

The Python program below implements a solver for the reaching-definition equations on the right. We say that the function F has a fixed point X if $X = F(X)$. Let's see if "solve" below has a fixed-point.

```
def eval(IN1, OUT1, IN2, OUT2, IN3, OUT3, IN4, OUT4):
    _IN1 = set()
    _OUT1 = IN1.difference([1, 3, 4]).union([1])
    _IN2 = OUT1.union(OUT2)
    _OUT2 = IN2
    _IN3 = OUT2
    _OUT3 = IN3.difference([1, 3, 4]).union([3])
    _IN4 = OUT2
    _OUT4 = IN4.difference([1, 3, 4]).union([4])
    return (_IN1, _OUT1, _IN2, _OUT2, _IN3, _OUT3, _IN4, _OUT4)

def solve(sets):
    new_sets = eval(*sets)
    while (new_sets != sets):
        new_sets = sets
        sets = eval(*new_sets)
    return sets
```

```
print(solve([set() for i in range(8)]))
print(solve([set([1, 5]) for i in range(8)]))
```

Figure 1: Implementation of an iterative solver for the data flow equations in Figure-2.

1. What would be printed by the first call to solve in Fig-1?
2. What would be printed by the second call to solve in Fig-1?
3. Does the "solve" function always reach a fixed point, regardless of its input?

```
IN[1] = {}
OUT[1] = (IN[1] \ {1, 3, 4}) U {1}
IN[2] = OUT[1] U OUT[3]
OUT[2] = IN[2]
IN[3] = OUT[2]
OUT[3] = (IN[3] \ {1, 3, 4}) U {3}
IN[4] = OUT[2]
OUT[4] = (IN[4] \ {1, 3, 4}) U {4}
```

Figure 2: Example of data-flow equations that solve an instance of reaching-definition analysis. We omit the program that gave origin to these equations.