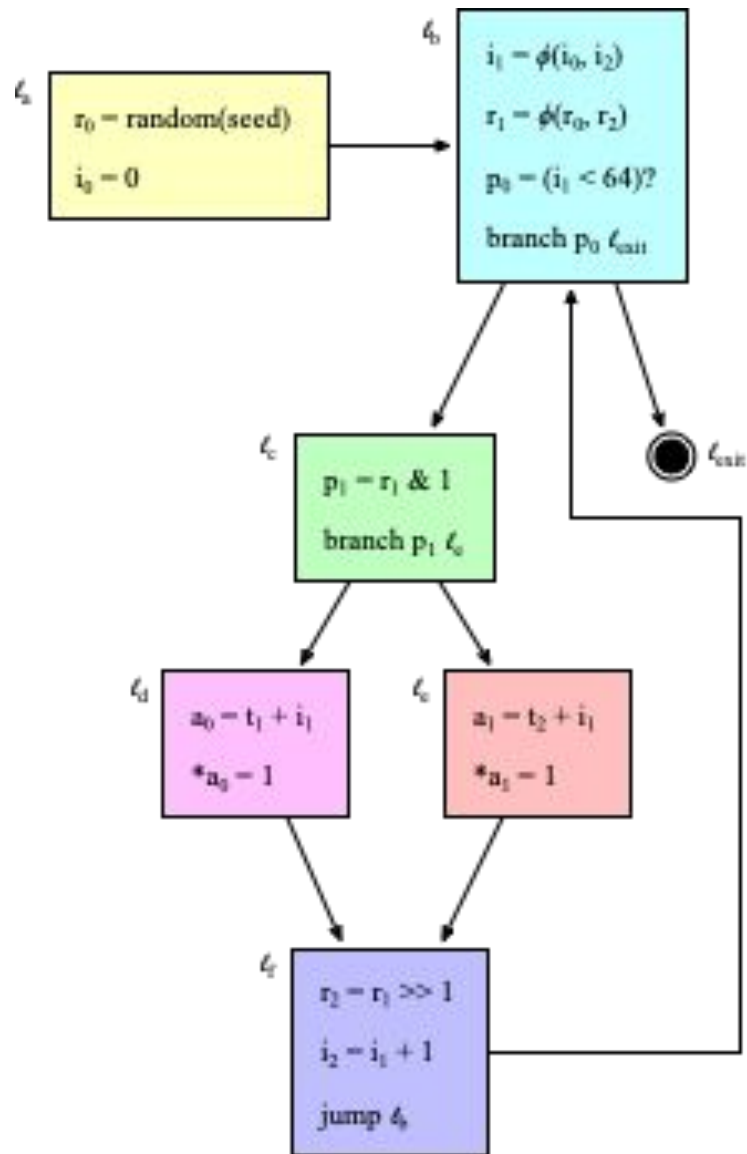
Some Motivation



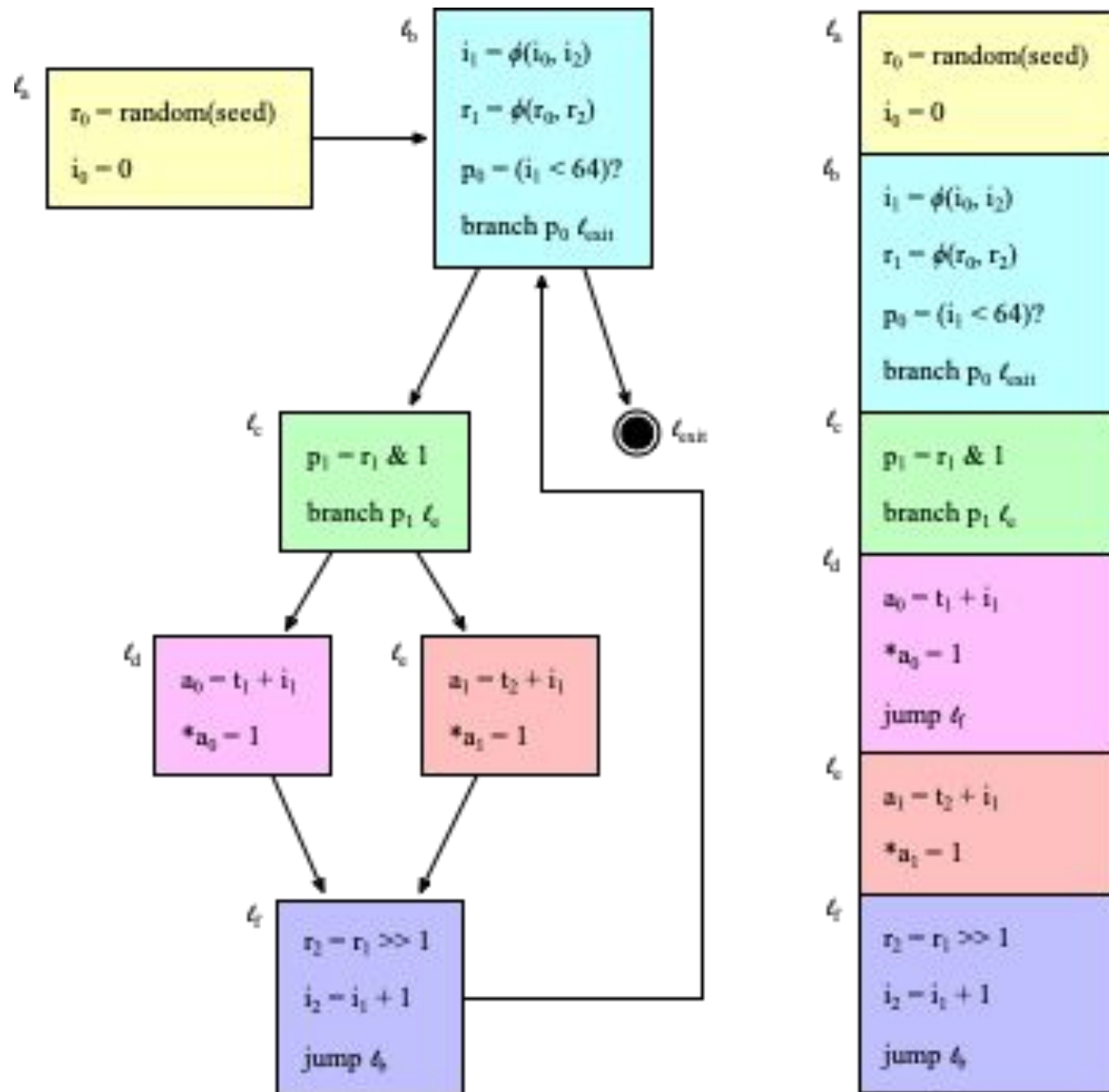
Brad Calder, Dirk Grunwald, M. Jones, Donald Lindsay, James Martin, Michael Mozer, B. Zorn:
Evidence-Based Static Branch Prediction Using Machine Learning.
ACM Trans. Program. Lang. Syst. 19(1): 188-222 (1997)

What can you do with this information?

