

CS:3820

Programming Language Concepts

Imperative languages, environment and store, micro-C

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Overview

- A Naive imperative language
- C concepts
 - Pointers and pointer arithmetic, arrays
 - Lvalue and rvalue
 - Parameter passing by value and by reference
 - Expression statements
- Micro-C, a subset of C
 - abstract syntax
 - lexing and parsing
 - interpretation

Imperative Programming

- Based on *stateful* computation
- A *state* is a mapping from variables to values
- (Terminating) programs start with an initial state and end with a final state
- Programs are sequences of *statements*
- Each statement modifies the current state
- Statements may contain *expressions*, which are evaluated to *values*
- Some expressions have also the *side effect* of modifying the store

A naive-store imperative language

- **Naive** store model:
 - a variable name maps to an integer value
 - a store is just a runtime environment

```
sum = 0;  
for i = 0 to 100 do  
    sum = sum + i;
```

i	100
sum	5050

```
i = 1;  
sum = 0;  
while sum < 10000 do begin  
    sum = sum + i;  
    i = 1 + i;  
end;
```

i	142
sum	10011

Naive-store statement execution, 1

- Executing a statement gives a new store
- Assignment $x = e$ updates the store
- Expressions do not affect the store

```
let rec exec stmt (store : naivestore) : naivestore =  
  match stmt with  
  | Asgn(x, e) ->  
    setSto store (x, eval e store)  
  | If(e1, stmt1, stmt2) ->  
    if eval e1 store <> 0 then exec stmt1 store  
    else exec stmt2 store  
  | ...
```

Update store
at x with
value of e

Naive-store statement execution, 2

- A block $\{s_1; \dots; s_n\}$ executes s_1 then $s_2 \dots$
- Example:

```
exec (Block [s1; s2]) store // F# interpreter
= loop [s1; s2] store
= exec s2 (exec s1 store)
```

```
let rec exec stmt (store : naivestore) : naivestore =
  match stmt with
  | Block stmts ->
    let rec loop ss sto =
      match ss with
      | [] -> sto
      | s1::sr -> loop sr (exec s1 sto)
    loop stmts store
  | ...
```

