

## Measurement

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## Measurement in Experiments

- Measurement is a central part in empirical studies
- Software measurement is crucial to enable control of projects, products and processes

## Evaluation is Control

*"You can't control what you can't measure"*

*Tom DeMarco*

- Control comes from being able to evaluate new methods, techniques, languages and tools

## Definitions

- Measurement is the process by which numbers or symbols are assigned to attributes of entities
  - They describe these attributes according to clearly defined rules
- A measure is a mapping from the attribute of an entity to a value
  - Usually a numeric value
- Entities are objects in the real world

## Measure vs. Metric

- A measure is the number or symbol assigned to an entity to characterize an attribute
- Software metrics denote the field of measurement in software engineering
- Product metric denotes a property which is measured
  - Example: lines of code (LOC)

## Measure Validation

- To use a measure, it must be valid
  - It must not violate any necessary property of the measured attribute
  - It must be a proper mathematical characterization of the attribute
- Different objects can have the same measurement value
  - The measure must preserve our intuitive notion about the attribute

## Analytical and Empirical Validation

- Analytical validity of a measure relates to its ability to capture accurately and reliably the item of interest
- Empirical validity describes how well a score correlates to something measured in another context

## Scale and Scale Type

## Measurement Scale

- Scale defines the mapping from an attribute to a measurement
  - Meters, centimetres and inches are different scales of length
- We can transform the measure from one scale to another
  - If the transformation preserves the relationship among the objects, it is called *admissible transformation* or *rescaling*

## Meaningful Statement

- Meaningful statements are true after rescaling
- Example
  - Object A is 1 meter long
  - Object B is 2 meters long
- Statement: B is twice as long as A
  - Statement is true even if we rescale to centimetres or inches

## Meaningless Statement

- Meaningless statements are not true after rescaling
- Example
  - Room A is 10° C
  - Room B is 20° C
- Statement: B is twice as warm as A
  - The statement is no longer true if we rescale to Fahrenheit (50° F and 68° F)

## Scale Types

- Scales belonging to the same scale type share the same properties
- The most common scale types are
  - Nominal
  - Ordinal
  - Interval
  - Ratio

## Nominal Scale

- The nominal scale is the least powerful of the scale types
- It maps the attribute into a name or symbol
- Transformations preserve the one-to-one mapping
- Example: Defect type
  - Requirements, Design, Coding, etc.

## Ordinal Scale

- The ordinal scale ranks entities after an ordering criterion
  - Greater than, better than, more complex...
- Transformations preserve the order of the entities
- Example
  - Sorting systems by their complexity

## Interval Scale

- In the interval scale, the difference between two measures are meaningful
  - The value itself is not meaningful
- It orders the values as the ordinal scale
- There is a notion of relative distance between two entities
- Example
  - Temperature in Celsius and Fahrenheit

## Ratio Scale

- It is the most powerful scale type
- In a ratio scale
  - There is a meaningful zero
  - Ratio between two measures is meaningful
- Example
  - Length of an array
  - Duration of a development phase

## Qualitative vs. Quantitative

- Qualitative research is concerned with measurement mainly in the nominal and ordinal scales
- Quantitative research treats measurement on the interval and ratio scales

## Types of Measures

Objective and Subjective  
Direct and Indirect

## [ Objective Measure ]

- There is no judgement in the measurement value
- It depends only on the measured object
- It can be measured by different people and the same value is obtained
  - Within the measurement error
- Example of objective measure
  - Number of Classes

## [ Subjective Measure ]

- The person measuring makes some judgement
- The measure depends on both the object and the viewpoint
- Its value can vary if the object is measured by different people
- Example of subjective measure
  - Programming skill of a developer

## [ Direct and Indirect Measures ]

- Direct Measure
  - It does not involve measurements of other attributes
  - Example: Defects found in tests
- Indirect Measure
  - It is derived from other measures
  - Example: Defect Density (defects divided by lines of code)

## Measurement in Software Engineering

## [ Object of Measurement ]

- The object can be divided into process, product, and resources
  - Process: describes which activities are needed to produce software
  - Product: the artefacts, deliverables or documents that results from an activity
  - Resources: are personnel, hardware or software needed for a process activity

## [ Internal and External Attributes ]

- Internal attribute can be measured purely in terms of the object
- External attribute can only be measured with respect to how objects relates to other objects
  - External attributes are mostly indirect measures and must be derived from internal attributes

## Examples of Measures

Class	Object	Attribute	Measure
Process	Testing	Internal	Effort
		External	Cost
Product	Code	Internal	Size
		External	Reliability
Resource	Personnel	Internal	Age
		External	Productivity

## Challenges in SE

- It is often sometimes hard to define an attribute in a measurable way
- Validation of indirect metrics is difficult
  - We have to validate the underlying model and the direct metrics
- It is difficult to prove that the measures are in a ratio scale (most powerful one)
  - Statistical analysis depends on the scale type

## Metric Collection

- Metrics should not require too much effort to be collected
- How to collect metrics?
  - Manual: e.g., subjects fill out forms
  - Automatic: e.g., development environment is instrumented
- The quality of the collected metrics is the basis for further analysis

## Analysis of Metrics

- It is important to understand what kind of metrics were collected
- Example of issues
  - Scale type: the most powerful statistical analyses require the ratio scale
  - Distribution: it is important to verify if measures are normally distributed
- Ratio of two metrics (A/B) should be used carefully

## Bibliography

- C. Wohlin et al. **Experimentation in Software Engineering**, Springer. 2012.
  - Chapter 3 - Measurement