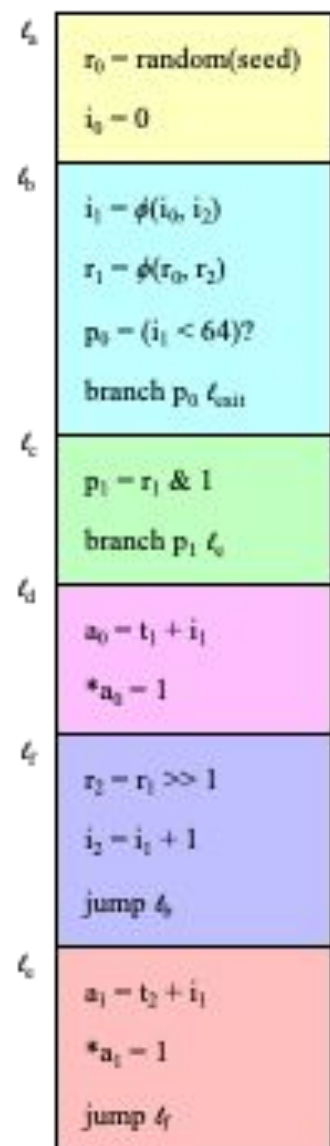
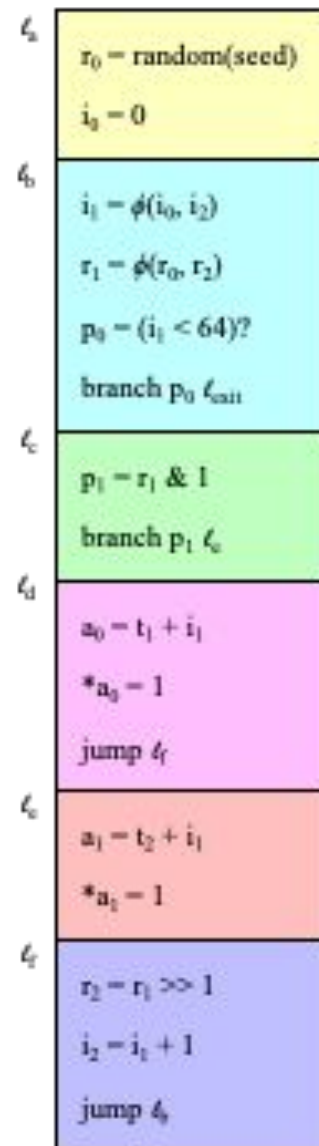
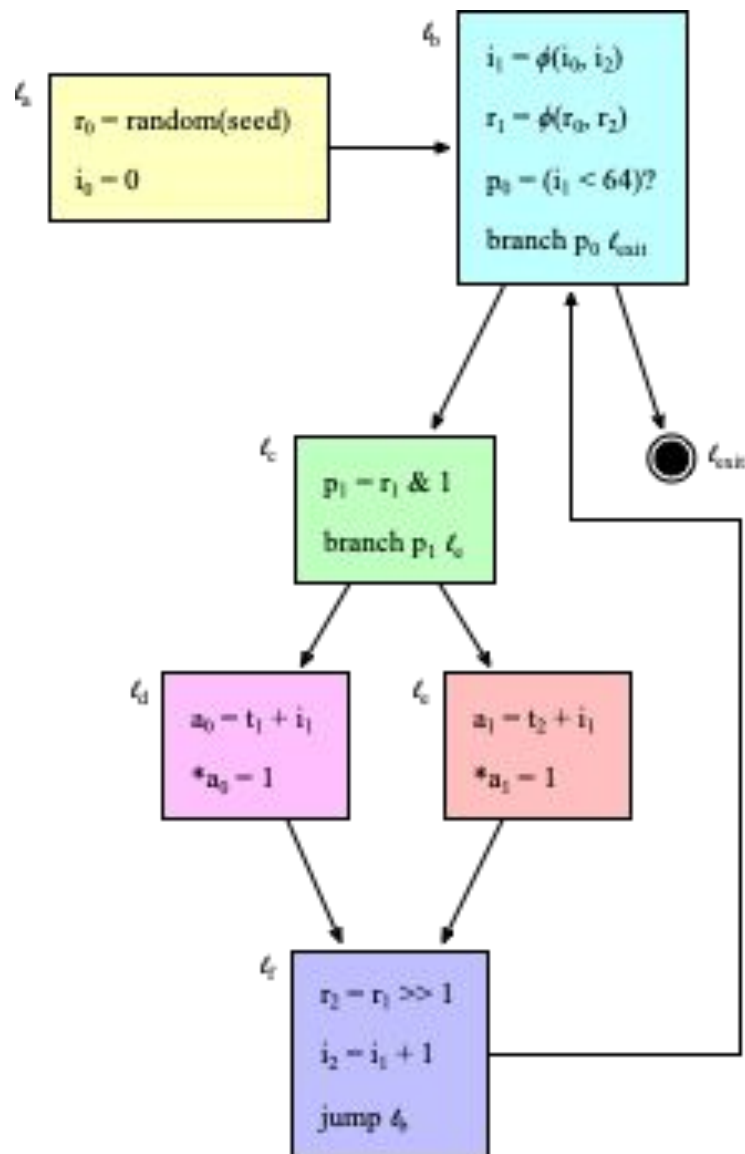
Some Motivation



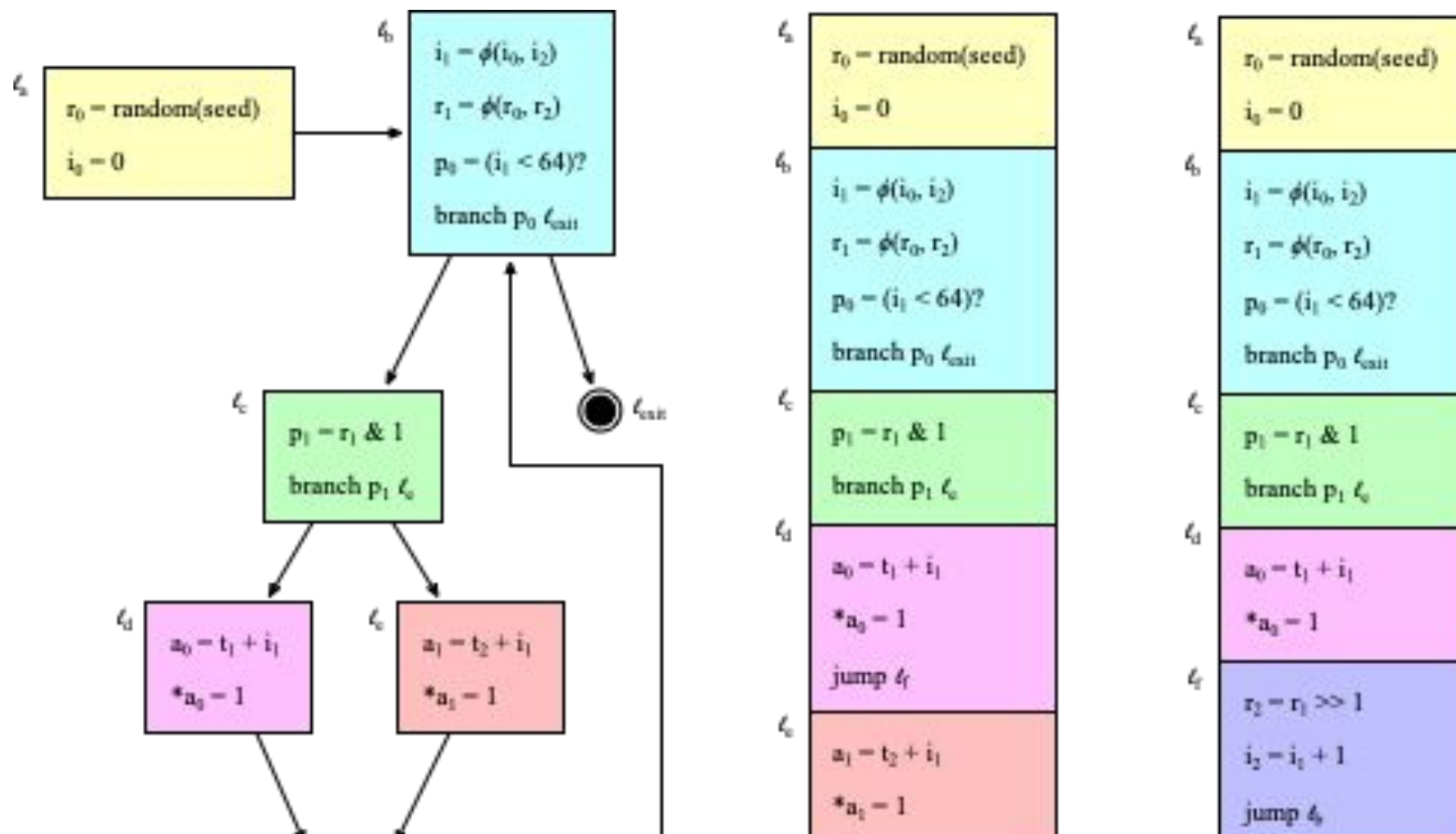
Some Motivation



Some Motivation



Some Motivation



Angélica Aparecida Moreira, Guilherme Ottoni, Fernando Magno Quintão Pereira:
VESPA: static profiling for binary optimization.
 Proc. ACM Program. Lang. 5(OOPSLA): 1-28 (2021)