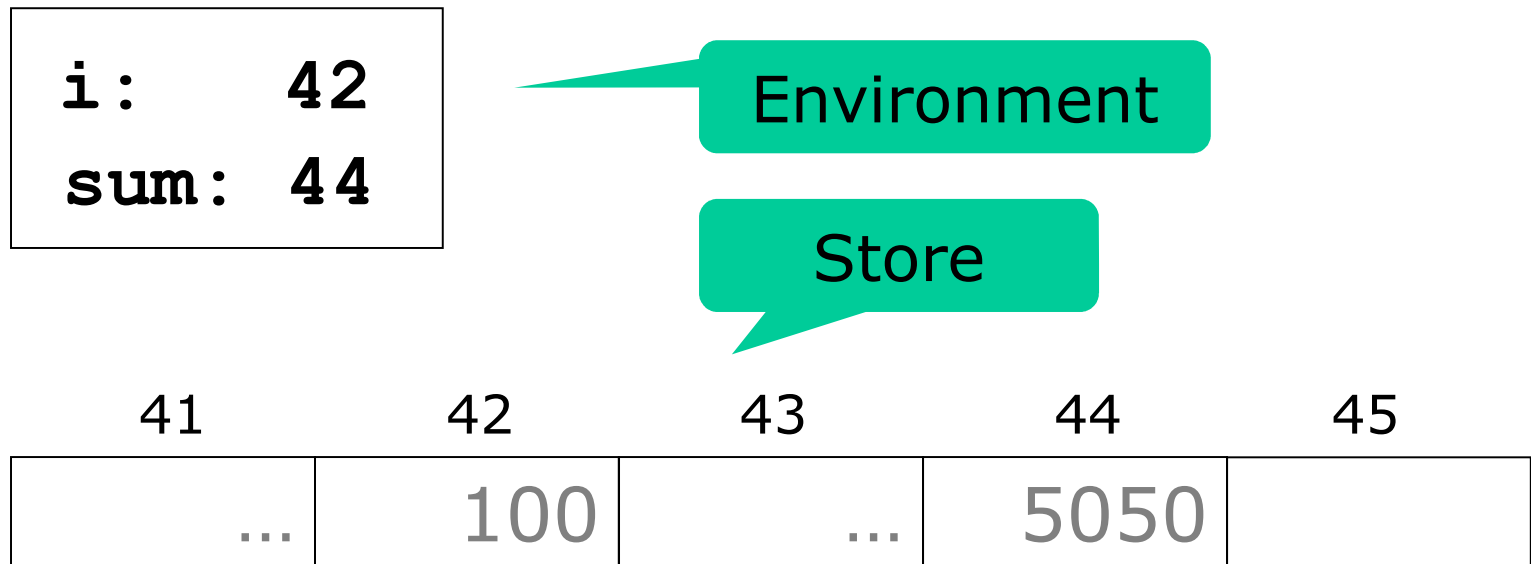
Naive-store statement execution, 3

- `for` and `while` update the store sequentially

```
let rec exec stmt (store : naivestore) : naivestore =  
  match stmt with  
  | ...  
  | For(x, estart, estop, stmt) -> ...  
  | While(e, stmt) ->  
    let rec loop sto =  
      if eval e sto = 0 then sto  
      else loop (exec stmt sto)  
    loop store
```

Environment and store, micro-C

- The naive model cannot describe *pointers* and *variable aliasing*
- A more realistic store model:
 - *Environment* maps a variable name to an address
 - *Store* maps address to value



The essence of C: Pointers

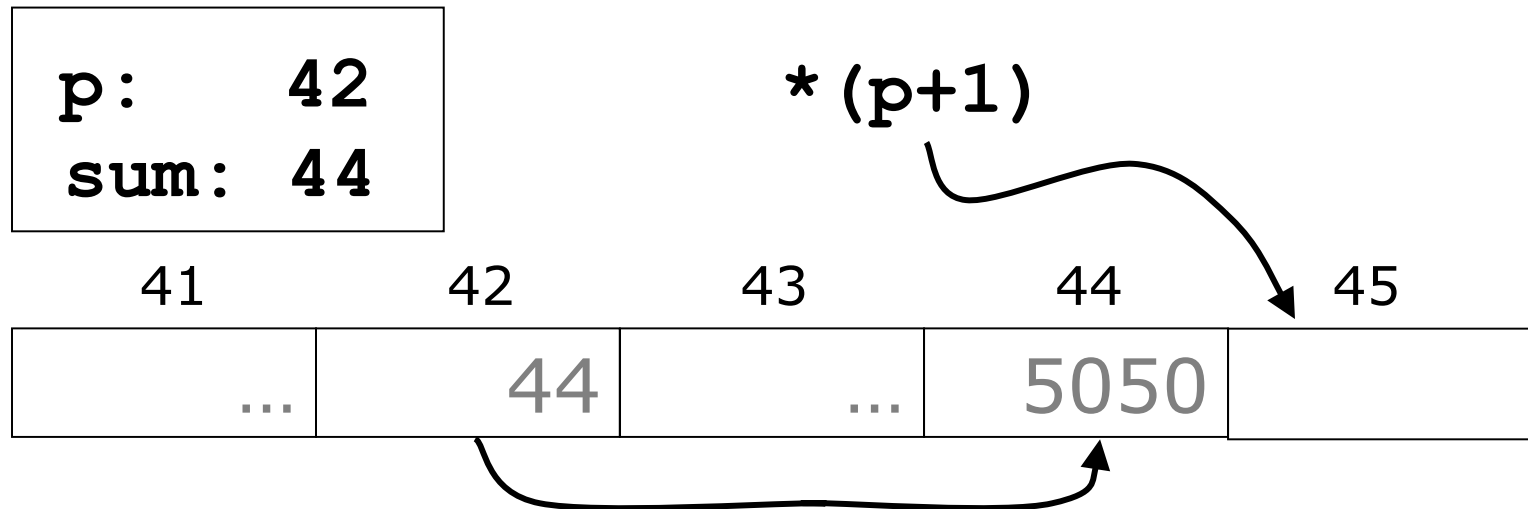
- Main innovations of C (1972) over Algol 60:
 - Structs, as in COBOL and Pascal
 - Pointers, pointer arithmetic, pointer types, array indexing as pointer indexing
 - Syntax: { } for blocks, as in C++, Java, C#
- Very different from Java and C#, which have no pointer arithmetic, but garbage collection

Desirable language features

	C	C++	F#/ML	Smtalk	Haskell	Java	C#
Garbage collection							
Exceptions							
Bounds checks							
Static types							
Generic types (para. polym.)							
Pattern matching							
Reflection							
Refl. on type parameters							
Anonymous functions (λ)							
Streams							
Lazy eval.							