Logistic Regression

Logistic Regression

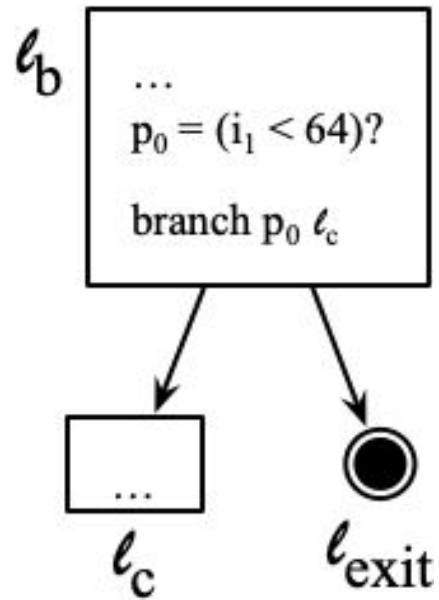
▶ Linear Regression

Logistic Regression

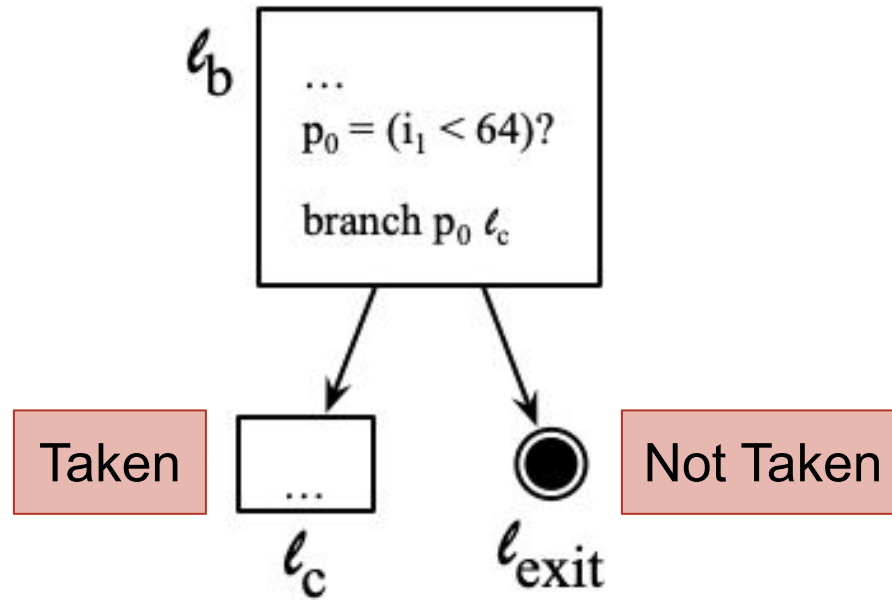
▶ ~~Linear Regression~~ Linear Classification

Branch Classification

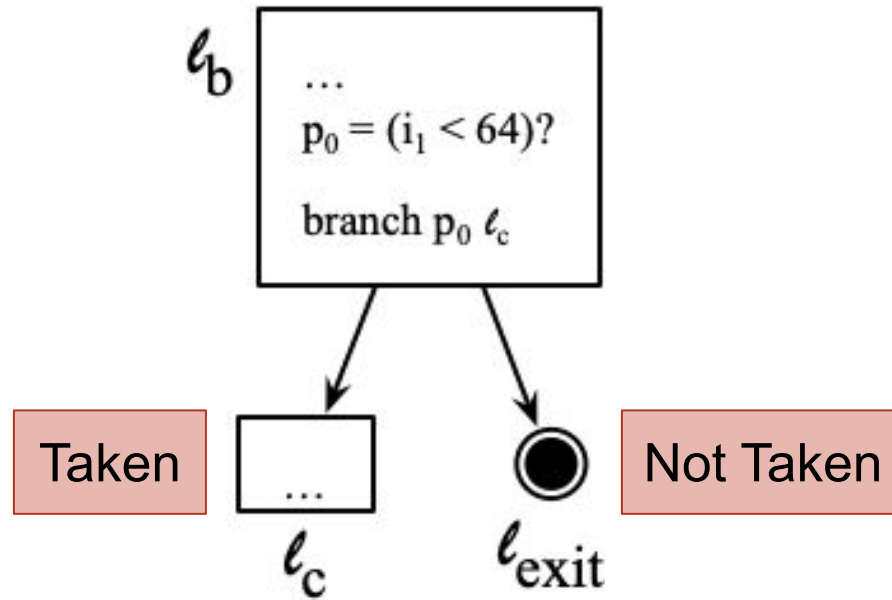
Branch Classification



Branch Classification

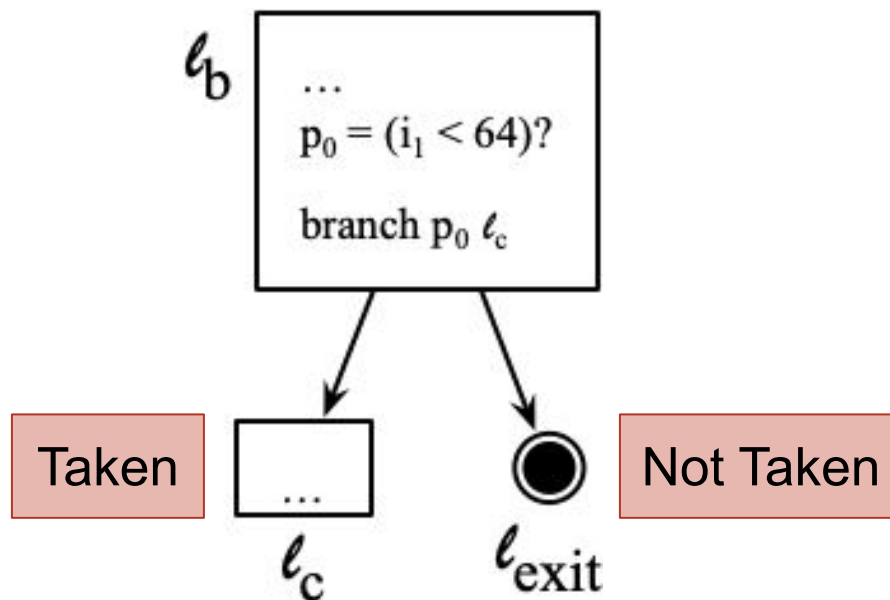


Branch Classification



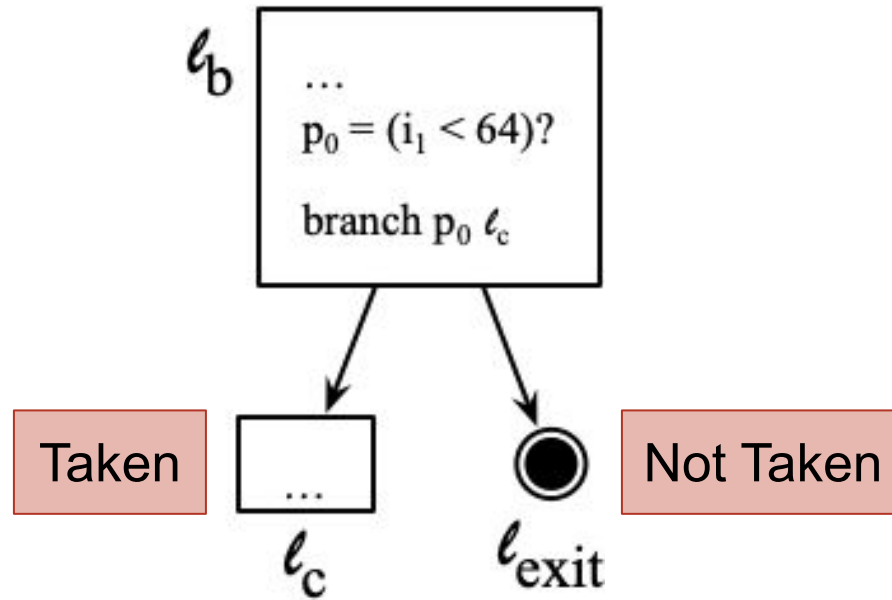
$$P_{\text{br}} = C_{\text{Break}} \text{Break} + C_{\text{BackEdge}} \text{BackEdge} + C_{\text{EqZero}} \text{EqZero} + C_{\text{IsZero}} \text{IsZero} \\ + C_{\text{NoPDom}} \text{NoPDom} + C_{\text{ToFun}} \text{ToFun} + C$$

Branch Classification



$$P_{\text{br}} = C_{\text{Break}} \text{Break} + C_{\text{BackEdge}} \text{BackEdge} + C_{\text{EqZero}} \text{EqZero} + C_{\text{IsZero}} \text{IsZero} \\ + C_{\text{NoPDom}} \text{NoPDom} + C_{\text{ToFun}} \text{ToFun} + C$$

The Logistic Function



$$P_{br} = \sigma(C_{Break} Break + C_{BackEdge} BackEdge + C_{EqZero} EqZero + C_{IsZero} IsZero + C_{NoPDom} NoPDom + C_{ToFun} ToFun + C)$$

The Logistic Function

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

$$P_{br} = \sigma(C_{Break} Break + C_{BackEdge} BackEdge + C_{EqZero} EqZero + C_{IsZero} IsZero + C_{NoPDom} NoPDom + C_{ToFun} ToFun + C)$$

The Logistic Function

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

```
sig <- function(x) {  
  1 / (1 + exp(-x))  
}
```

The Logistic Function

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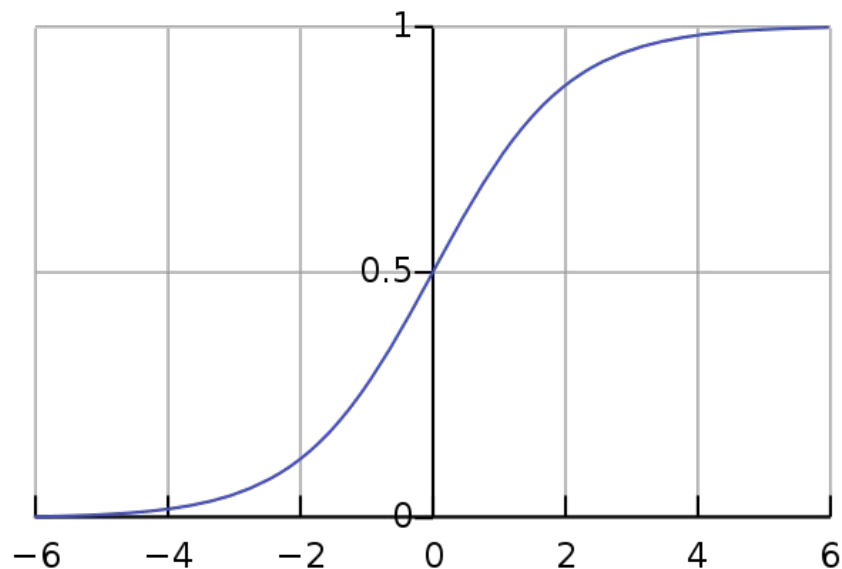
```
plot(sigmoid, -6, 6)
```

The Logistic Function

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

```
sig <- function(x) {  
  1 / (1 + exp(-x))  
}
```

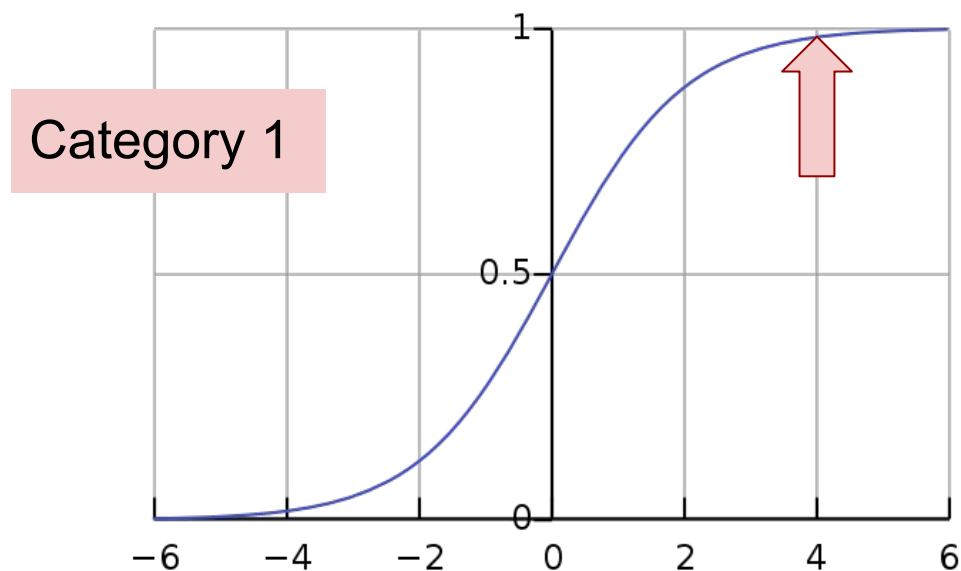
```
plot(sigmoid, -6, 6)
```



The Logistic Function

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

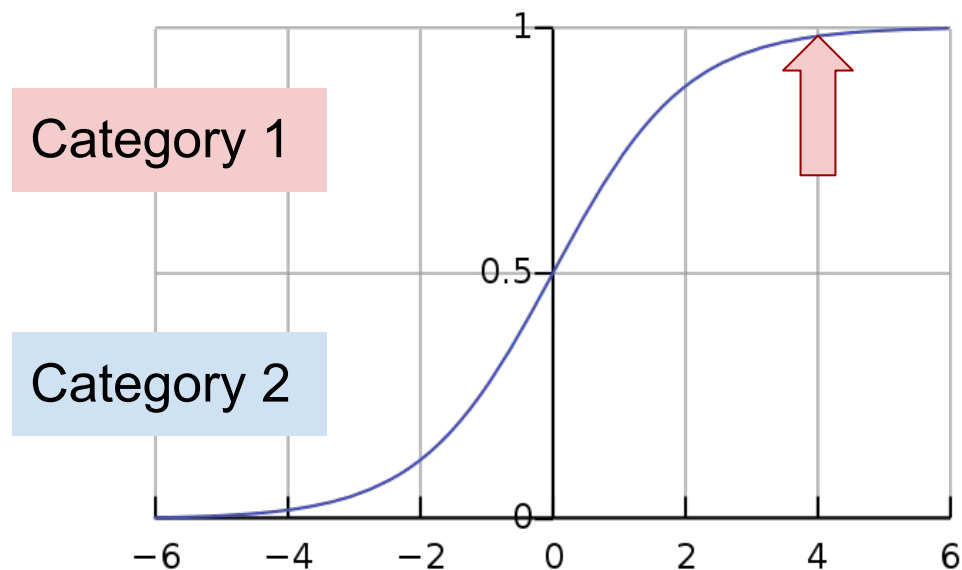
`sig(n) >= 0.5`



The Logistic Function

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

`sig(n) < 0.5`

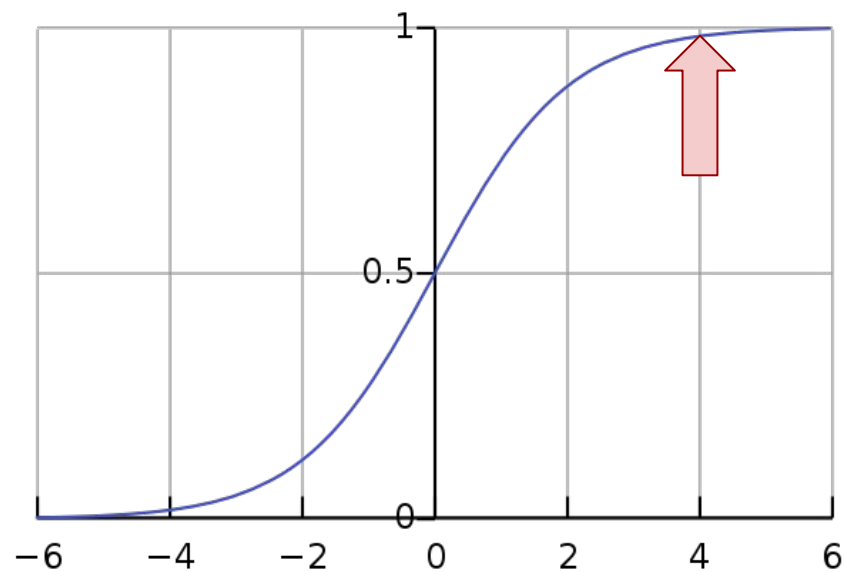


The Logistic Function

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

```
sig(4.0)
```

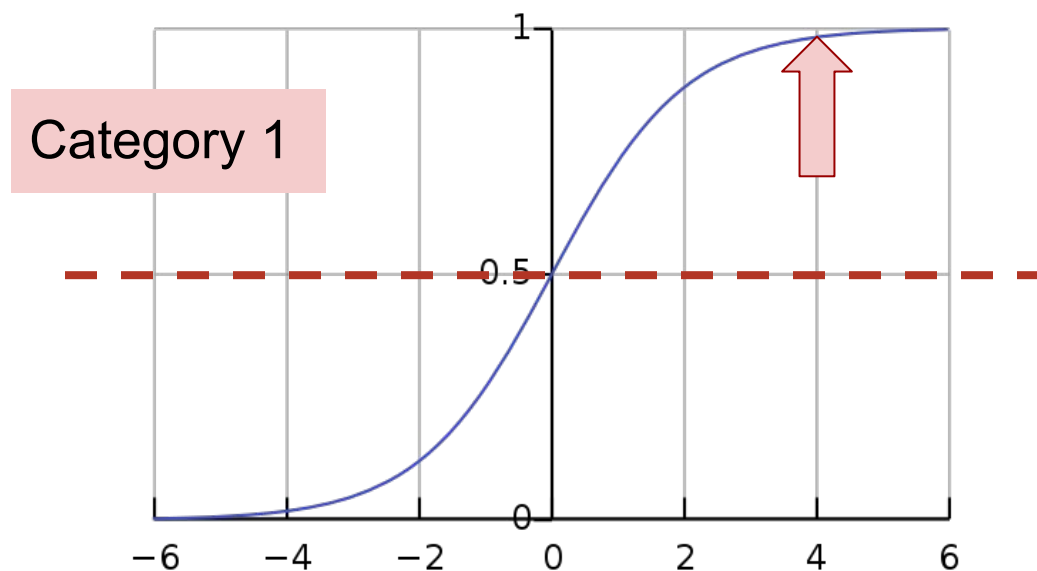
```
[1] 0.9820138
```



The Logistic Function

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

```
sig(4.0)  
[1] 0.9820138
```