C variable basics

- A variable x refers to an address (storage location)
- Addresses are mapped to values in the store
- *Pointers* are variables whose values is an address



C variable basics

- What a variable **x** refers to depends on its position in a statement
- It can be:
 - *the content of **x** 's storage location* (rvalue), as in
x + 4
 - *the storage location itself* (lvalue), as in
x = y + 4

C pointer basics

- The value of a pointer **p** is a storage location (address)
- Depending on context, the dereference expression ***p** means:
 - *the content of the location* (rvalue), as in
***p + 4**
 - *the storage location itself* (lvalue), as in
***p = x + 4**

C pointer basics

- The pointer that points to `x` is `&x`
- Pointer arithmetic:
 - `*(p+1)` is the content of the loc just after `p`
- If `p` equals `&a[0]`
then `*(p+i)` equals `p[i]` equals `a[i]`,
so an array is a pointer
- `a[0]` equals `*a`

Lvalue and rvalue of an expression

- Rvalue is *usual* value, on right-hand side of assignment: `17`, `true`
- Lvalue is *location*, on left-hand side of assignment: `x`, `a[2]`
- In assignment `e1 = e2`, expression `e1` must have lvalue

	Has lvalue	Has rvalue
<code>x</code>	yes	yes
<code>a[2]</code>	yes	yes
<code>*p</code>	yes	yes
<code>x+2</code>	no	yes
<code>&x</code>	no	yes

C variable declarations

Declaration	Meaning
int n	n is an integer
int *p	p is a pointer to integer
int ia[3]	ia is array of 3 integers
int *ipa[4]	ipa is array of 4 pointers to integers
int (*iap)[3]	iap is pointer to array of 3 integers
int **p	p is a pointer to a pointer to an integer

Unix program `cdecl` or www.cdecl.org may help:

```
cdecl> explain int *(*ipap)[4]
declare ipap as pointer to array 4 of pointer to int
cdecl> declare n as array 7 of pointer to pointer to int
int **n[7]
```

Using pointers for return values

Example ex5.c, computing square(x):

```
void main(int n) {  
    ...  
    int r;  
    square(n, &r);  
    print r;  
}  
  
void square(int i, int *rp) {  
    *rp = i * i;  
}
```

for input

for return value: a
pointer to where to
put the result

Recursion and return values

Computing factorial with micro-C/ex9.c

```
void main(int i) {
    int r;
    fac(i, &r);
    print r;
}

void fac(int n, int *res) {
    if (n == 0)
        *res = 1;
    else {
        int tmp;
        fac(n-1, &tmp);
        *res = tmp * n;
    }
}
```

- **n** is input parameter
- **res** is output parameter:
a pointer to where to
put the result
- **tmp** holds the result
of the recursive call
- **&tmp** gets a pointer
to **tmp**

Possible evaluation of main(3)

main(3):

fac(3, 117):

&r is 117

fac(2, 118):

&tmp is 118

fac(1, 119):

&tmp is 119

fac(0, 120):

&tmp is 120

*120 = 1

*119 = 1 * 1

n is 1

*118 = 1 * 2

n is 2

*117 = 2 * 3

n is 3

print 6

...

117

118

119

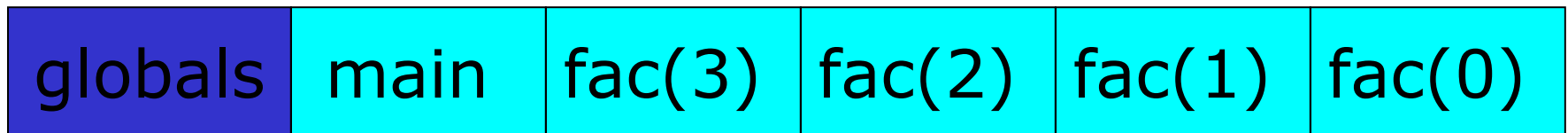
120

121

...	6	2	1	1	...
-----	---	---	---	---	-----

Storage model for micro-C

- The store is an indexable stack
 - Bottom: global variables at fixed addresses
 - Plus, a stack of activation records