Logistic Regression

$$P_{br} = \sigma(C_{Break} Break + C_{BackEdge} BackEdge + C_{EqZero} EqZero + C_{IsZero} IsZero + C_{NoPDom} NoPDom + C_{ToFun} ToFun + C)$$

Logistic Regression

$(C_{\text{Break}}, C_{\text{BackEdge}}, C_{\text{EqZero}}, C_{\text{IsZero}}, C_{\text{NoPDom}},$
 $C_{\text{ToFun}})$

$$P_{\text{br}} = \sigma(C_{\text{Break}} \text{Break} + C_{\text{BackEdge}} \text{BackEdge} + C_{\text{EqZero}} \text{EqZero} + C_{\text{IsZero}} \text{IsZero} \\ + C_{\text{NoPDom}} \text{NoPDom} + C_{\text{ToFun}} \text{ToFun} + C)$$

Logistic Regression

$(C_{\text{Break}}, C_{\text{BackEdge}}, C_{\text{EqZero}}, C_{\text{IsZero}}, C_{\text{NoPDom}}, C_{\text{ToFun}})$

(Break
BackEdge
EqZero
IsZero
NoPDom
ToFun)

$$P_{\text{br}} = \sigma(C_{\text{Break}} \text{Break} + C_{\text{BackEdge}} \text{BackEdge} + C_{\text{EqZero}} \text{EqZero} + C_{\text{IsZero}} \text{IsZero} + C_{\text{NoPDom}} \text{NoPDom} + C_{\text{ToFun}} \text{ToFun} + C)$$

Logistic Regression

$$\mathbf{n} = (C_{\text{Break}}, C_{\text{BackEdge}}, C_{\text{EqZero}}, C_{\text{IsZero}}, C_{\text{NoPDom}}, C_{\text{ToFun}})$$

$$\begin{pmatrix} \text{Break} \\ \text{BackEdge} \\ \text{EqZero} \\ \text{IsZero} \\ \text{NoPDom} \\ \text{ToFun} \end{pmatrix} \times \begin{pmatrix} + \\ + \\ + \\ + \\ + \\ + \end{pmatrix} \mathbf{C}$$

$$P_{\text{br}} = \sigma(C_{\text{Break}} \text{Break} + C_{\text{BackEdge}} \text{BackEdge} + C_{\text{EqZero}} \text{EqZero} + C_{\text{IsZero}} \text{IsZero} + C_{\text{NoPDom}} \text{NoPDom} + C_{\text{ToFun}} \text{ToFun} + \mathbf{C})$$

Logistic Regression

$$n = (C_{\text{Break}}, C_{\text{BackEdge}}, C_{\text{EqZero}}, C_{\text{IsZero}}, C_{\text{NoPDom}}, C_{\text{ToFun}}) \times \begin{pmatrix} \text{Break} \\ \text{BackEdge} \\ \text{EqZero} \\ \text{IsZero} \\ \text{NoPDom} \\ \text{ToFun} \end{pmatrix} + C$$

$$P_{\text{br}} = \sigma(n)$$

$$P_{\text{br}} = \sigma(C_{\text{Break}} \text{Break} + C_{\text{BackEdge}} \text{BackEdge} + C_{\text{EqZero}} \text{EqZero} + C_{\text{IsZero}} \text{IsZero} + C_{\text{NoPDom}} \text{NoPDom} + C_{\text{ToFun}} \text{ToFun} + C)$$

Logistic Regression

$$n = (C_{\text{Break}}, C_{\text{BackEdge}}, C_{\text{EqZero}}, C_{\text{IsZero}}, C_{\text{NoPDom}}, C_{\text{ToFun}})$$

$$\begin{aligned} & \times \begin{pmatrix} \text{Break} \\ \text{BackEdge} \\ \text{EqZero} \\ \text{IsZero} \\ \text{NoPDom} \\ \text{ToFun} \end{pmatrix} + C \end{aligned}$$

$$P_{\text{br}} = \sigma(n)$$

if (P_{br}) ≥ 0.5 then "Taken" else "Not Taken"

Branch Features

Break

BackEdge

EqZero

IsZero

NoPDom

ToFun

Branch Features

 Binary

Break

BackEdge

EqZero

IsZero

NoPDom

ToFun

Branch Features

▶ Binary

▶ Static

Break

BackEdge

EqZero

IsZero

NoPDom

ToFun

Branch Features

▶ Binary

▶ Static

▶ Deterministic

Break

BackEdge

EqZero

IsZero

NoPDom

ToFun

Branch Features

▶ Binary

▶ Static

▶ Deterministic

▶ Available

Break

BackEdge

EqZero

IsZero

NoPDom

ToFun

Features

- ▶ Binary
- ▶ Static
- ▶ Deterministic
- ▶ Available

Fernando Magno Quintão Pereira, Guilherme V. Leobas, Abdoulaye Gamatié:
Static Prediction of Silent Stores.

ACM Trans. Archit. Code Optim. 15(4): 44:1-44:26 (2019)

Break

BackEdge

EqZero

IsZero

NoPDom

ToFun

Break

BackEdge

EqZero

IsZero

NoPDom

ToFun

Break

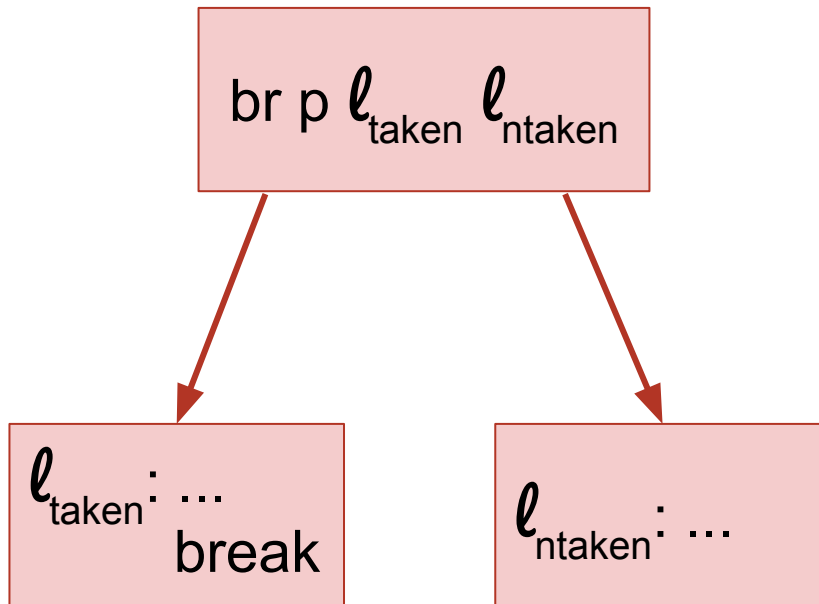
BackEdge

EqZero

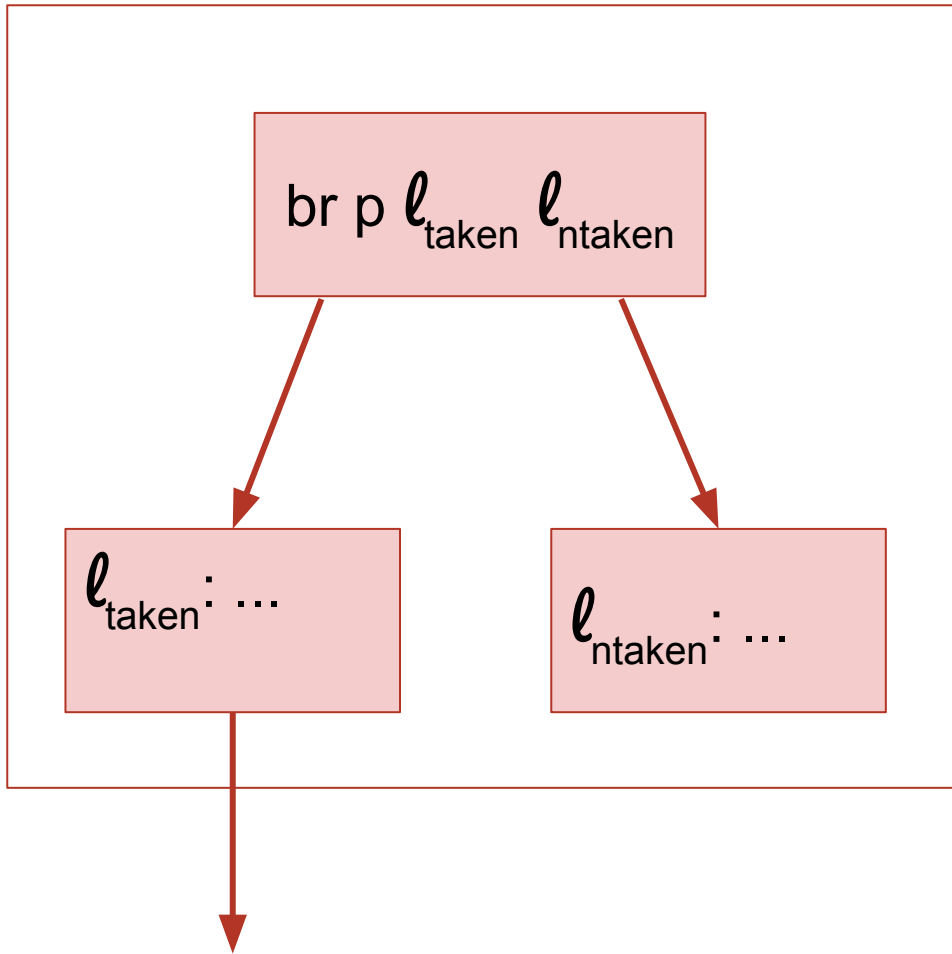
IsZero

NoPDom

ToFun)



Loop:



Break

BackEdge

EqZero

IsZero

NoPDom

ToFun)

(Break

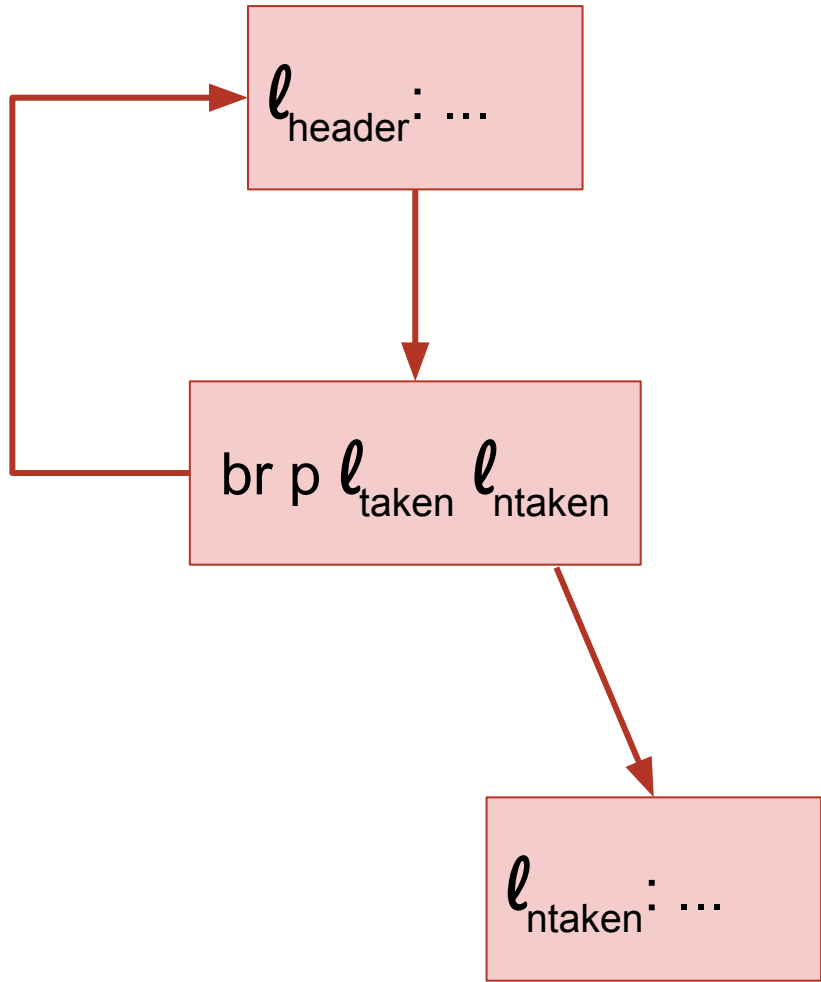
BackEdge

EqZero

IsZero

NoPDom

ToFun)



(Break
BackEdge
EqZero
IsZero
NoPDom
ToFun)

(Break

BackEdge

EqZero

IsZero

NoPDom

ToFun)

```
p = (x == 0)
```

```
br p  $\ell_{\text{taken}}$   $\ell_{\text{ntaken}}$ 
```

(Break

BackEdge

EqZero

IsZero

NoPDom

ToFun)

$p = (x == 0)$

$\text{br } p \ell_{\text{taken}} \ell_{\text{ntaken}}$

$p = (0 == x)$

$\text{br } p \ell_{\text{taken}} \ell_{\text{ntaken}}$

(Break

BackEdge

EqZero

IsZero

NoPDom

ToFun)

```
p = (x == 0)
br p ltaken lntaken
```

```
p = (0 == x)
br p ltaken lntaken
```

```
p = (0 == x)
q = !p
br p ltaken lntaken
```

(Break

BackEdge

EqZero

IsZero

NoPDom

ToFun)

(Break

BackEdge

EqZero

IsZero

NoPDom

ToFun)

(Break

BackEdge

EqZero

NonConstantOperandCouldBeZero ~~IsZero~~

NoPDom

ToFun)

```
int foo(int x, int* z) {  
    int sum = 0;  
    for (int i = 0; i < x; i++) {  
        if (z[i] == 0) {  
            sum += z[0];  
        }  
    }  
    return sum;  
}
```

(Break

BackEdge

EqZero

IsZero

NoPDom

ToFun)

What are the branches
in this example?

```
int foo(int x, int* z) {  
    int sum = 0;  
    for (int i = 0; i < x; i++) {  
        if (z[i] == 0) {  
            sum += z[0];  
        }  
    }  
    return sum;  
}
```

(Break

BackEdge

EqZero

IsZero

NoPDom

ToFun)

```
int foo(int x, int* z) {  
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        if (z[i] == 0) {  
            sum += z[0];  
        }  
    }  
    return sum;  
}
```

(Break

BackEdge

EqZero

IsZero

NoPDom

ToFun)

```
int foo(int x, int* z) {  
    int sum = 0;  
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        if (z[i] == 0) {  
            sum += z[0];  
        }  
    }  
    return sum;  
}
```

(Break

BackEdge

EqZero

IsZero

NoPDom

ToFun)

```
int foo(int x, int* z) {  
    int sum = 0;  
    for (int i = 0; i < x; i++) {  
        if (z[i] == 0) {  
            sum += z[0];  
        }  
    }  
    return sum;  
}
```

(Break

BackEdge

EqZero

IsZero

NoPDom

ToFun)

Static Analysis

```
int foo(int x, int* z) {
    int sum = 0;
    for (int i = 0; i < x; i++) {
        if (z[i] == 0) {
            sum += z[0];
        }
    }
    return sum;
}
```

(Break

BackEdge

EqZero

IsZero

NoPDom

ToFun)

Static Analysis

Can you think about a static analysis to compute this feature?

```
int foo(int x, int* z) {  
    int sum = 0;  
    for (int i = 0; i < x; i++) {  
        if (z[i] == 0) {  
            sum += z[0];  
        }  
    }  
    return sum;  
}
```

(Break

BackEdge

EqZero

IsZero

NoPDom

ToFun)