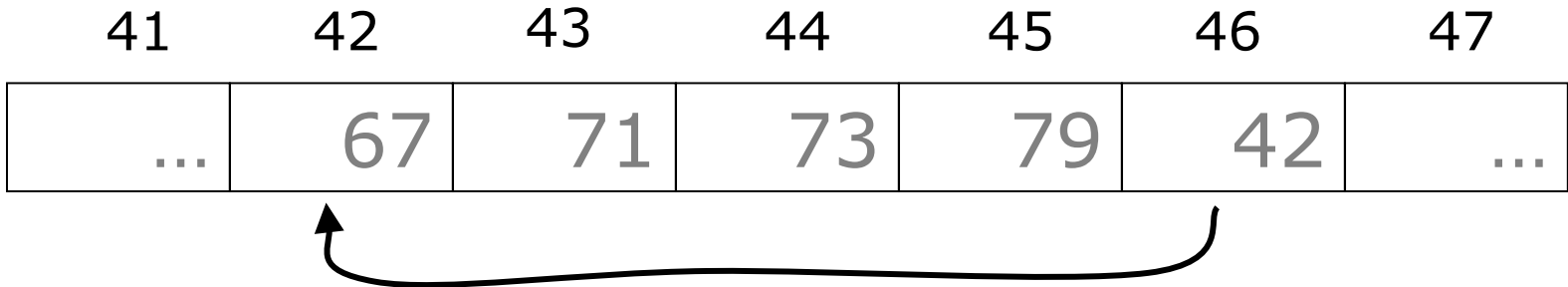
- An *activation record* is an executing function
 - return address and other administrative data
 - parameters and local variables
 - temporary results



Micro-C array layout

- An array `int a[4]` consists of
 - its 4 `int` elements
 - a pointer to `a[0]`

<code>a: 46</code>



Operators **&x** and ***p** are inverses

x:	41
y:	45
p:	42

41	42	43	44	45
1	45	7	8	6

- The address-of operator **&** in **&e**
 - evaluates **e** to its lvalue (address) and returns it as an rvalueEx: **&x == 41, &p == 42**
- The dereferencing operator ***** in ***e**
 - evaluates **e** to its rvalue and returns as an lvalueEx: ***p** *is effectively the same as y*
- It follows that
 1. **&(*e)** equals **e** Ex: **&(*p) == &y == 45 == p**
 2. ***(&e)** equals **e**,
provided **e** has lvalue Ex: ***(&y) == *45 == 6 == y**

Modifying input parameters

```
int a = 11;  
int b = 22;  
swap1(a, b);  
swap2(&a, &b);
```

a: 41
b: 42

addresses

incorrect

```
static void swap1(int x, int y) {  
    int tmp = x; x = y; y = tmp;  
}
```

x: 43
y: 44
tmp: 45

correct

```
static void swap2(int *p, int *q) {  
    int tmp = *p; *p = *q; *q = tmp;  
}
```

x: 41
y: 42
tmp: 43

store

41	42	43	44	45
11	22	22	11	11

Micro-C syntactic concepts

Types

`int`

`int *x`

`int x[4]`

Abstract Syntax

`TypI`

`TypP (TypI)`

`TypA (TypI, Some 4)`

Expressions

`(*p + 1) * 12`

Statements

`if (x != 0) y = 1/x;`

Declarations

- of global or local variables

`int x;`

- of global functions

`void swap(int *x, int *y) { ... }`

micro-C abstract syntax

```
type typ =
  | TypI                      (* Type int                *)
  | TypC                      (* Type char            *)
  | TypA of typ * int option  (* Array type           *)
  | TypP of typ               (* Pointer type          *)

and expr =
  | Access of access          (* x or *p or a[e]      *)
  | Assign of access * expr   (* x=e or *p=e or a[e]=e *)
  | Addr of access            (* &x or &*p or &a[e]    *)
  | CstI of int               (* Constant              *)
  | Prim1 of string * expr    (* Unary primitive operator *)
  | Prim2 of string * expr * expr (* Binary primitive operator *)
  | Andalso of expr * expr    (* Sequential and        *)
  | Orelse of expr * expr     (* Sequential or         *)
  | Call of string * expr list (* Function call f(...) *)

and access =
  | AccVar of string          (* Variable access      x *)
  | AccDeref of expr          (* Pointer dereferencing *p *)
  | AccIndex of access * expr (* Array indexing      a[e] *)

and stmt =
  | If of expr * stmt * stmt  (* Conditional           *)
  | While of expr * stmt      (* While loop            *)
  | Expr of expr              (* Expression statement  e; *)
  | Return of expr option     (* Return from method    *)
  | Block of stmtordec list   (* Block: grouping and scope *)

and stmtordec =
  | Dec of typ * string        (* Local variable declaration *)
  | Stmt of stmt               (* A statement              *)

and topdec =
  | Fundec of typ option * string * (typ * string) list * stmt
  | Vardec of typ * string

and program =
  | Prog of topdec list
```