► **Static Analysis: backward slice**

Break

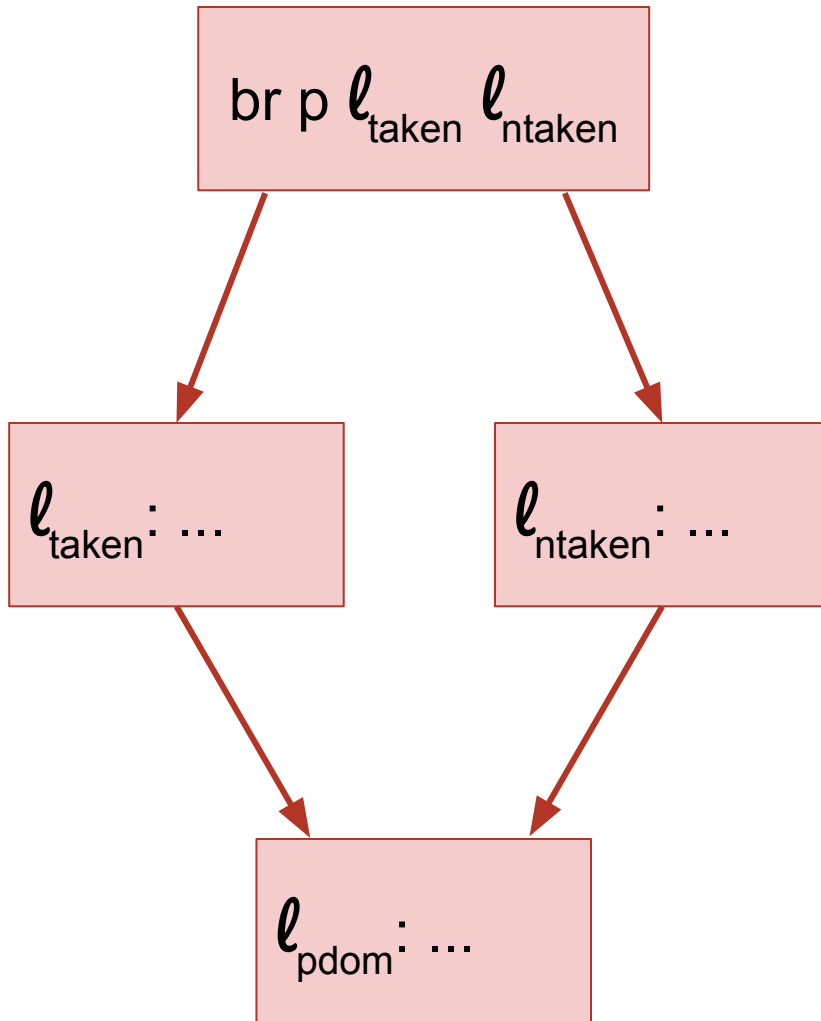
BackEdge

EqZero

IsZero

NoPDom

ToFun)



Break

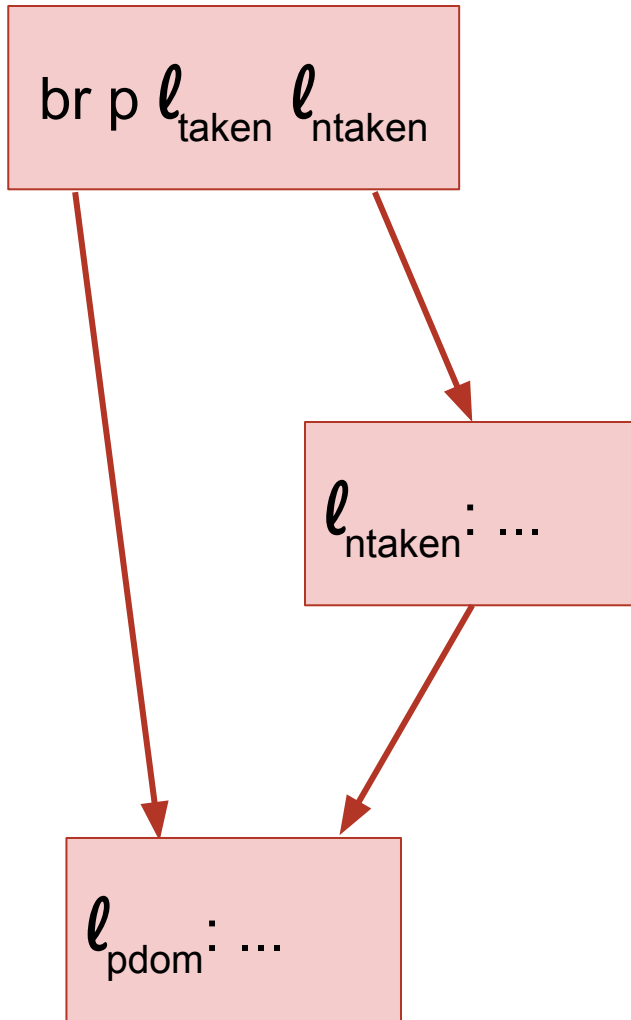
BackEdge

EqZero

IsZero

1 == NoPDom

ToFun)



Break

BackEdge

EqZero

IsZero

0 == NoPDom

ToFun)

(Break

BackEdge

EqZero

IsZero

NoPDom

ToFun

(Break

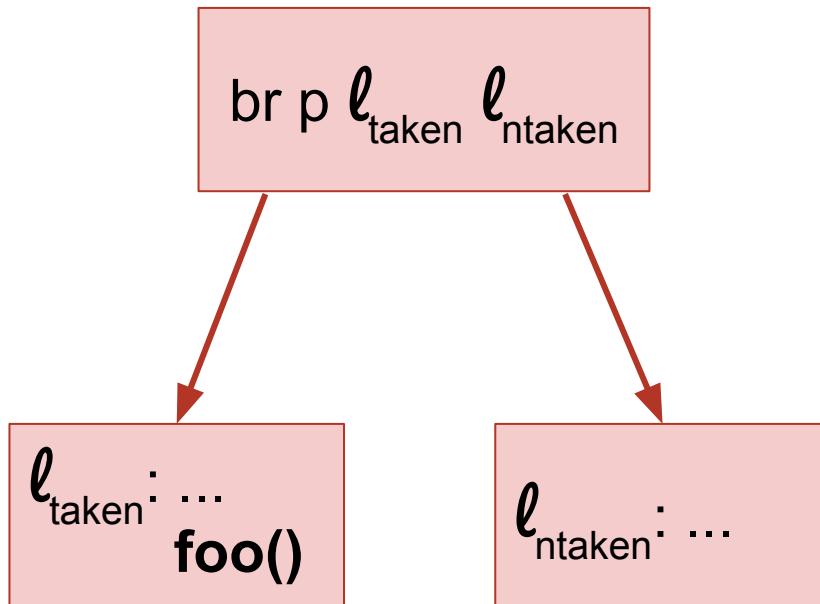
BackEdge

EqZero

IsZero

NoPDom

ToFun



Break

BackEdge

EqZero

IsZero

NoPDom

ToFun

Example: Logistic Classification in R

Example: Logistic Classification in R

https://www.dcc.ufmg.br/~fernando/classes/dcc888/ementa/data_ml/branch_features.csv

Example: Logistic Classification in R

https://www.dcc.ufmg.br/~fernando/classes/dcc888/ementa/data_ml/branch_features.csv

Branch	Break	BackEdge	EqZero	IsZero	NoPDom	ToFun	Freq	Taken
B1	0	0	0	0	0	0	1	0
B2	0	0	0	0	0	1	63	0
B3	0	0	0	0	1	0	51	0
B4	0	0	0	0	1	1	113	0
B5	0	0	0	1	0	0	46	0
B6	0	0	0	1	0	1	108	0
B7	0	0	0	1	1	0	96	0
B8	0	0	0	1	1	1	158	1
B9	0	0	1	0	0	0	19	0
B10	0	0	1	0	0	1	81	0
B11	0	0	1	0	1	0	69	0

Example: Logistic Classification in R

https://www.dcc.ufmg.br/~fernando/classes/dcc888/ementa/data_ml/branch_features.csv

Branch	Break	BackEdge	EqZero	IsZero	NoPDom	ToFun	Freq	Taken
B1	0	0	0	0	0	0	1	0
B2	0	0	0	0	0	1	63	0
B3	0	0	0	0	1	0	51	0
B4	0	0	0	0	1	1	113	0
B5	0	0	0	1	0	0	46	0
B6	0	0	0	1	0	1	108	0
B7	0	0	0	1	1	0	96	0
B8	0	0	0	1	1	1	158	1
B9	0	0	1	0	0	0	19	0
B10	0	0	1	0	0	1	81	0
B11	0	0	1	0	1	0	69	0

Example: Logistic Classification in R

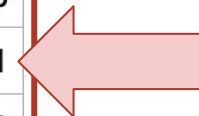
https://www.dcc.ufmg.br/~fernando/classes/dcc888/ementa/data_ml/branch_features.csv

Branch	Break	BackEdge	EqZero	IsZero	NoPDom	ToFun	Freq	Taken
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B2	0	0	0	0	0	1	63	0
B3	0	0	0	0	1	0	51	0
B4	0	0	0	0	1	1	113	0
B5	0	0	0	1	0	0	46	0
B6	0	0	0	1	0	1	108	0
B7	0	0	0	1	1	0	96	0
B8	0	0	0	1	1	1	158	1
B9	0	0	1	0	0	0	19	0
B10	0	0	1	0	0	1	81	0
B11	0	0	1	0	1	0	69	0

Example: Logistic Classification in R

https://www.dcc.ufmg.br/~fernando/classes/dcc888/ementa/data_ml/branch_features.csv

Branch	Break	BackEdge	EqZero	IsZero	NoPDom	ToFun	Freq	Taken
B1	0	0	0	0	0	0	1	0
B2	0	0	0	0	0	1	63	0
B3	0	0	0	0	1	0	51	0
B4	0	0	0	0	1	1	113	0
B5	0	0	0	1	0	0	46	0
B6	0	0	0	1	0	1	108	0
B7	0	0	0	1	1	0	96	0
B8	0	0	0	1	1	1	158	1
B9	0	0	1	0	0	0	19	0
B10	0	0	1	0	0	1	81	0
B11	0	0	1	0	1	0	69	0



Example: Logistic Classification in R

```
data <- read.csv("~/branch_features.csv")
shuffled_data <- data[sample(1:nrow(data)), ]
num_samples <- nrow(shuffled_data)
train_size <- ceiling(num_samples*0.8)
train <- shuffled_data[1:train_size,]
test <- shuffled_data[(train_size+1):num_samples,]
model <- glm(Taken ~ Break + BackEdge + EqZero + IsZero +
NoPDom + ToFun, family=binomial(link='logit'), data=train)
results <- predict(model, test, type="response")
predictions <- ifelse(results > 0.5, 1, 0)
misses <- mean(predictions != test$Taken)
accuracy <- 1 - misses
```



Example: Logistic Classification in R

```
data <- read.csv("~/branch_features.csv")  
shuffled_data <- data[sample(1:nrow(data)), ]  
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train_size <- ceiling(num_samples*0.8)  
train <- shuffled_data[1:train_size,]  
test <- shuffled_data[(train_size+1):num_samples,]  
model <- glm(Taken ~ Break + BackEdge + EqZero + IsZero +  
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Example: Logistic Classification in R

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data <- read.csv("~/branch_features.csv")
shuffled_data <- data[sample(1:nrow(data)), ]
num_samples <- nrow(shuffled_data)
train_size <- ceiling(num_samples*0.8)
train <- shuffled_data[1:train_size,]
test <- shuffled_data[(train_size+1):num_samples,]
model <- glm(Taken ~ Break + BackEdge + EqZero + IsZero +
NoPDom + ToFun, family=binomial(link='logit'), data=train)
results <- predict(model, test, type="response")
predictions <- ifelse(results > 0.5, 1, 0)
misses <- mean(predictions != test$Taken)
accuracy <- 1 - misses
```



Example: Logistic Classification in R

```
data <- read.csv("~/branch_features.csv")
```

```
shuffled_data <- data[sample(1:nrow(data)), ]
```

```
num_samples <- nrow(shuffled_data)
```

Branch	Break	BackEdge	EqZero	IsZero	NoPDom	ToFun	Freq	Taken
B1	0	0	0	0	0	0	1	0
B2	0	0	0	0	0	1	63	0
B3	0	0	0	0	1	0	51	0
B4	0	0	0	0	1	1	113	0
B5	0	0	0	1	0	0	46	0
B6	0	0	0	1	0	1	108	0
B7	0	0	0	1	1	0	96	0
B8	0	0	0	1	1	1	158	1
B9	0	0	1	0	0	0	19	0
B10	0	0	1	0	0	1	81	0
B11	0	0	1	0	1	0	69	0

```
num_samples, ]
```

```
EqZero + IsZero +  
'it'), data=train)
```

```
response")
```

```
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```



Example: Logistic Classification in R

```
data <- read.csv("~/branch_features.csv")
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shuffled_data <- data[sample(1:nrow(data)), ]
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data <- read.csv("~/branch_features.csv")
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num_samples <- nrow(shuffled_data)
train_size <- ceiling(num_samples*0.8)
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0.9166

Example: Logistic Classification in R

```
data <- read.csv("~/branch_features.csv")
shuffled_data <- data[sample(1:nrow(data)), ]
num_samples <- nrow(shuffled_data)
train_size <- ceiling(num_samples*0.6)
train <- shuffled_data[1:train_size,]
test <- shuffled_data[(train_size+1):num_samples,]
model <- glm(Taken ~ Break + BackEdge + EqZero + IsZero +
NoPDom + ToFun, family=binomial(link='logit'), data=train)
results <- predict(model, test, type="response")
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```

0.8400

Looking into the Model

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Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	-242.03	141368.40	-0.002	0.999
Break	-88.19	57995.29	-0.002	0.999
BackEdge	177.13	105428.63	0.002	0.999
EqZero	131.67	81713.77	0.002	0.999
IsZero	133.52	84777.53	0.002	0.999
NoPDom	87.37	57022.02	0.002	0.999
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$$P_{br} = \sigma(C_{Break} \text{Break} + C_{BackEdge} \text{BackEdge} + C_{EqZero} \text{EqZero} + C_{IsZero} \text{IsZero} + C_{NoPDom} \text{NoPDom} + C_{ToFun} \text{ToFun} + C)$$


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Can you come up with an interpretation for this negative coefficient?


$$P_{br} = \sigma(C_{Break} \text{Break} + C_{BackEdge} \text{BackEdge} + C_{EqZero} \text{EqZero} + C_{IsZero} \text{IsZero} + C_{NoPDom} \text{NoPDom} + C_{ToFun} \text{ToFun} + C)$$

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```
int comp(int* s, int* pw, int N) {  
    for (int i = 0; i < N; i++) {  
        if (s[i] != pw[i]) {  
            break;  
        }  
    }  
}
```

Linearity

$$P_{br} = \sigma(C_{Break} Break + C_{BackEdge} BackEdge + C_{EqZero} EqZero + C_{IsZero} IsZero + C_{NoPDom} NoPDom + C_{ToFun} ToFun + C)$$

Linearity

IsZero

EqZero

$$P_{br} = \sigma(C_{Break} Break + C_{BackEdge} BackEdge + C_{EqZero} EqZero + C_{IsZero} IsZero + C_{NoPDom} NoPDom + C_{ToFun} ToFun + C)$$

Linearity

IsZero = 0

EqZero = 1

$p = (x == 0)$

br p l_{taken} l_{ntaken}

$$P_{\text{br}} = \sigma(C_{\text{Break}} \text{Break} + C_{\text{BackEdge}} \text{BackEdge} + C_{\text{EqZero}} \text{EqZero} + C_{\text{IsZero}} \text{IsZero} + C_{\text{NoPDom}} \text{NoPDom} + C_{\text{ToFun}} \text{ToFun} + C)$$

Linearity

IsZero = 0

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p = (x == 0)
```

```
br p ltaken lntaken
```

$$P_{br} = \sigma(C_{Break} Break + C_{BackEdge} BackEdge + C_{EqZero} EqZero + C_{IsZero} IsZero + C_{NoPDom} NoPDom + C_{ToFun} ToFun + C_{Comb} IsZero * EqZero + C)$$

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IsZero = 0

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```
model <- glm(Taken ~ Break + BackEdge + EqZero + IsZero +  
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Other Examples

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Angélica Aparecida Moreira, Guilherme Ottoni, Fernando Magno Quintão Pereira:
VESPA: static profiling for binary optimization.
Proc. ACM Program. Lang. 5(OOPSLA): 1-28 (2021)

Other Examples

Brad Calder, Dirk Grunwald, M. Jones, Donald Lindsay, James Martin, Michael Mozer, B. Zorn:
Evidence-Based Static Branch Prediction Using Machine Learning.
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John Cavazos, Michael F. P. O'Boyle:
Method-specific dynamic compilation using logistic regression.
OOPSLA 2006: 229-240

Brad Calder, Dirk Grunwald, M. Jones, Donald Lindsay, James Martin, Michael Mozer, B. Zorn:
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