Types

rvalue

Expressions

lvalue

Statements

Declarations

Interpreting Micro-C in F#

Interpreter data:

- **locEnv**, *environment* mapping local variable names to store addresses
- **gloEnv**, *environment* mapping global variable names to store addresses, and global function names to (parameter list, body statement)
- **store**, *store* mapping addresses to (integer) values

Main interpreter functions:

exec: `stmt -> locEnv -> gloEnv -> store -> store`

eval: `expr -> locEnv -> gloEnv -> store -> int * store`

access: `access -> locEnv -> gloEnv -> store ->
 address * store`

Interpreter's functions

`run: program -> int list -> store`

`(run p [a1; ...; an])`

Execute program `p` by initializing global vars and then calling `p`'s `main` function with args `a1; ...; an`, returning final store

`exec: stmt -> locEnv -> gloEnv -> store -> store`

`(exec sta lenv genv sto)`

Execute statement `sta` in local env `lenv` and global env `genv` and store `sto`, returning updated store

`stmtordec: stmtordec -> locEnv -> gloEnv -> store ->
locEnv * store`

`(stmtordec sd lenv genv sto)`

Execute statement or declaration `sd` in local env `lenv` and global env `genv` and store `sto`, returning updated local env and store

Interpreter's functions

`eval: expr -> locEnv -> gloEnv -> store -> int * store`
`(eval e lenv genv st)`

Evaluate expression `e` in local env `lenv` and global env `genv` and store `sto`, returning `e`'s result and updated store

`access: access -> locEnv -> gloEnv -> store ->`
`address * store`
`(access a lenv genv st)`

Evaluate access expression `a` in local env `lenv` and global env `genv` and store `sto`, returning an address and updated store

`allocate: typ * string -> locEnv -> store ->`
`locEnv * store`
`(allocate t x lenv sto)`

Bind var `x` in local env `lenv` and allocate space for `x` in store `sto`, returning updated env and store

Micro-C statement execution

As with the naive language, but two envs:

```
let rec exec stmt locEnv gloEnv store : store =  
  match stmt with  
  
  | If(e, stmt1, stmt2) ->  
    let (v, store1) = eval e locEnv gloEnv store  
    if v <> 0 then exec stmt1 locEnv gloEnv store1  
    else exec stmt2 locEnv gloEnv store1  
  
  | While(e, body) ->  
    let rec loop store1 =  
      let (v, store2) = eval e locEnv gloEnv store1  
      if v<>0 then loop (exec body locEnv gloEnv store2)  
      else store2  
    in loop store  
  
  | ...
```

Expression statements in C, C++, Java and C#

- The “assignment statement”

x = 2+4 ;

is really an expression

x = 2+4

followed by a semicolon

Value: none
Effect: change x

Value: 6
Effect: change x

- The semicolon means: ignore value

```
let rec exec stmt locEnv gloEnv store : store =  
  match stmt with  
  | ...  
  | Expr e ->  
    let (_, store1) = eval e locEnv gloEnv store  
    store1
```

Evaluate expression
then ignore its value

Micro-C expression evaluation, 1

- Evaluation of an expression
 - takes local and global env and a store
 - gives a resulting *rvalue* and a *new store*

```
and eval e locEnv gloEnv store : int * store =  
  match e with  
  | ...  
  | CstI i -> (i, store)  
  | Prim2(op, e1, e2) ->  
    let (i1, store1) = eval e1 locEnv gloEnv store in  
    let (i2, store2) = eval e2 locEnv gloEnv store1 in  
    let res =  
      match op with  
      | "*" -> i1 * i2  
      | "+" -> i1 + i2  
      | ...  
    in  
    (res, store2)
```

Micro-C expression evaluation, 2

- To evaluate access expression **x**, ***p**, **arr[i]**
 - find its lvalue, as a location **loc**
 - look up the rvalue in the store, as **store1[loc]**
- To evaluate **&e**
 - just evaluate **e** as lvalue
 - return the lvalue

rvalue

```
eval e locEnv gloEnv store : int * store =  
  match e with  
  | Access acc ->  
    let (loc, store1) = access acc locEnv gloEnv store  
    (getSto store1 loc, store1)  
  
  | Addr acc -> access acc locEnv gloEnv store  
  | ...
```

Micro-C access evaluation, to *lvalue*

- A variable x is looked up in environment
- A dereferencing $*e$ just evaluates e to an address
- An array indexing $a[e]$
 - evaluates a to address k , then gets $v = \text{store}[k]$
 - evaluates e to rvalue index i
 - returns address $v+i$

lvalue

```
access acc locEnv gloEnv store : int * store =  
  match acc with  
  | AccVar x                -> (lookup (fst locEnv) x, store)  
  
  | AccDeref e              -> eval e locEnv gloEnv store  
  
  | AccIndex(a, e) ->  
    let (k, store1) = access a locEnv gloEnv store  
    let v = getSto store1 k  
    let (i, store2) = eval e locEnv gloEnv store1  
    (v + i, store2)
```

Lexer specification for Micro-C

- New: endline comments // blah blah
and delimited comments if (x /* y? */)

```
rule Token = parse
| ...
| "//"          { EndLineComment lexbuf; Token lexbuf }
| "/*"          { Comment lexbuf; Token lexbuf }
```

```
and EndLineComment = parse
| ['\n' '\r']    { () }
| (eof | '\026') { () }
| _              { EndLineComment lexbuf }
```

```
and Comment = parse
| "/*"          { Comment lexbuf; Comment lexbuf }
| "*/"          { () }
| ['\n' '\r']    { Comment lexbuf }
| (eof | '\026') { lexerError lexbuf "Unterminated" }
| _              { Comment lexbuf }
```

Parsing C variable declarations

- Hard, declarations are *mixfix*: `int *a[4]`
- Parser trick: Parse a variable declaration as a type followed by a variable description:

`int *x[4]`

type info

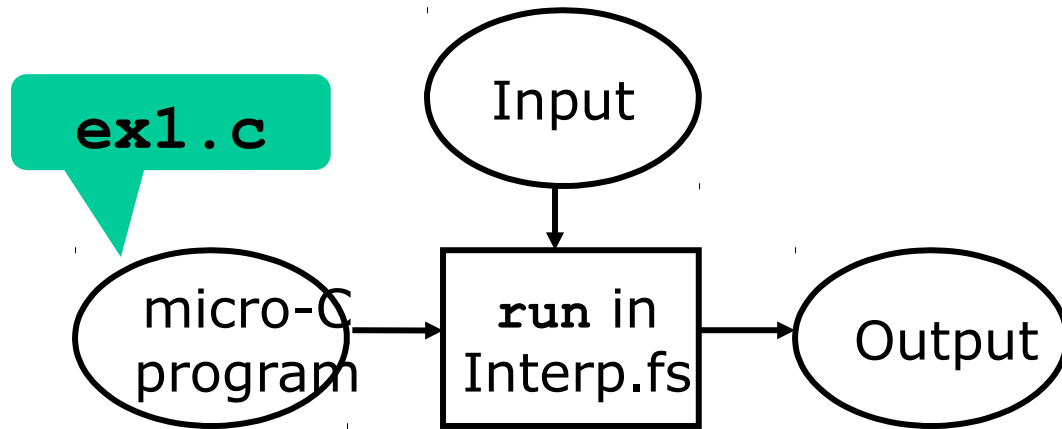
`TypI`

`((fun t -> TypA (TypP t, Some 4)), "a")`

- Parse var description to get pair $(\mathbf{f}, \mathbf{x})$ of type function $\mathbf{f}$, and variable name $\mathbf{x}$
- Apply $\mathbf{f}$ to the declared type to get type of $\mathbf{x}$
`Vardec(TypA(TypP TypI, Some 4), "a")`

Micro-C, interpreter and compiler

- So far: Interpretation of micro-C



- Next: Compilation of micro-C

